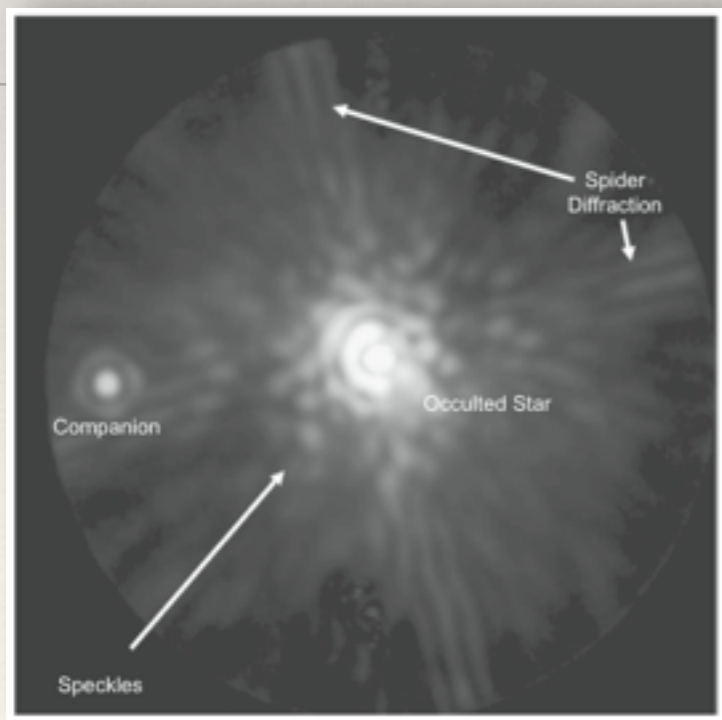


R. Claudi - INAF - Astronomical Observatory of Padova

DIRECT IMAGING OF EXTRASOLAR PLANETS

III: ADAPTIVE OPTICS



*1st ADVANCED SCHOOL OF EXOPLANETARY SCIENCE
METHODS OF DETECTING EXOPLANETS
MAY 25-29, 2015 - VIETRI SUL MARE (SA)*



Adaptive Optics

AO: the very beginning ...



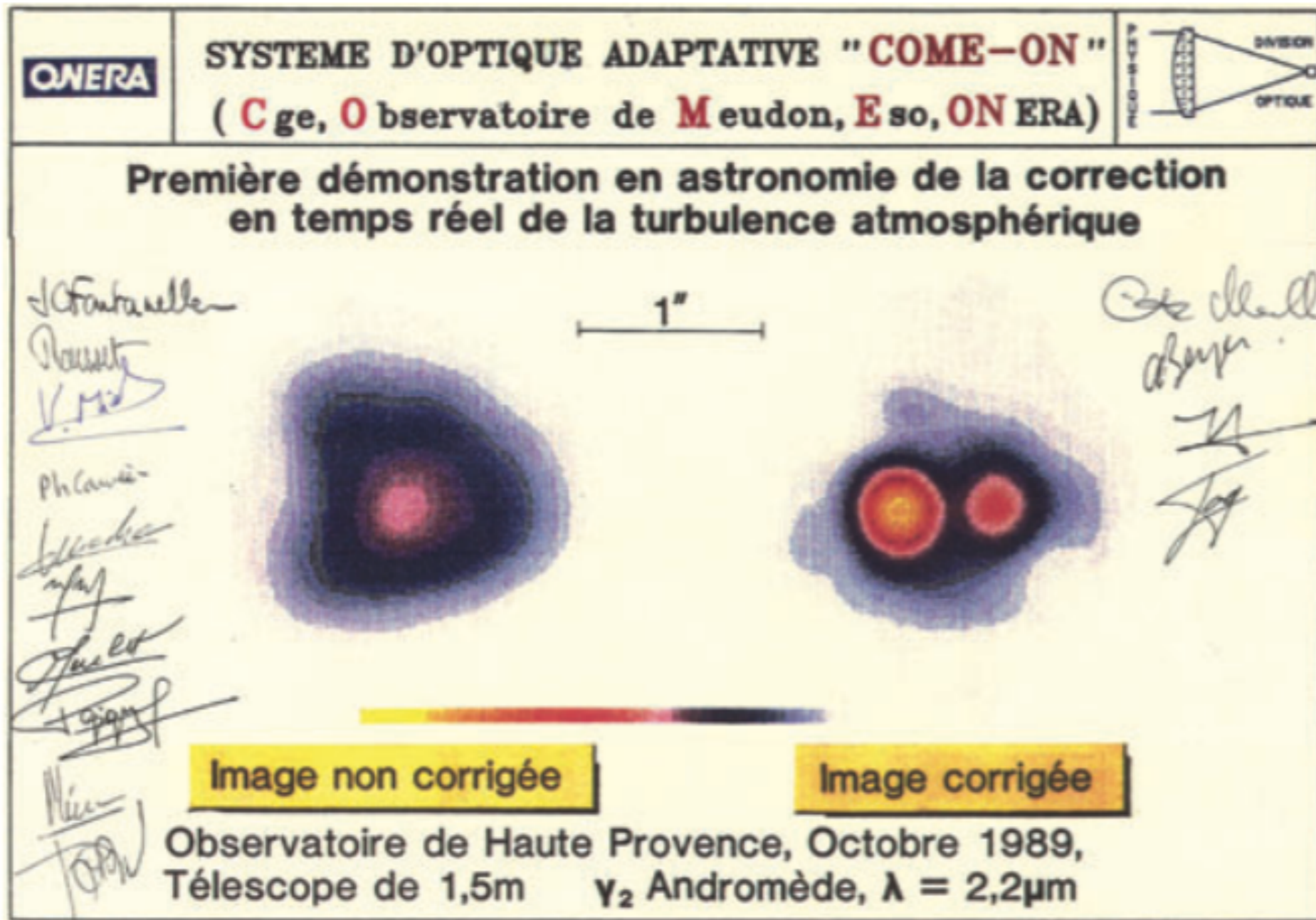
Mt. Wilson



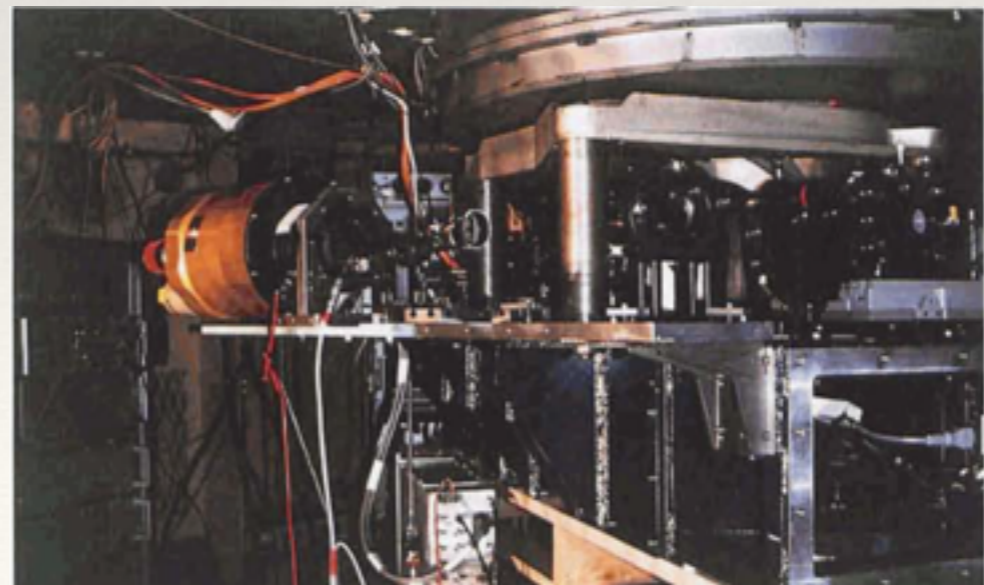
If we had the means of continually measuring the deviation of rays from all parts of the mirror, and of amplifying and feeding back this information so as to correct locally the figure of the mirror in response to the schlieren pattern, we could expect to compensate both for the seeing and for any inherent imperfection of the optical figure

Babcock 1953, Publ. Astron. Soc. Pac. 65:229

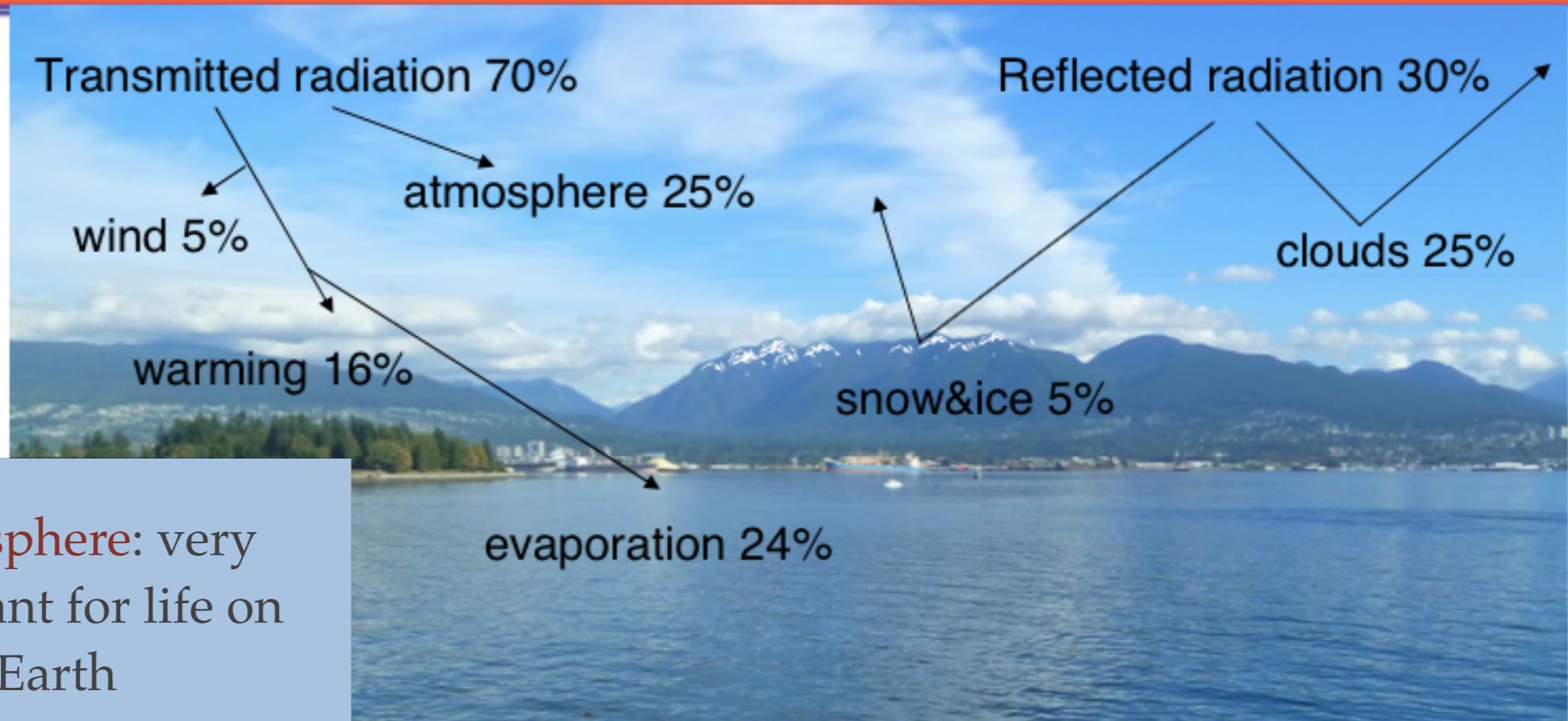
In the late 1980s **COME-ON** was tested at the 1.52-m telescope (Merkle et al. 1989, 1989. *Messenger* 58:1, Rousset et al. 1990, *Astron. Astrophys.* 230:L29) of the Observatoire de Haute-Provence and later installed at **ESO's 3.6-m telescope on La Silla in Chile** (Rigaut et al. 1991, *Astron. Astrophys.* 250:280).



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Earth's Atmosphere



Atmosphere: very important for life on Earth

Day-time: Sun shield (UV radiation)

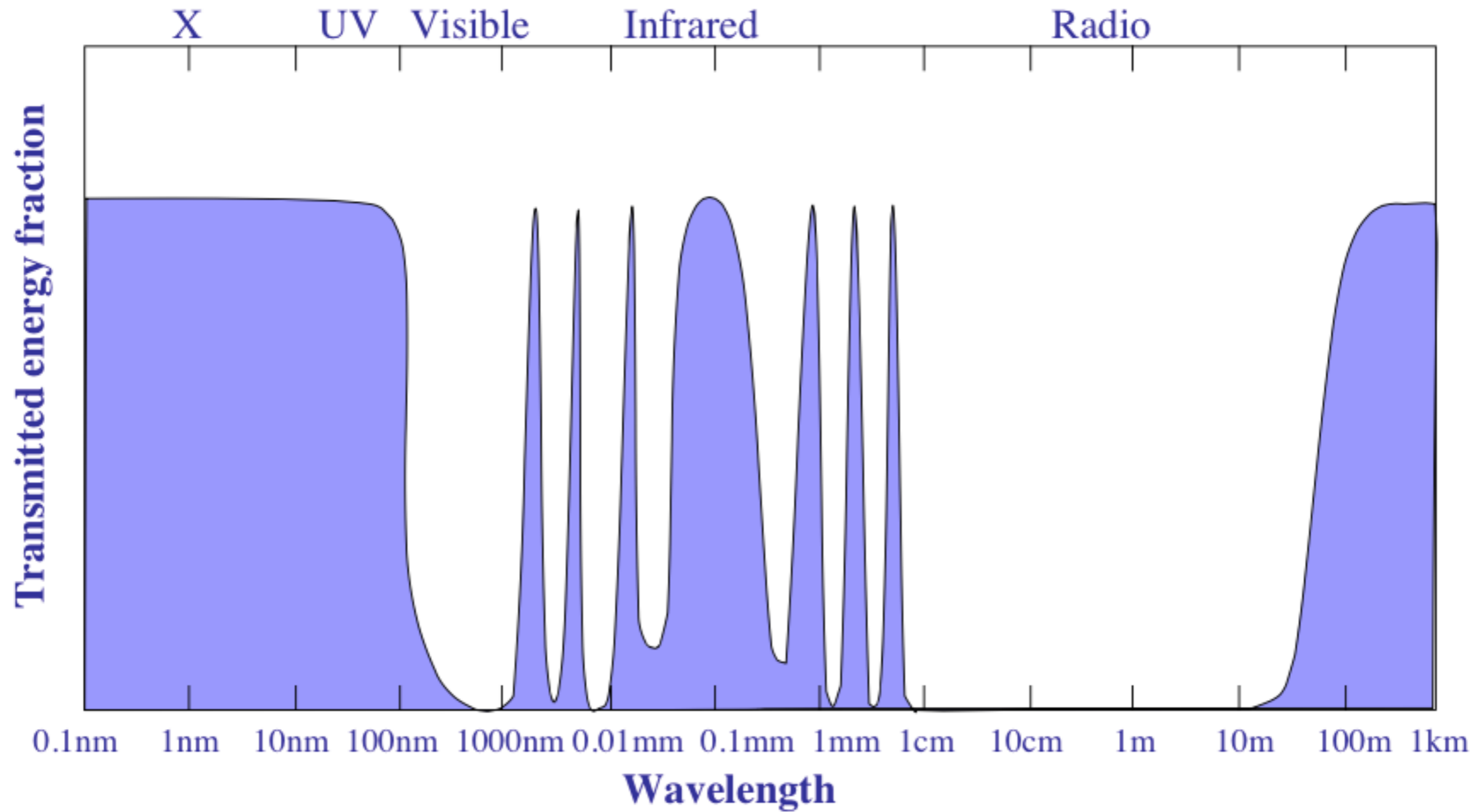
Night-time: low thermal excursion

Absorbes part of the radiation

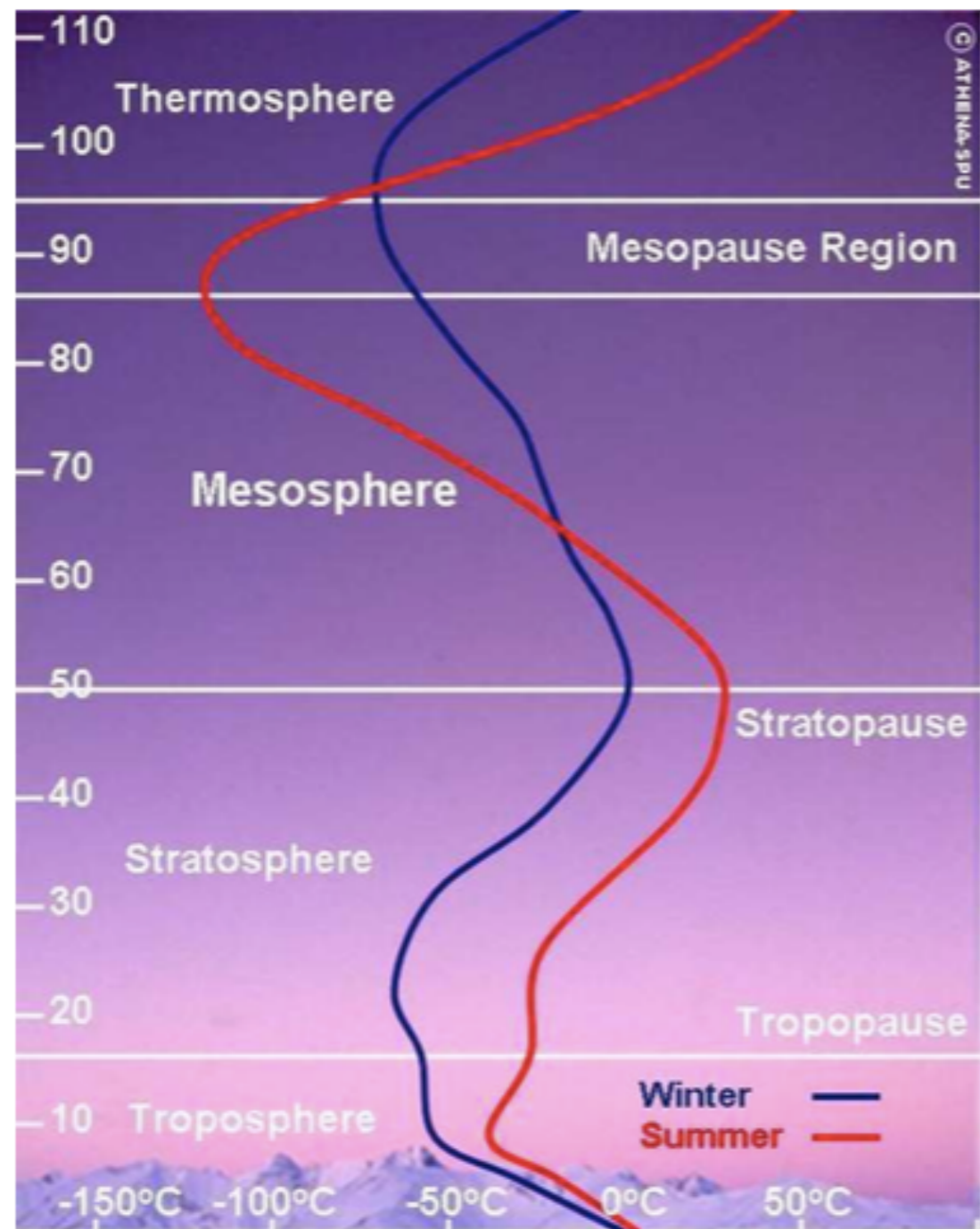
Deformation of the light coming from astronomical objects



Atmospheric Absorption



Atmospheric Structure



Troposphere

Lower part: ~10 km

Contains about 80% of the total atmospheric mass

Tropopause

Thermal inversion zone

Height ~10 km (16 km @ equator and 9 km @ poles)

Stratosphere

~10 to 50 km height

O₃ molecules → The temperature increases

Mesosphere

Extends up to about 90 km

Negative thermal gradient

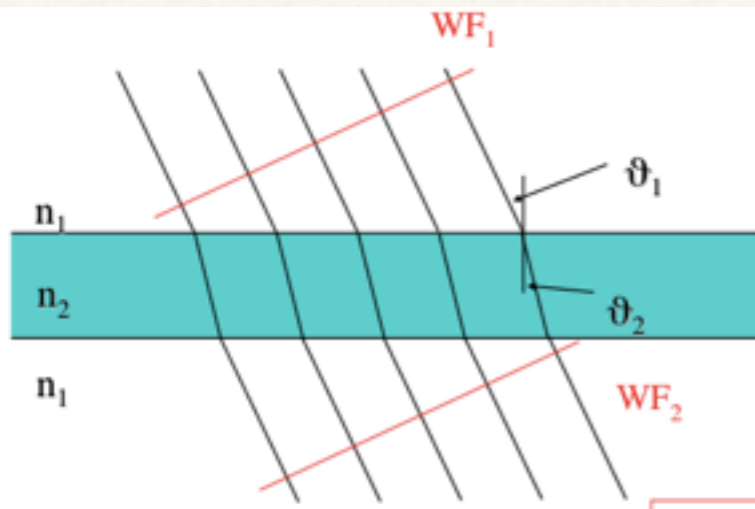
Mesopause

Coldest layer of the atmosphere (no solar heating, CO₂ radiative cooling)

Sodium Layer

Thermosphere

...rarified air



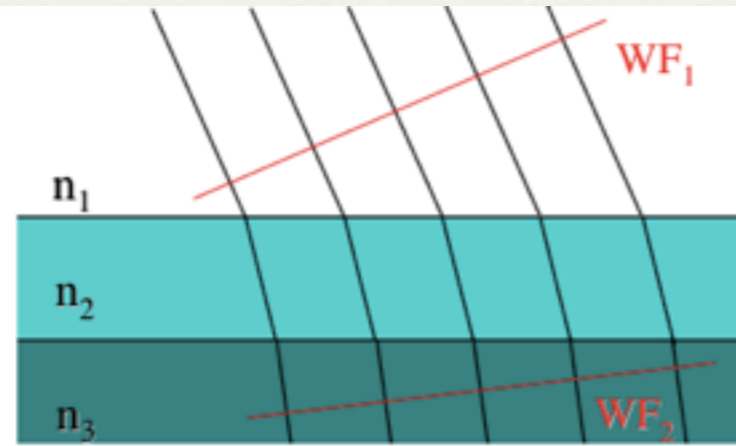
Snell Law
 $n_1 \sin \vartheta_1 = n_2 \sin \vartheta_2$

$$WF_1 = WF_2$$

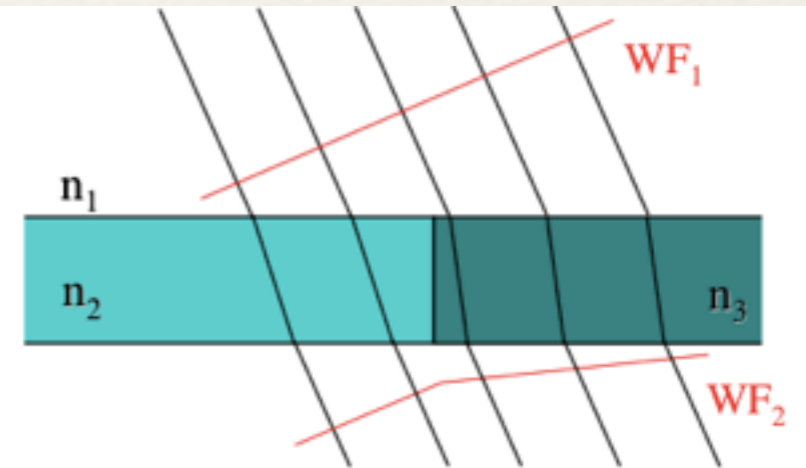
...only shift...

Ideal Atmosphere!

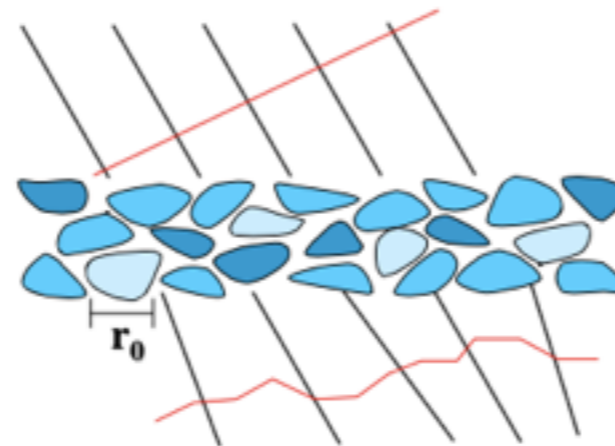
Real Atmosphere!



$$WF_1 = WF_2 + \text{inclination}$$



$$WF_1 = WF_2 + \text{deformation}$$

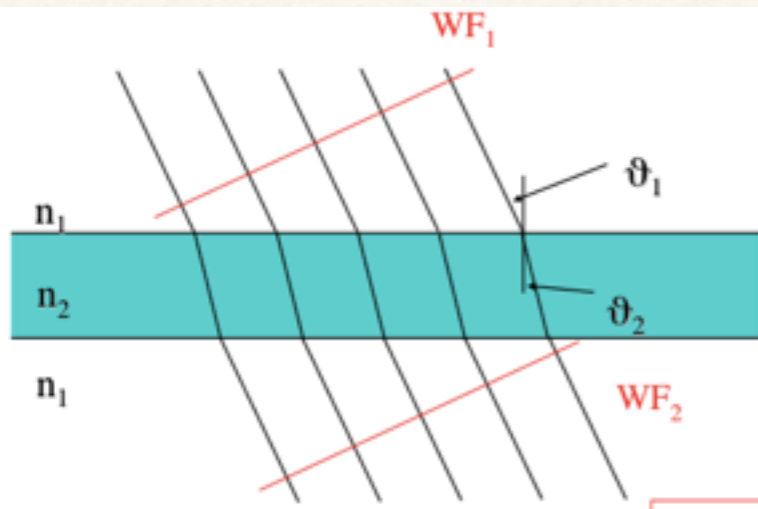


Cauchy equation:

$$n - 1 = \frac{77 \times 10^{-6}}{T} (1 + 7.52 \times 10^{-3} \lambda^{-2}) (P + 4810 \frac{P}{T})$$

Gladstone Equation:

$$n - 1 = 77 \times 10^{-6} \frac{P}{T}$$



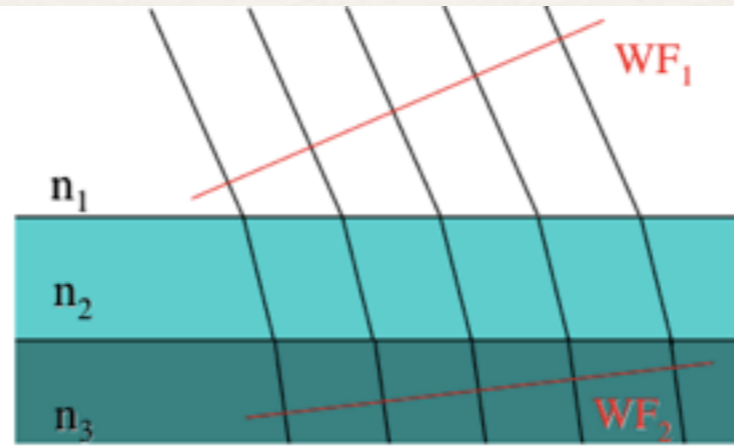
Snell Law
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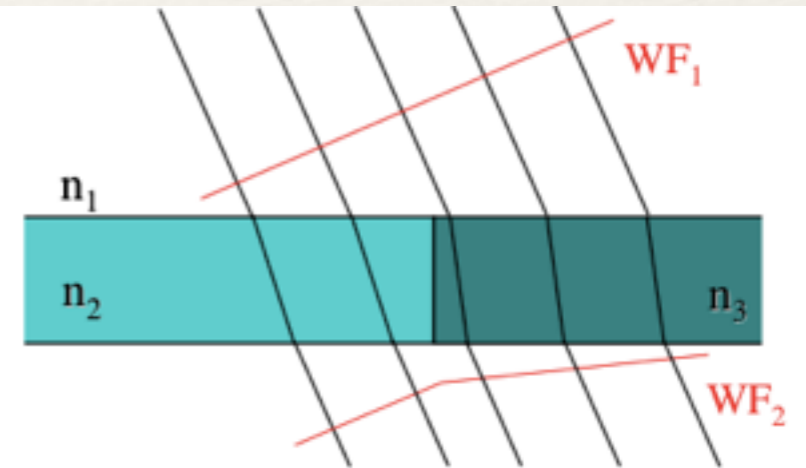
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Ideal Atmosphere!

Real Atmosphere!

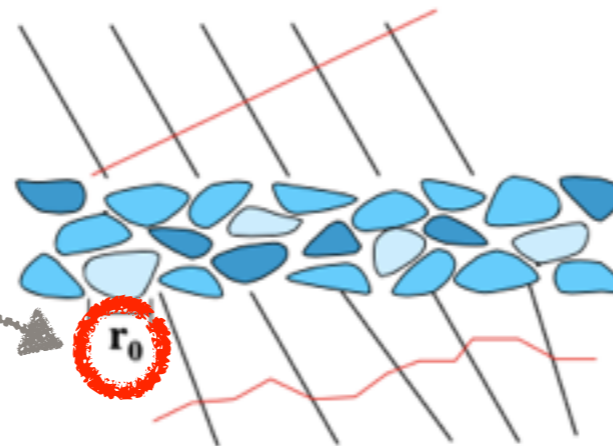


$WF_1 = WF_2 + \text{inclination}$



$WF_1 = WF_2 + \text{deformation}$

Fried Parameter



Cauchy equation:

$$n - 1 = \frac{77 \times 10^{-6}}{T} (1 + 7.52 \times 10^{-3} \lambda^{-2}) (P + 4810 \frac{P}{T})$$

Gladstone Equation:

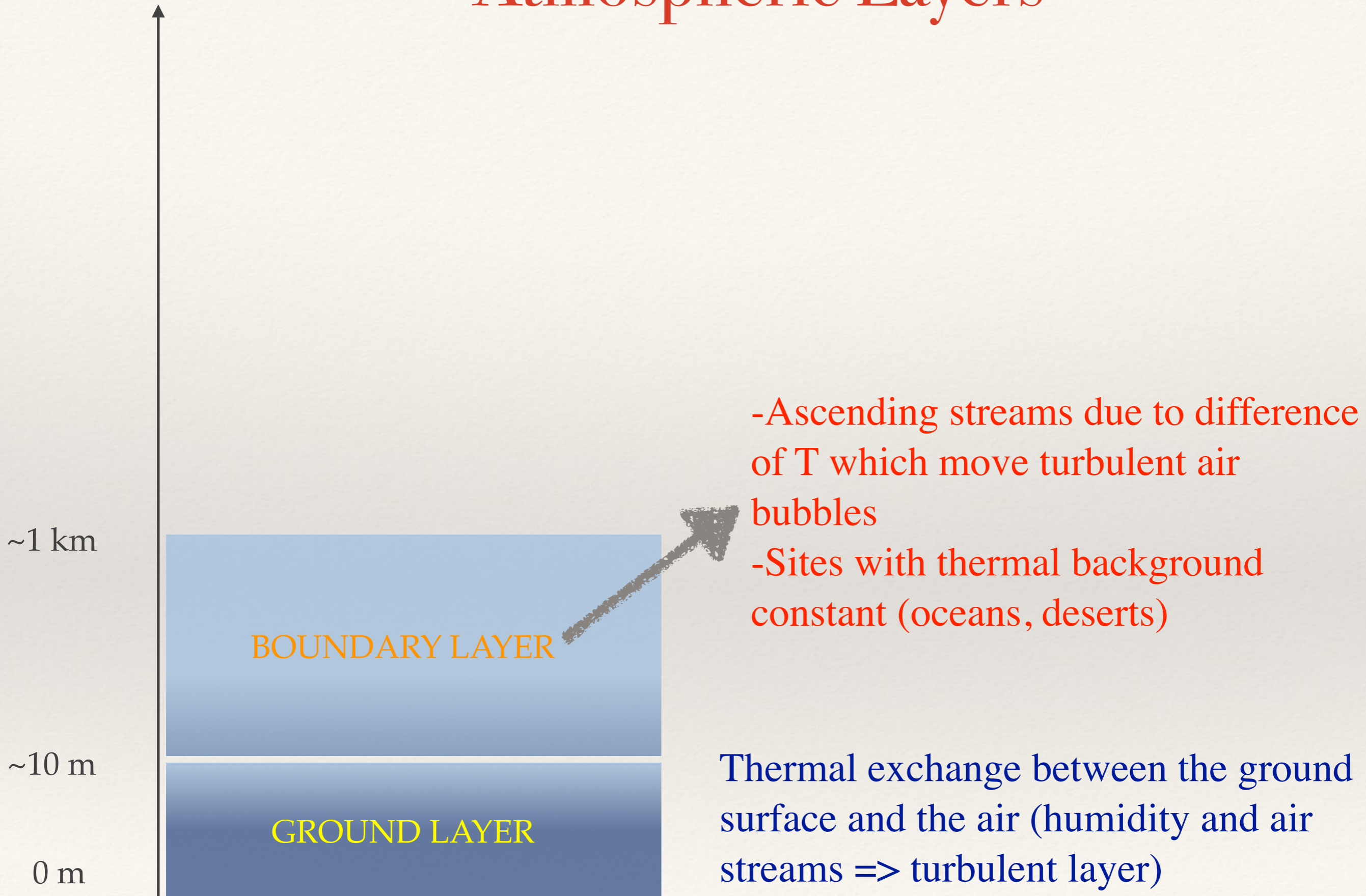
$$n - 1 = 77 \times 10^{-6} \frac{P}{T}$$

Atmospheric Layers

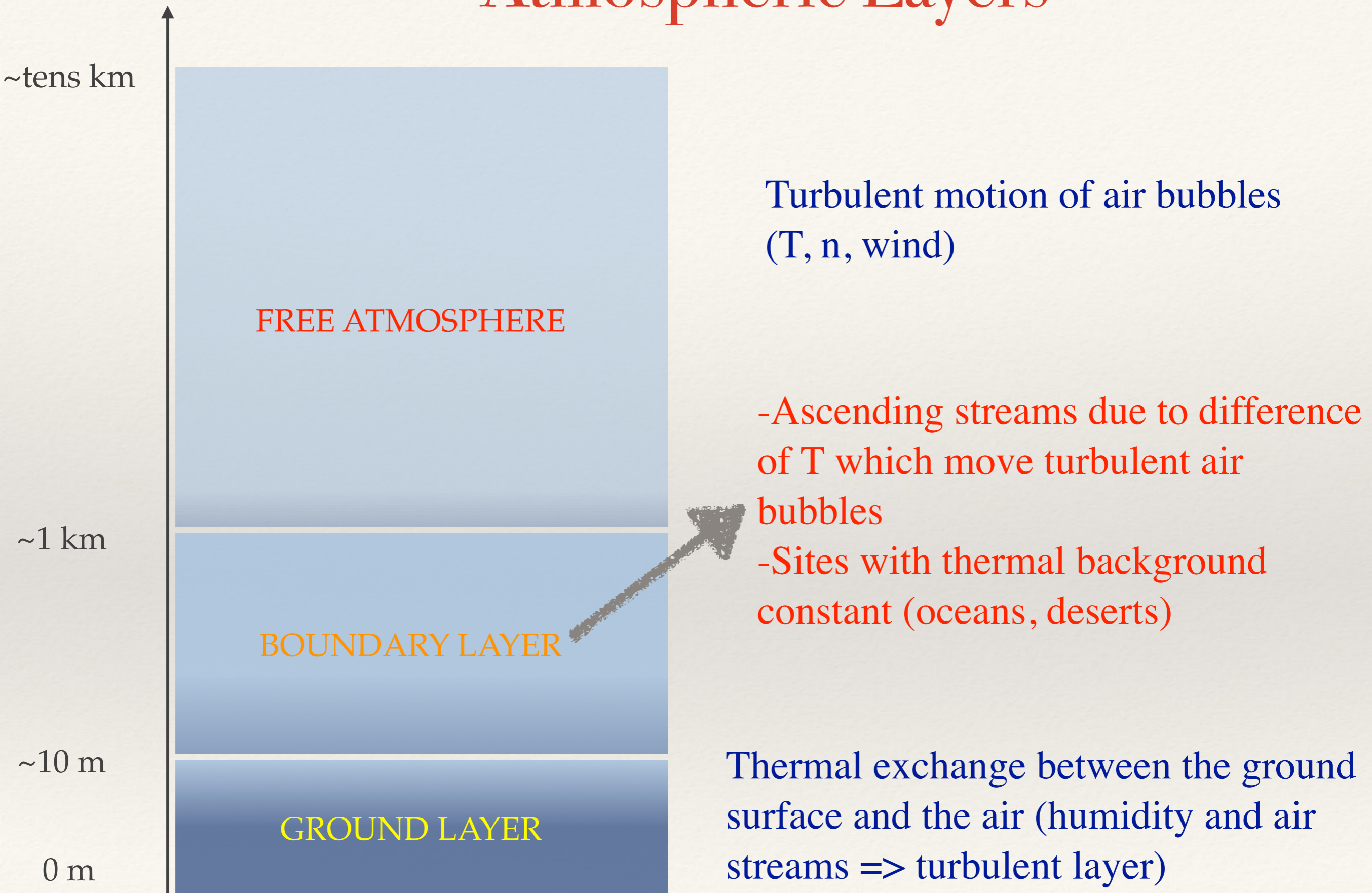


Thermal exchange between the ground surface and the air (humidity and air streams => turbulent layer)

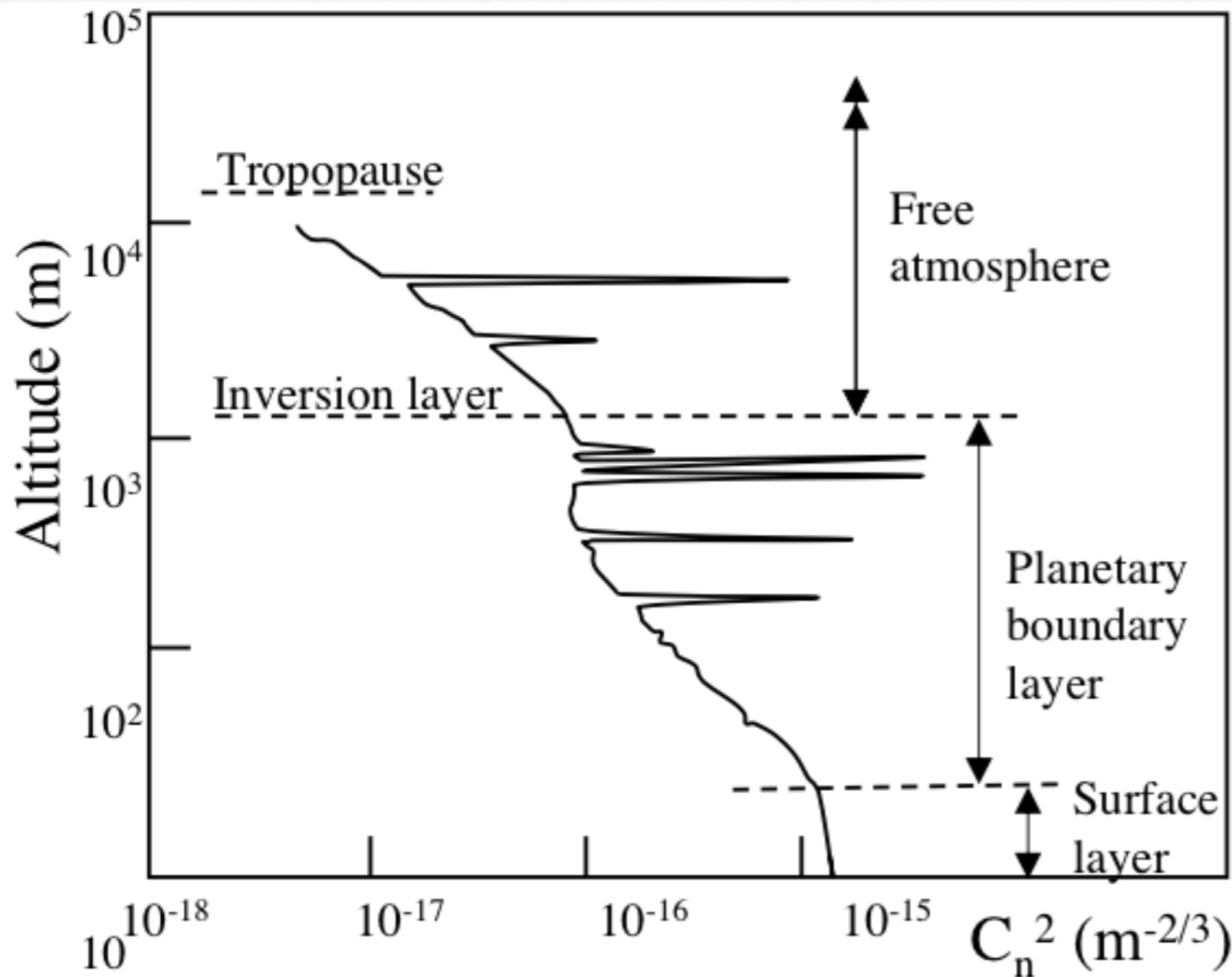
Atmospheric Layers



Atmospheric Layers



Atmospheric Layers



Several models describing the most important observing sites

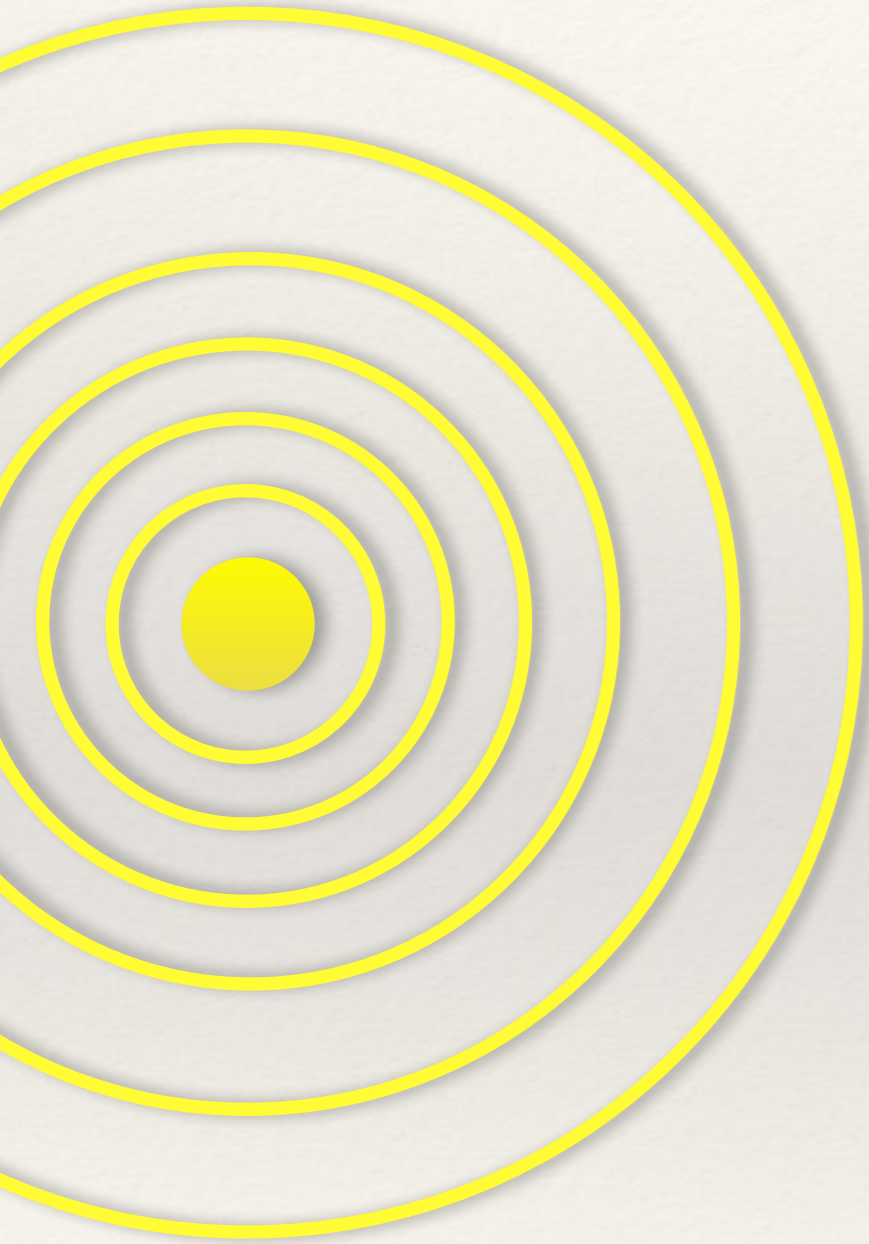
$C_n^2(h)$: structural function of the refractive index n

Thus, the definition of the average r_0 is more complicated...

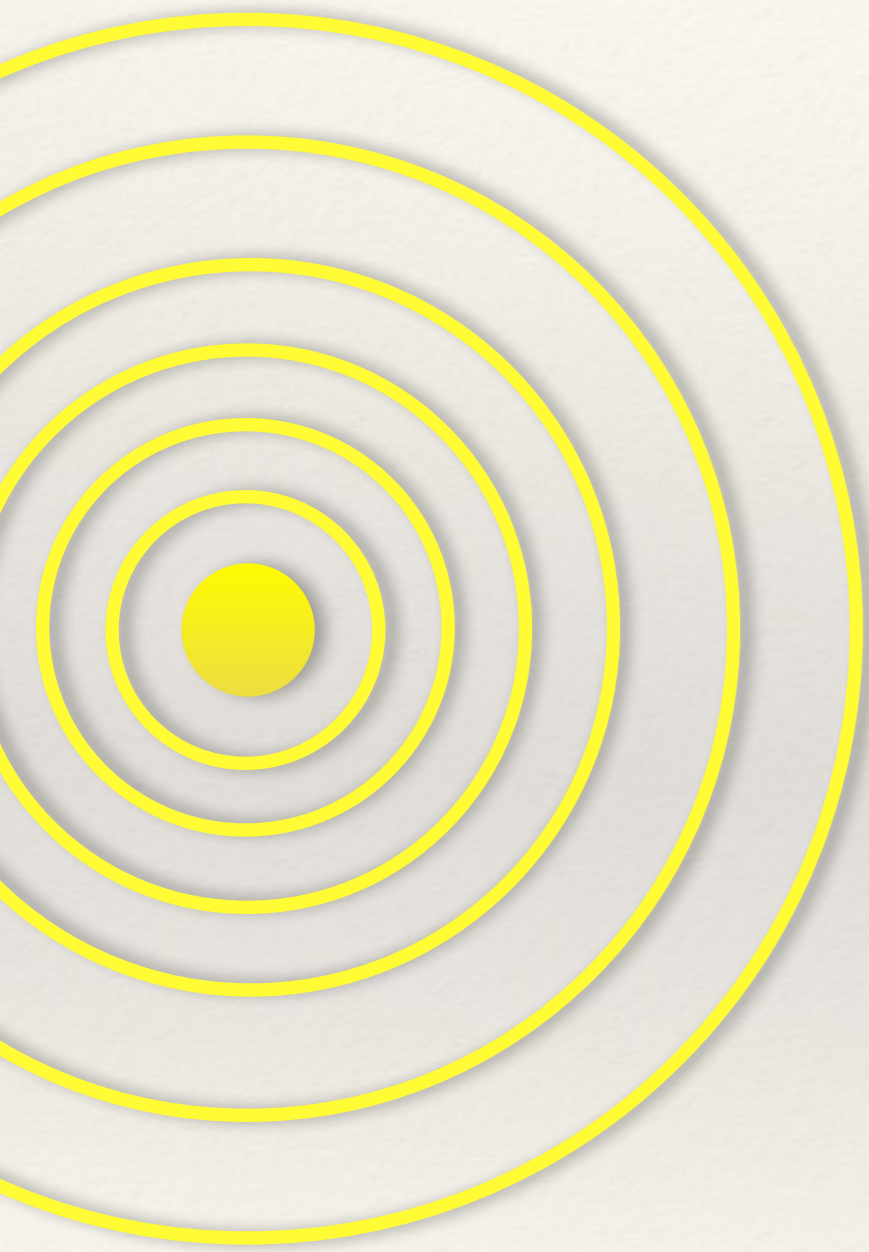
Wavefront Deformation



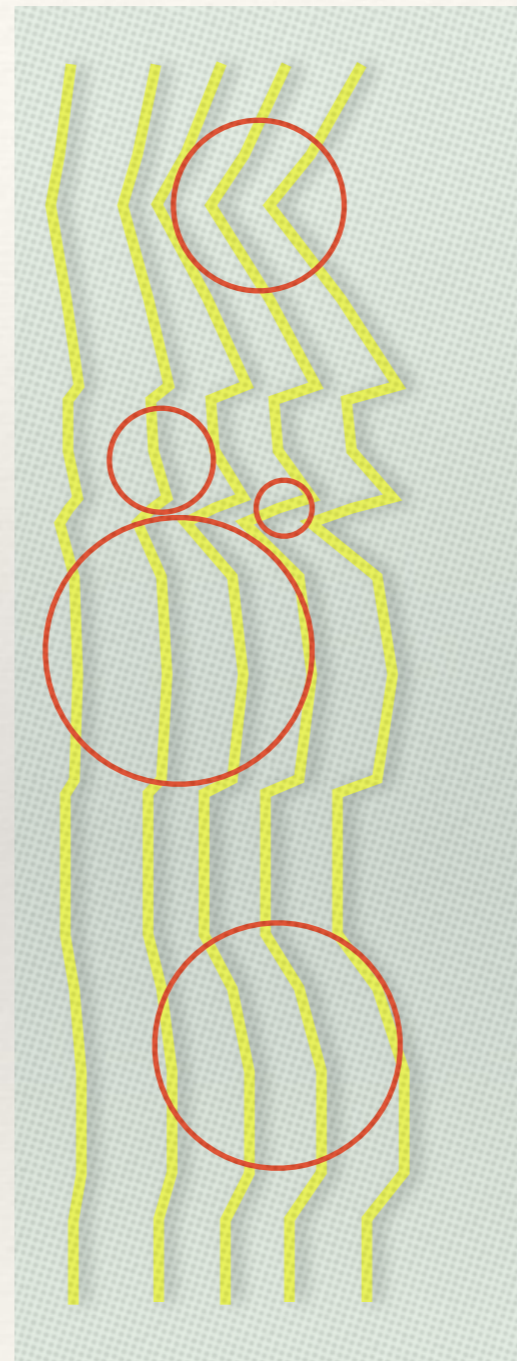
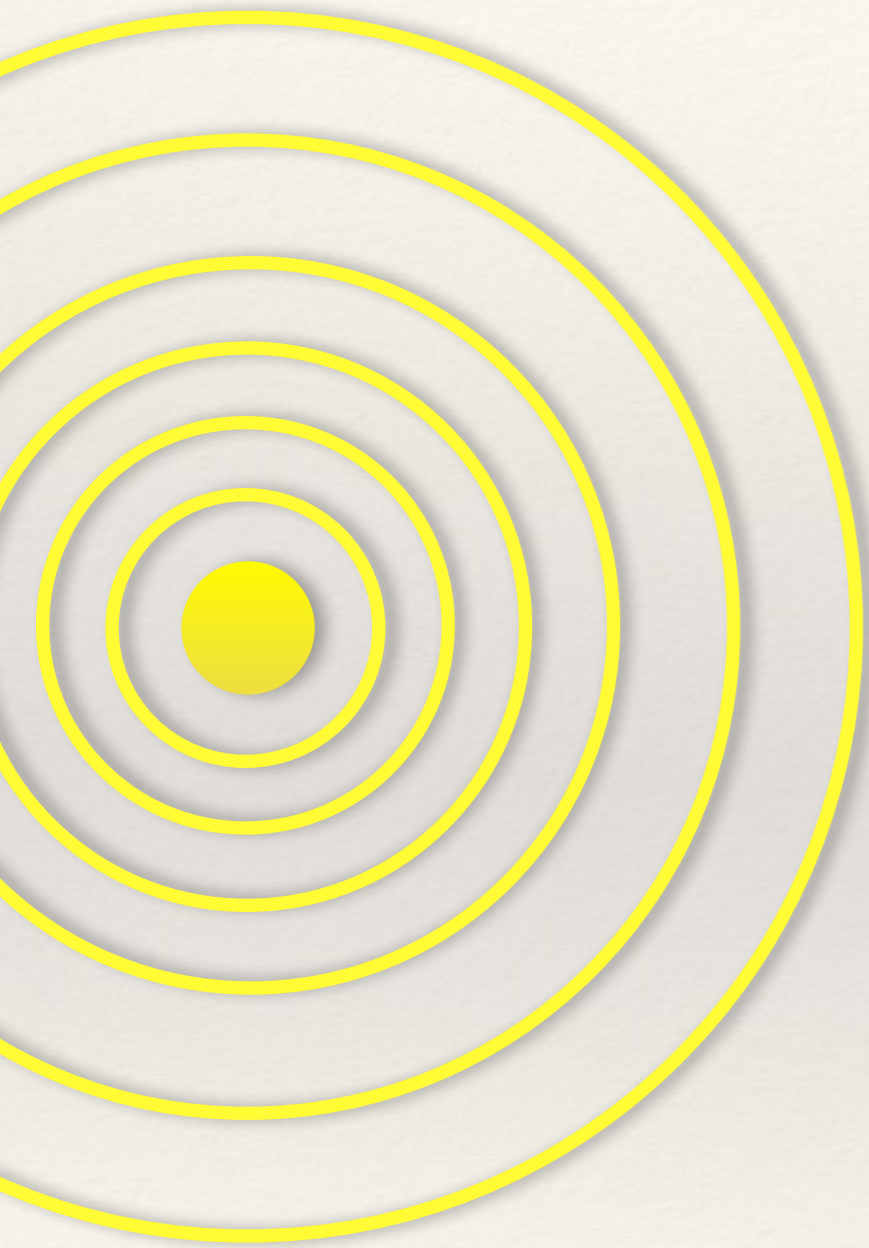
Wavefront Deformation



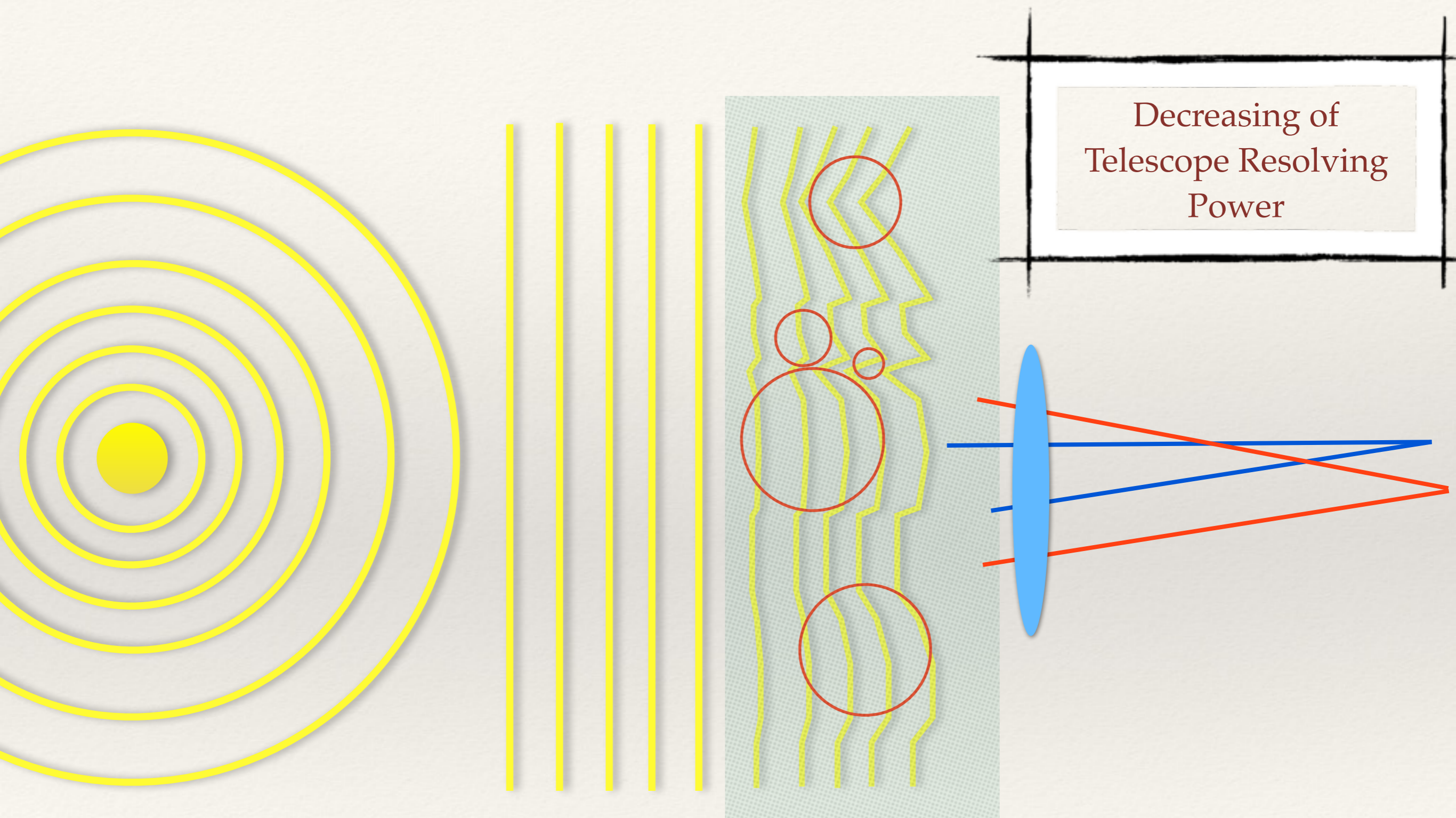
Wavefront Deformation



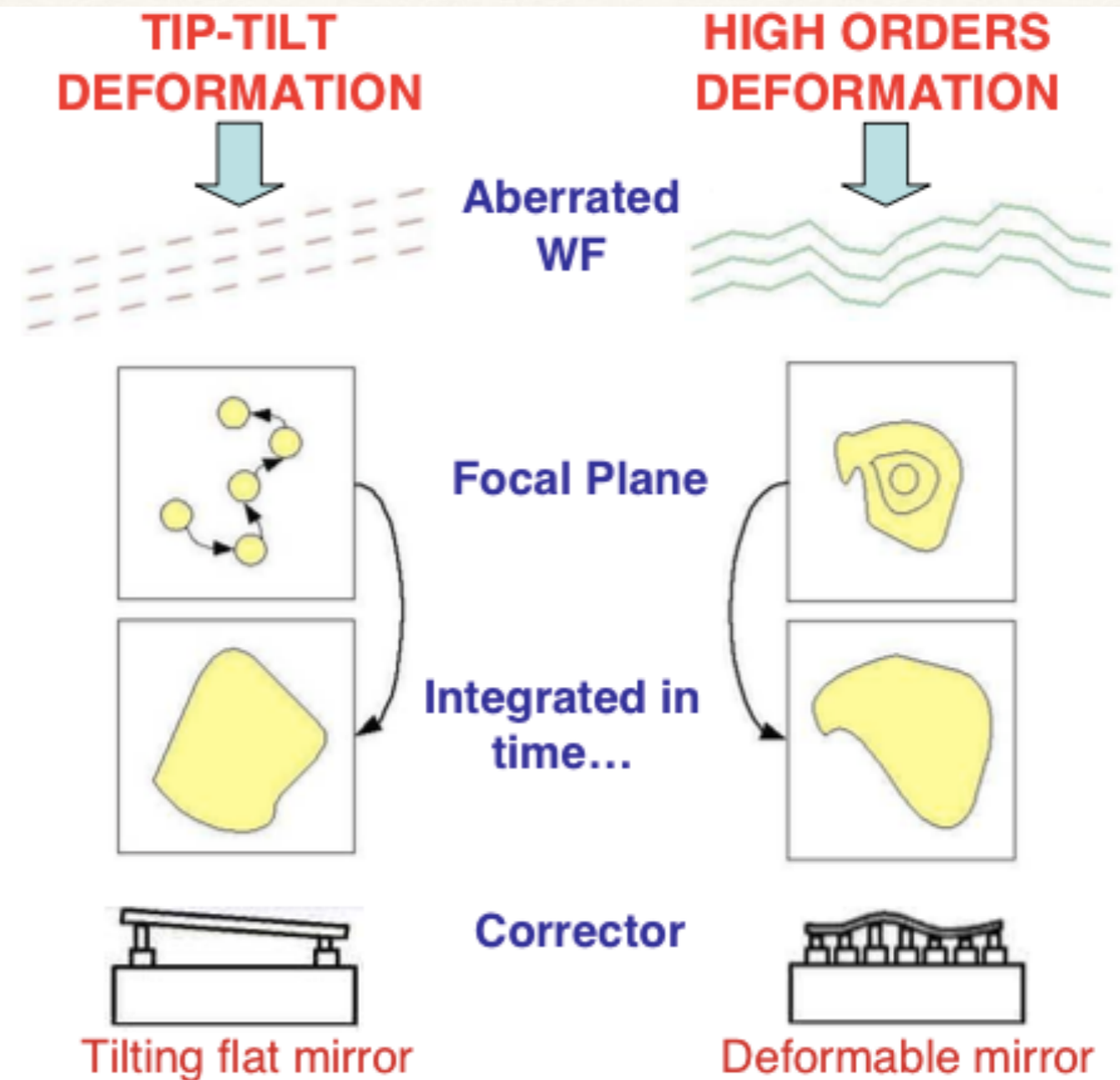
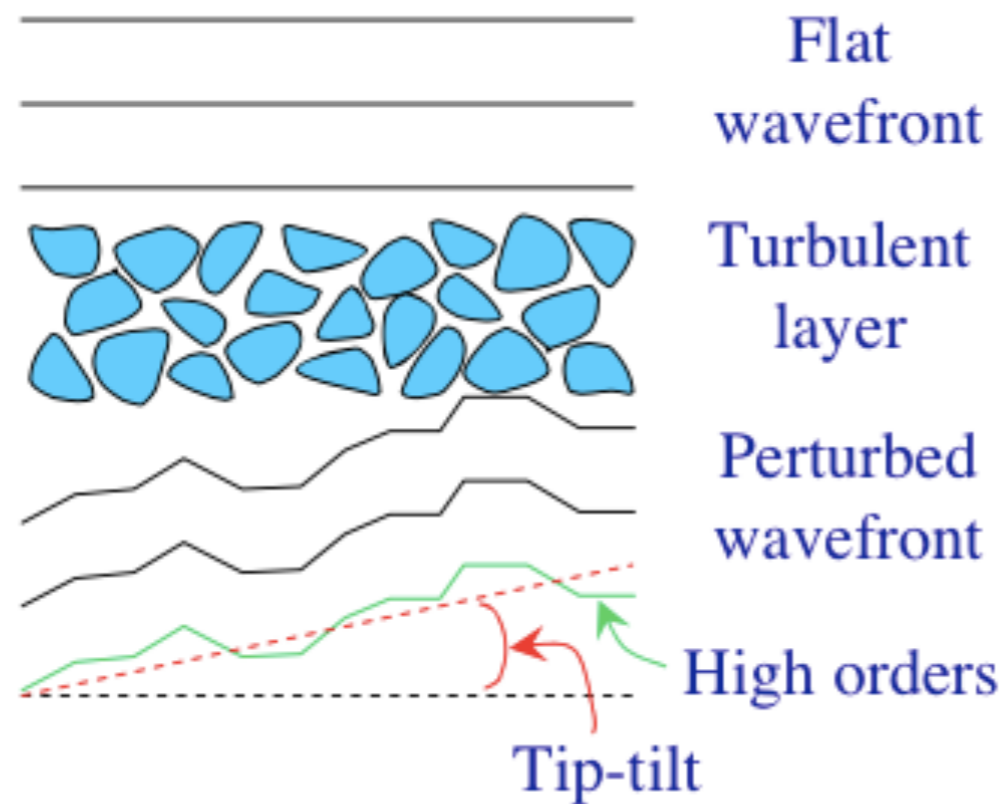
Wavefront Deformation



Wavefront Deformation



...what happen on the focal plane of the telescope?



Both Tip-Tilt and High-Orders have the same final effect: integrating with time, loss of resolution in the telescope!

Temporal Frequency: few ms
Spatial Frequency: tenth of cm

Atmospheric Parameters

FRIED parameter:

- Spatial scale inside which the WF statistically varies less than 1 rad
- Average size of turbulent cell
- Size of an air bubble with constant n

$$r_0 \propto \lambda^{6/5} \left[\int_0^{\infty} dh C_n^2(h) \right]^{-3/5}$$

Good sites:

K band $\Rightarrow r_0=30\text{cm}$

ISOPLANATIC angle:

- Angular scale inside which the WF statistically varies less than 1 rad

$$\theta_0 \propto r_0 / \bar{h} \propto \lambda^{6/5}$$

COHERENCE time:

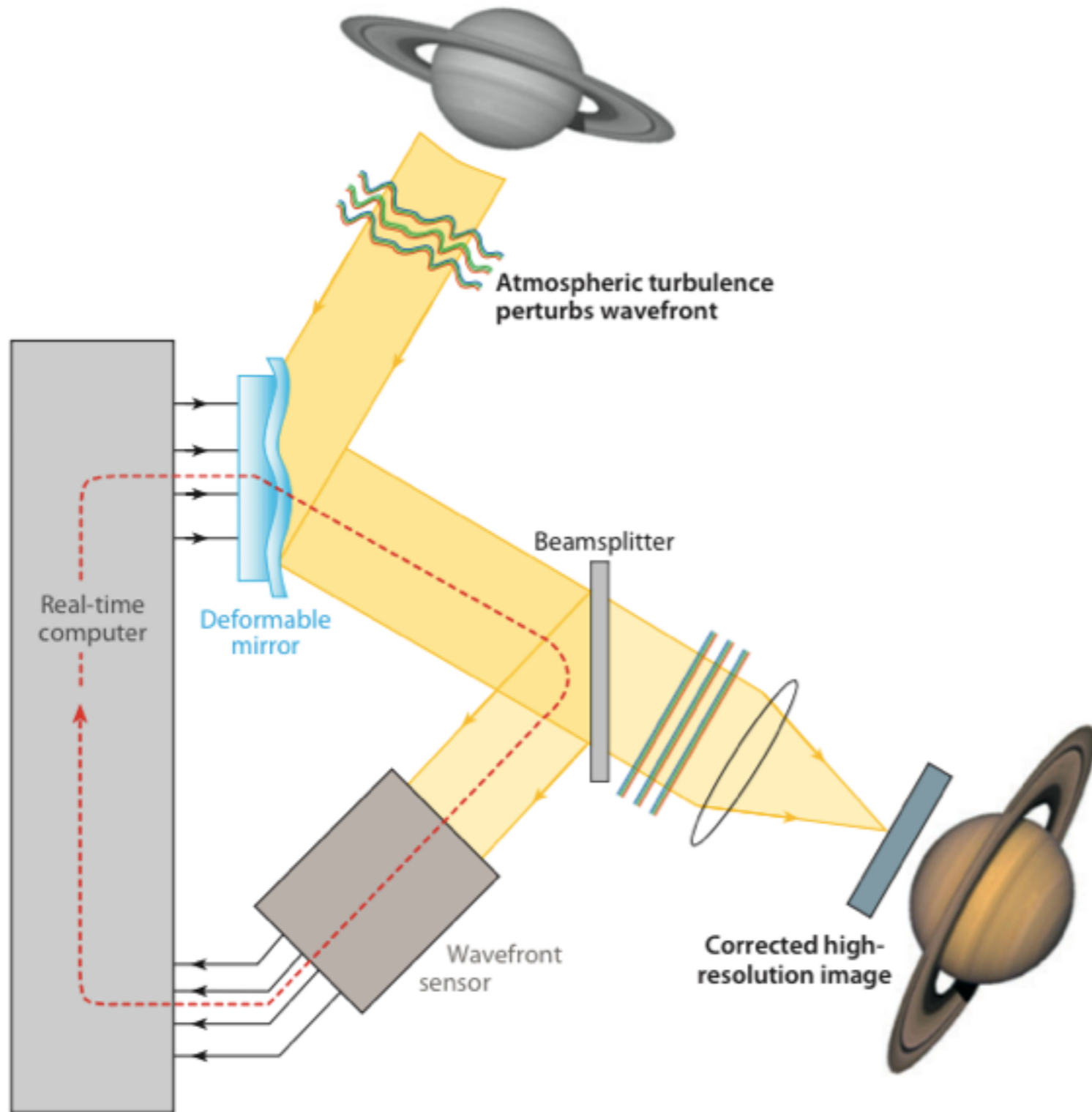
- Time scale inside which the WF statistically varies less than 1 rad

$$\tau_0 = r_0 / v \propto \lambda^{6/5}$$

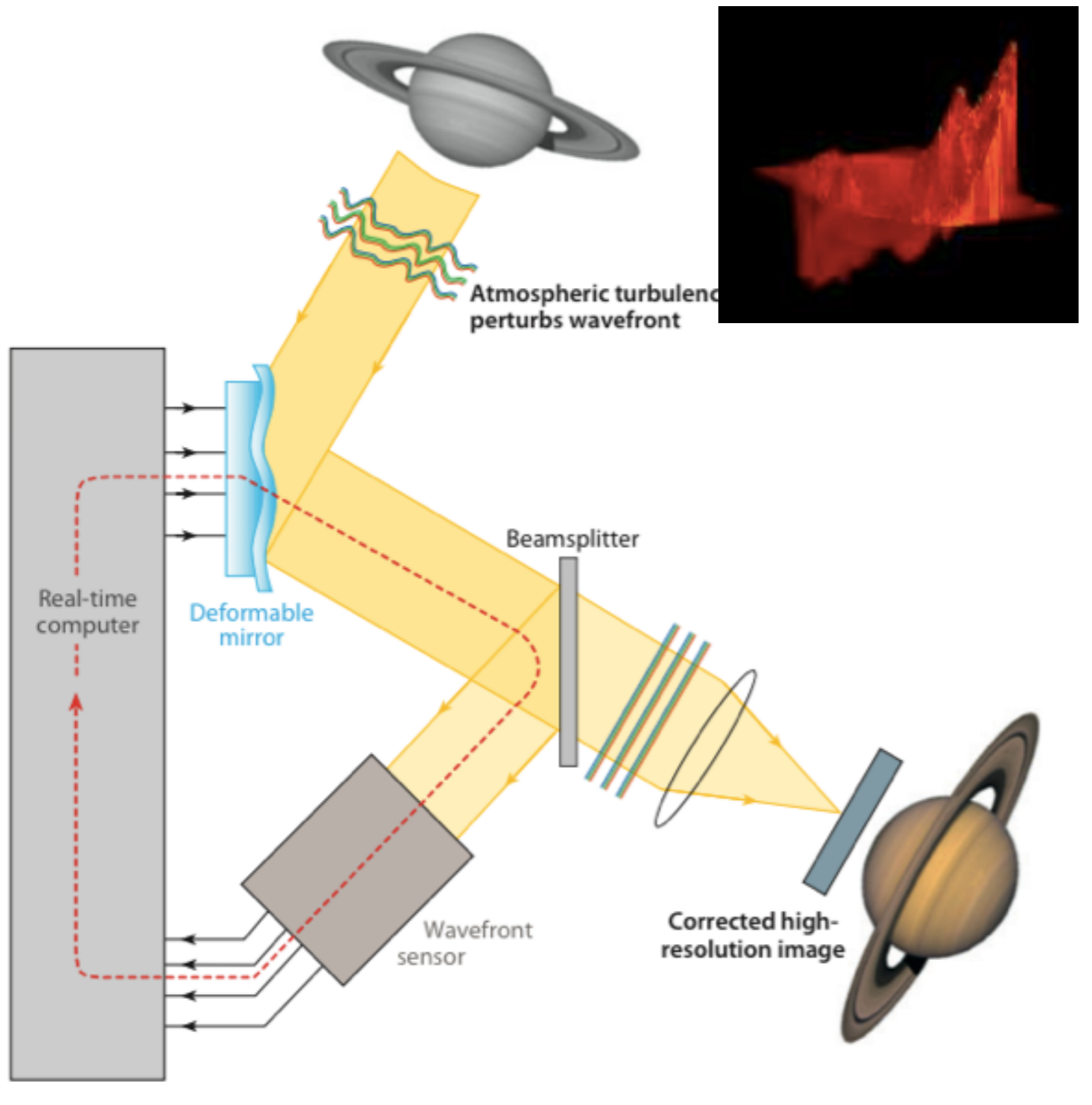
$$\tau_0 \approx 1\text{ms}$$

Strehl Ratio: $\text{PSF}_{\text{obs}} / \text{PSF}_{\text{teo}}$

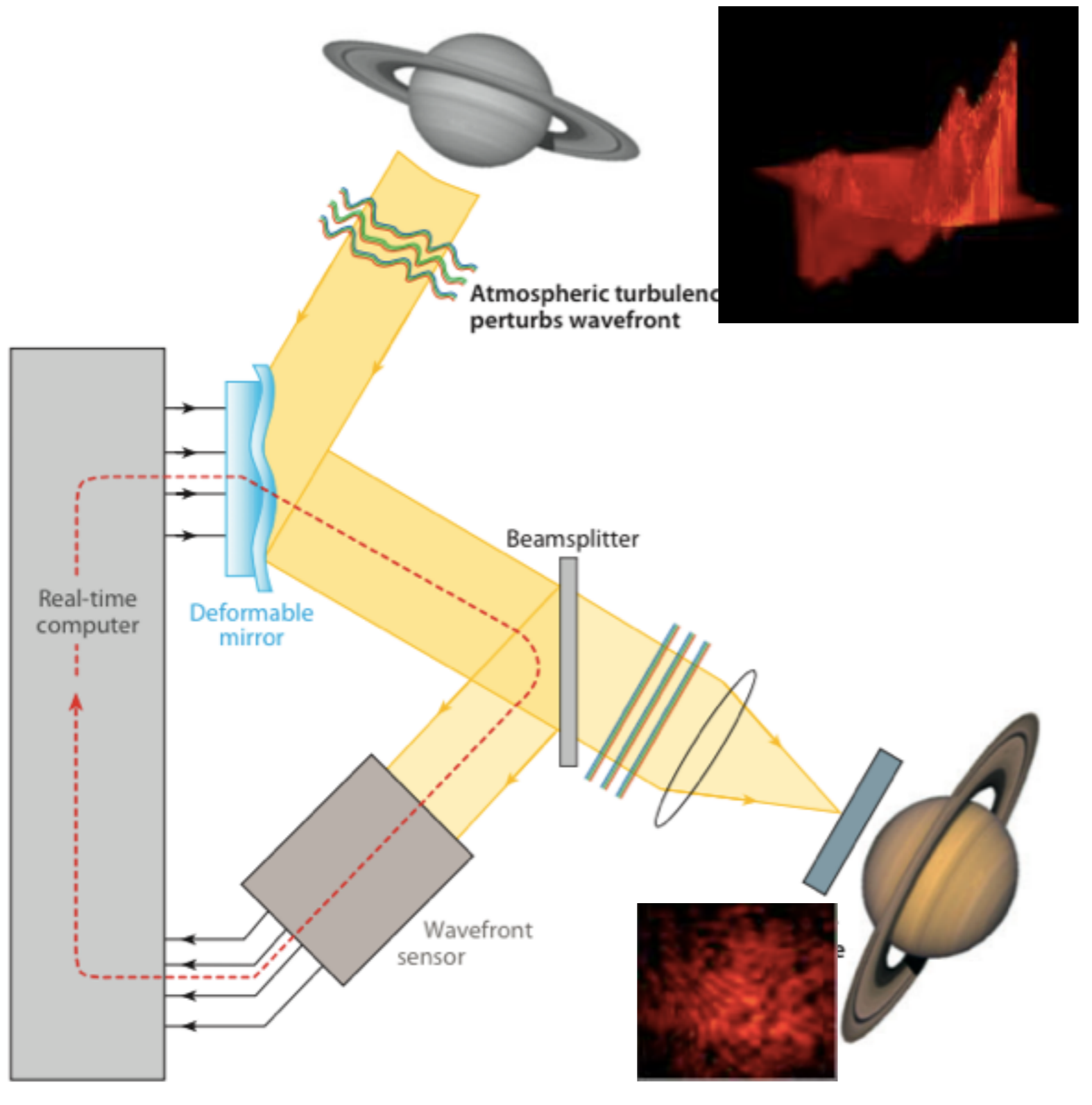
AO Working Principles



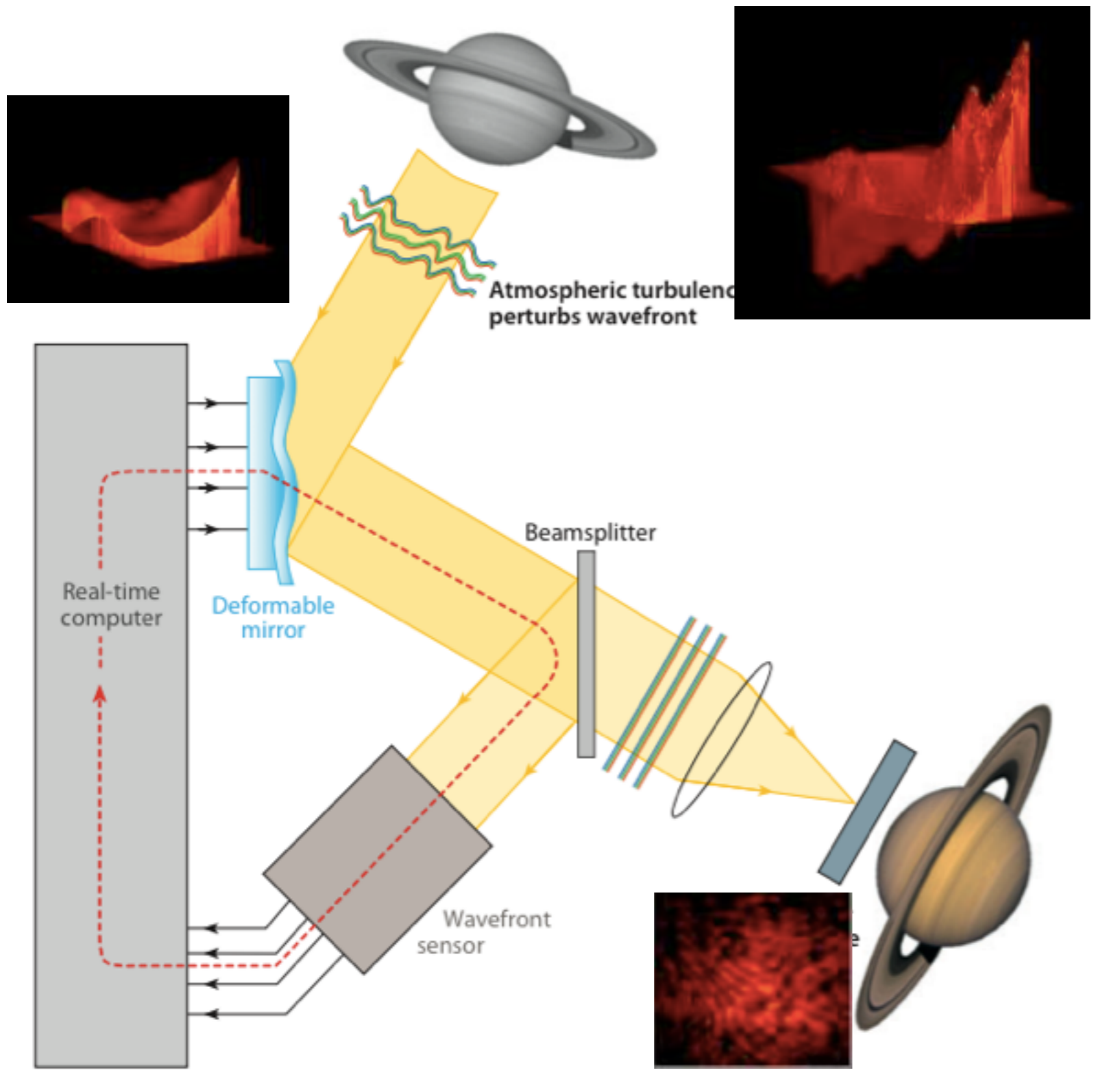
AO Working Principles



AO Working Principles

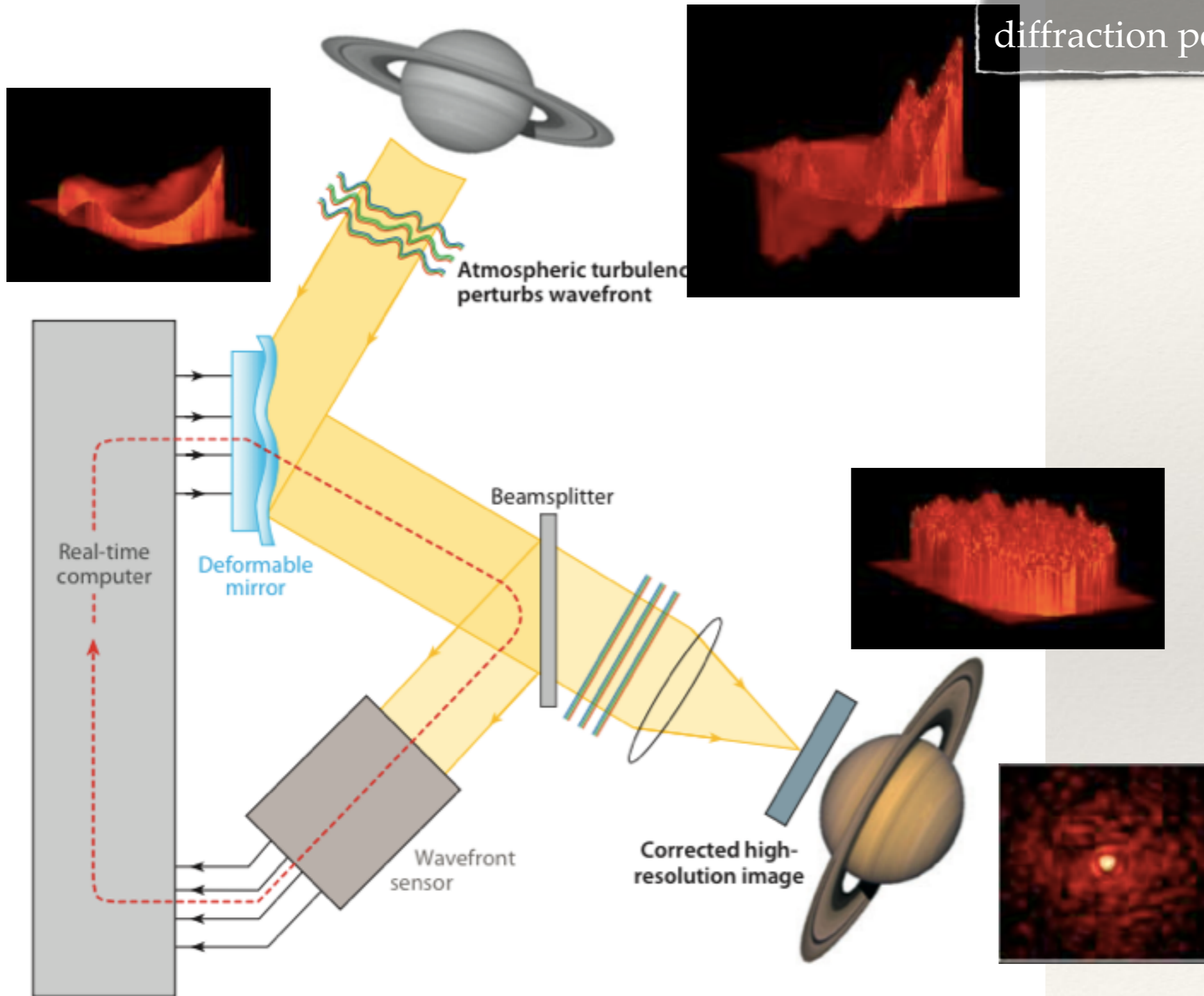


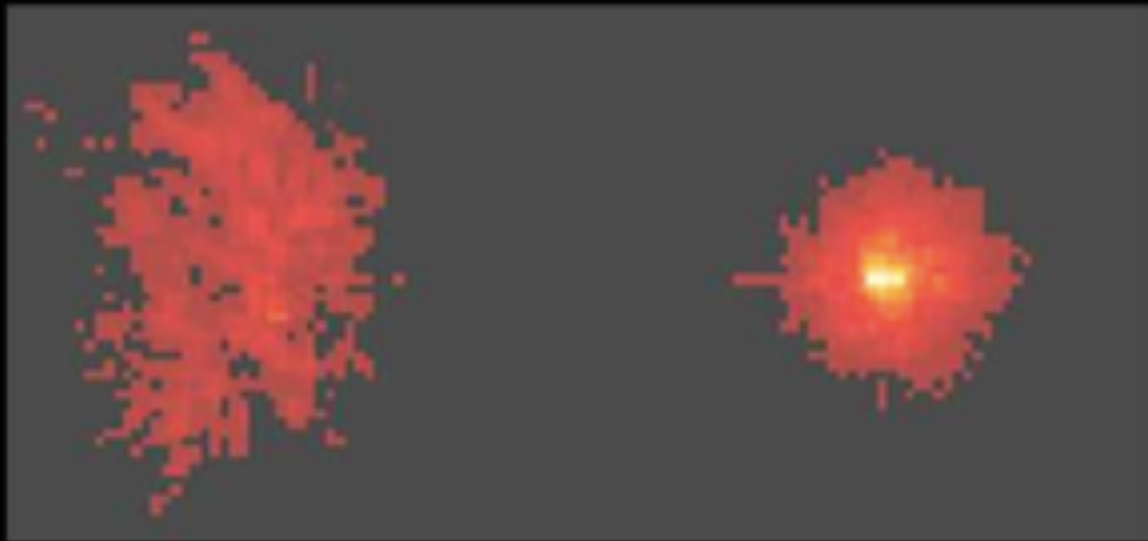
AO Working Principles



AO Working Principles

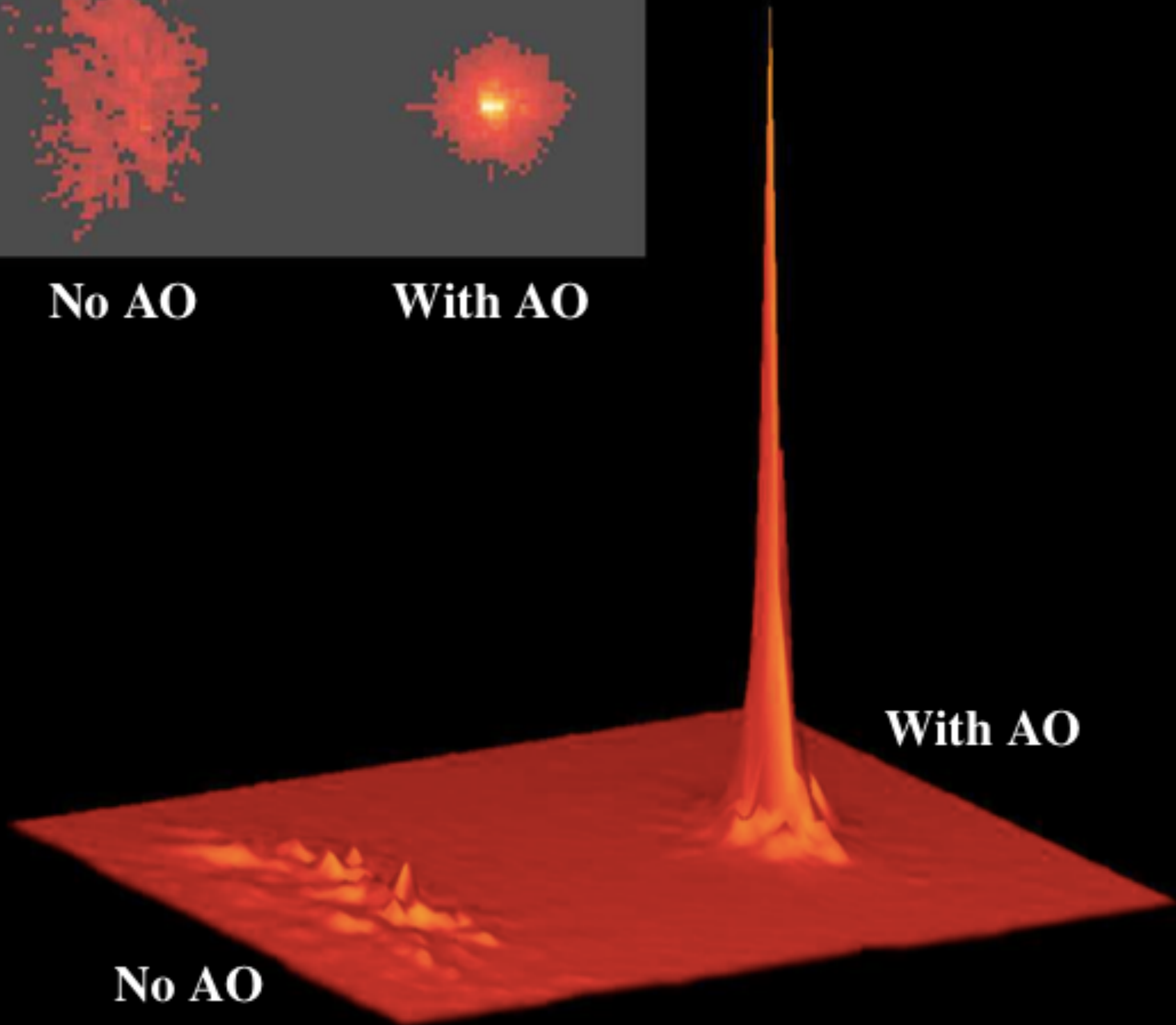
- ✓ Restore the theoretical angular resolution
- ✓ Concentrate the flux inside the diffraction peak





No AO

With AO



No AO

With AO

Main Elements of an AO System

Wavefront Sensor

Real Time Computer

Deformable Mirror

Main Elements of an AO System

Wavefront Sensor

should allow high order correction and be very sensitive (fast response).

Real Time Computer

Deformable Mirror

Main Elements of an AO System

Wavefront Sensor

should allow high order correction and be very sensitive (fast response).

Real Time Computer

should close the loop at >1 kHz frequency.

Deformable Mirror

Main Elements of an AO System

Wavefront Sensor

should allow high order correction and be very sensitive (fast response).

Real Time Computer

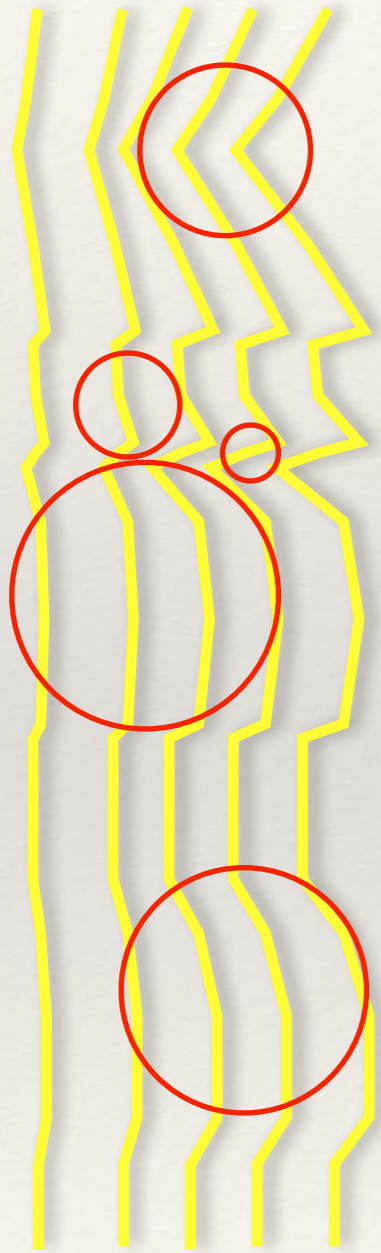
should close the loop at >1 kHz frequency.

Deformable Mirror

the highest the number of actuators, best correction of the wavefront error can be obtained. Other important parameters are speed, dynamic range, number of fault elements, and density of actuators (optics size)

Wavefront Measurement

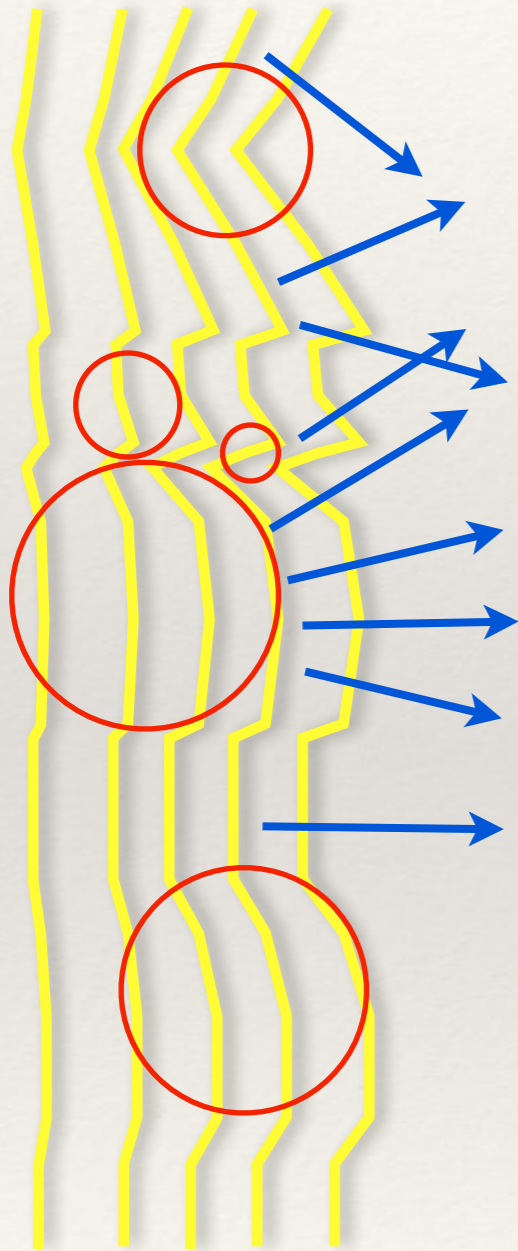
to improve ... we need measurements



Wavefront Measurement

to improve ... we need measurements

the direction of propagation is perpendicular to the wavefront

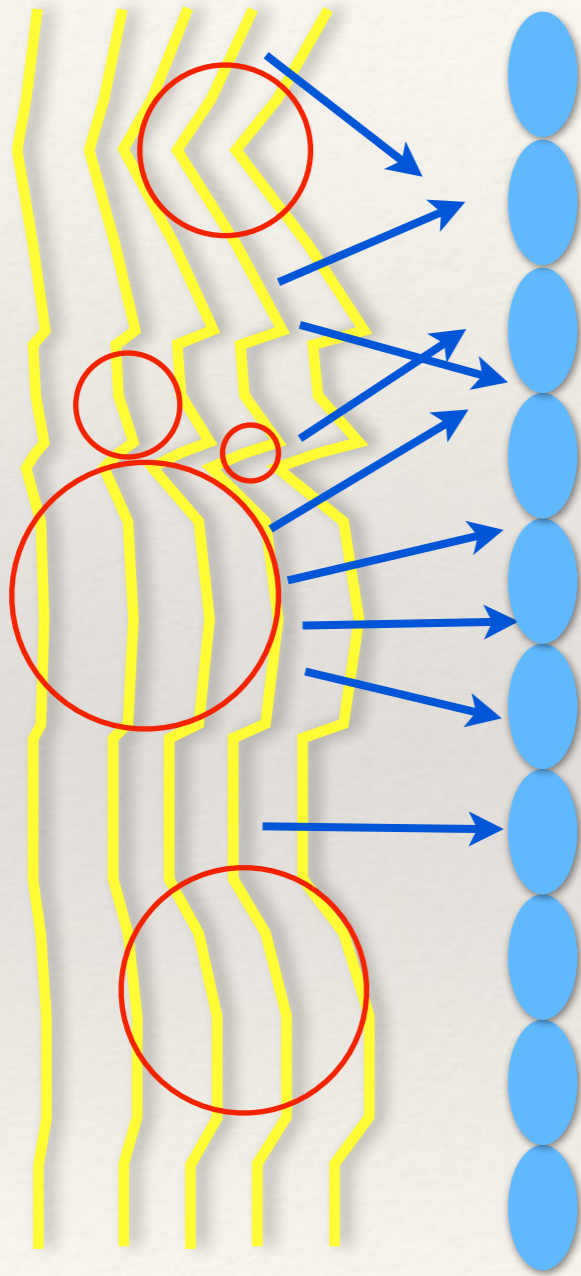


Wavefront Measurement

to improve ... we need measurements

the direction of propagation is perpendicular to the wavefront

Using micro lenses we can have an idea on the "local" tilt of the wavefront

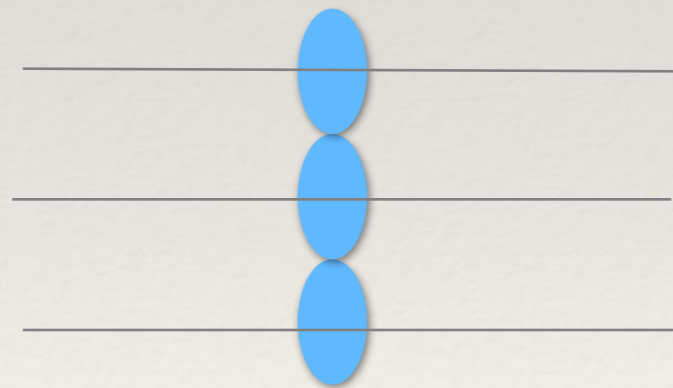
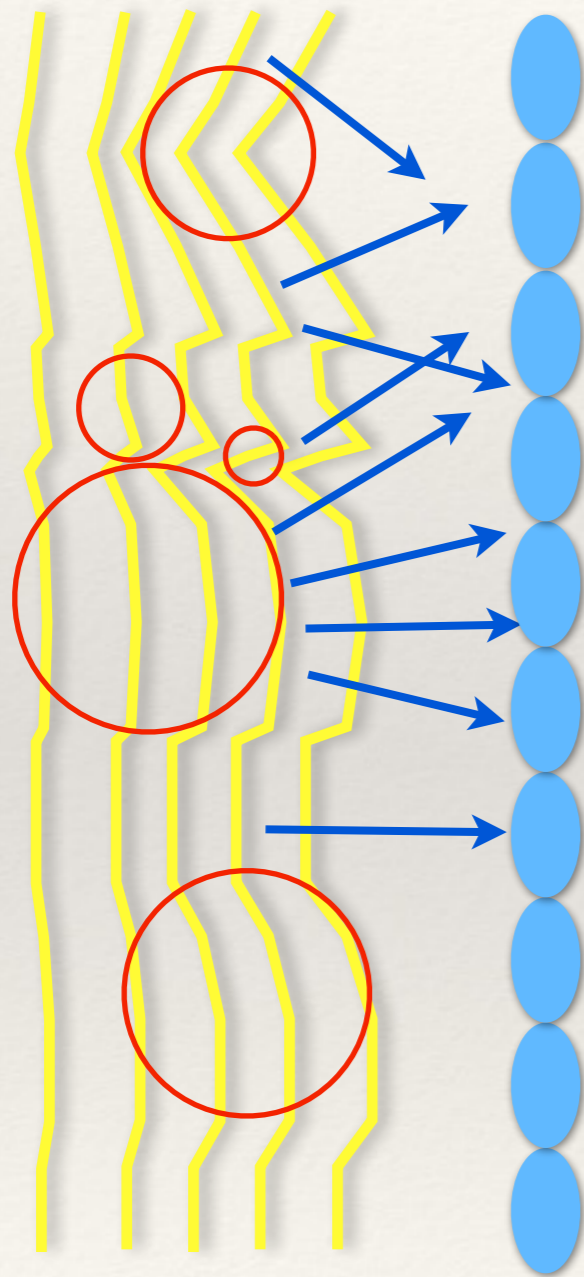


Wavefront Measurement

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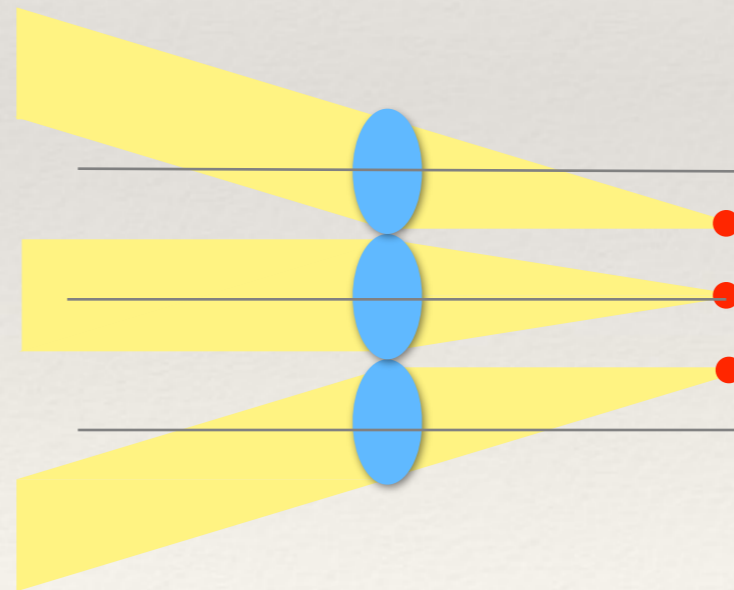
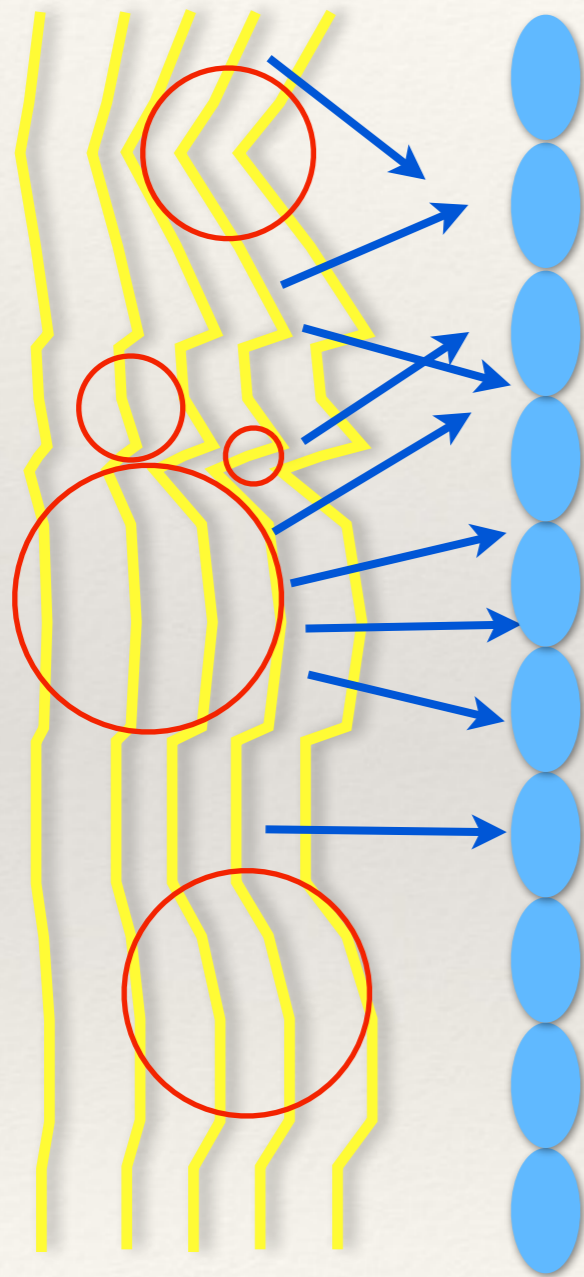


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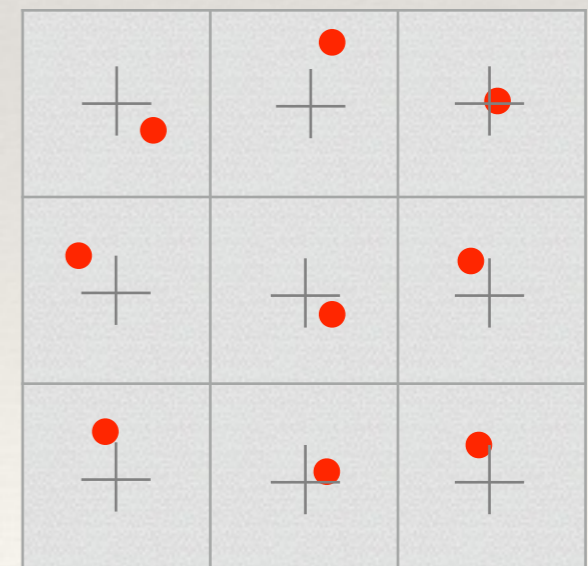
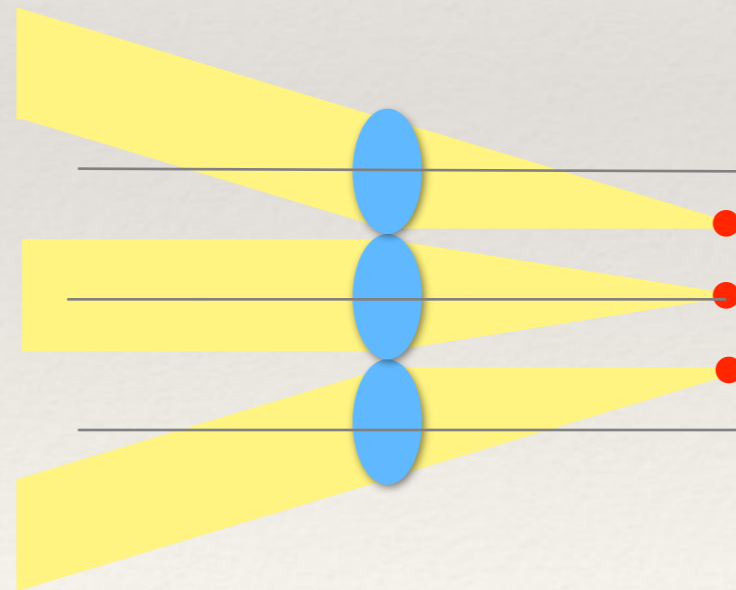
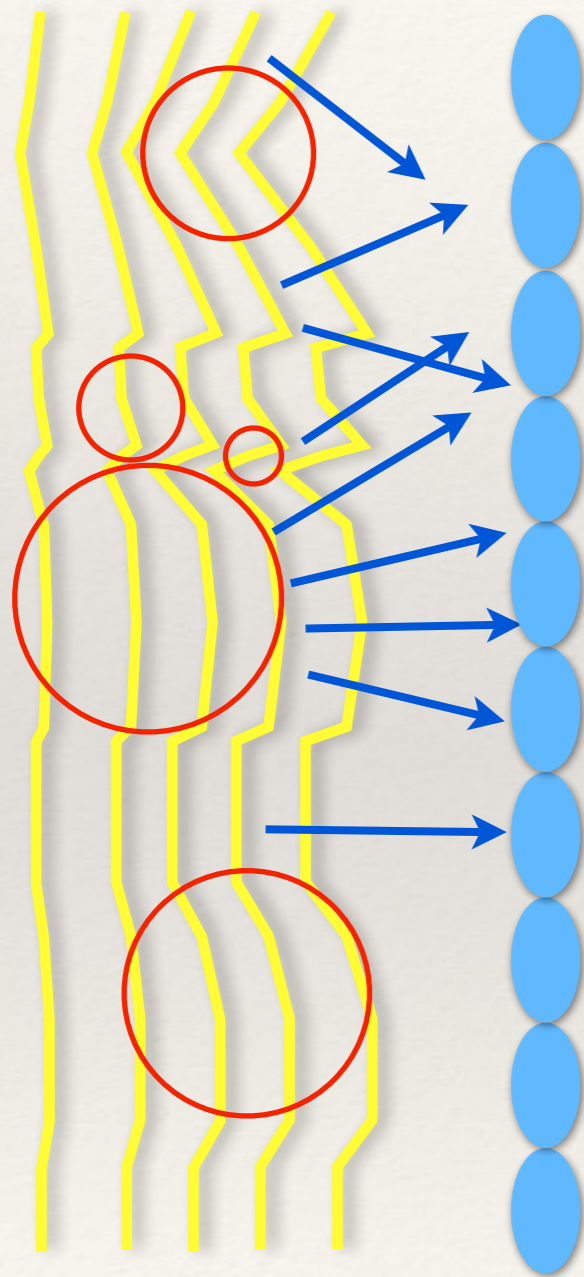


Wavefront Measurement

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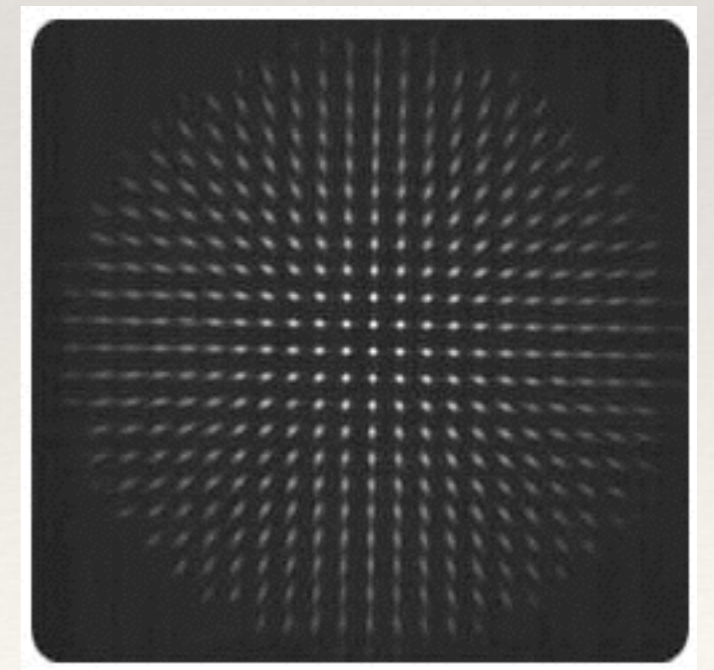
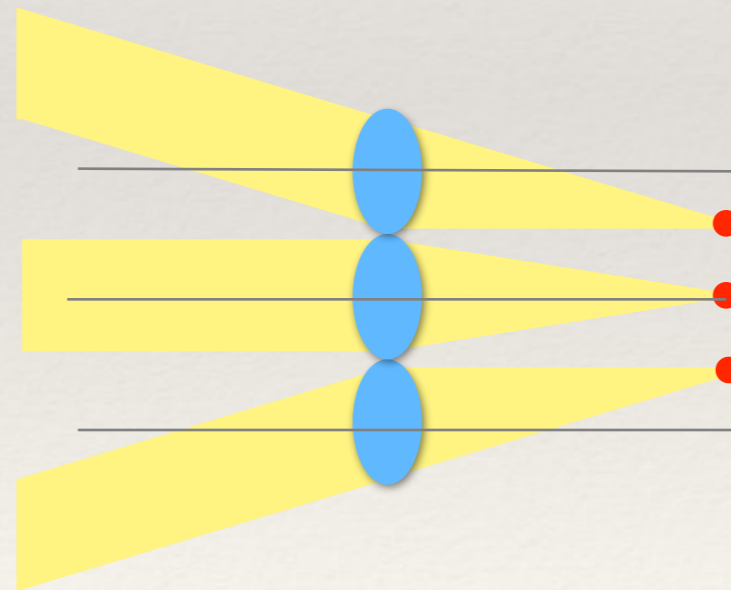
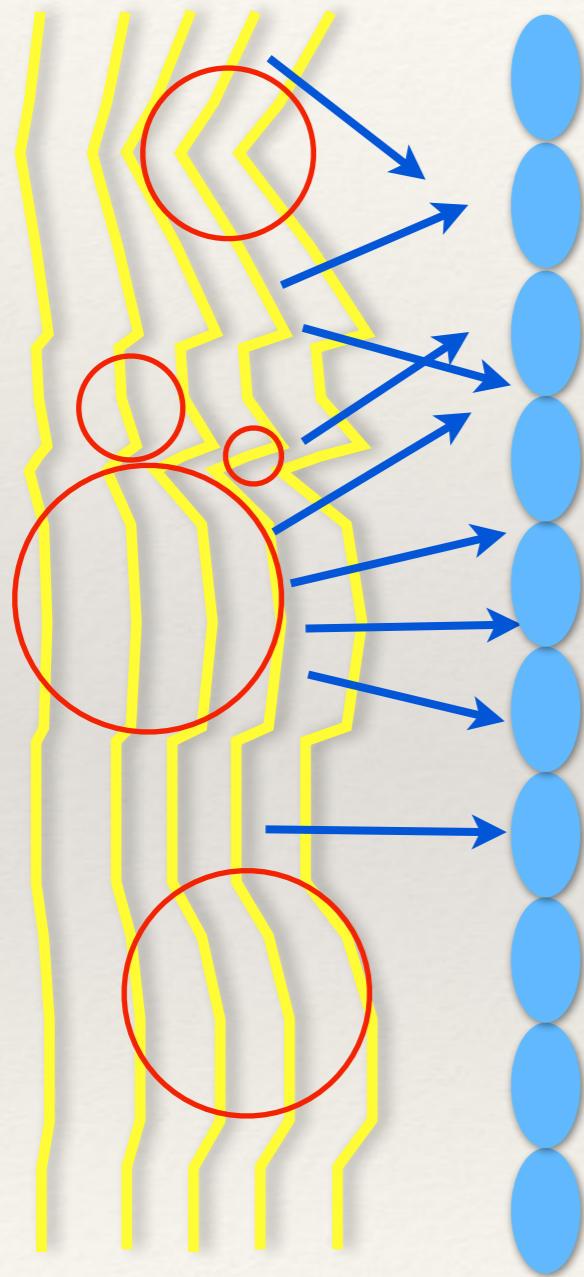


Wavefront Measurement

to improve ... we need measurements

the direction of propagation is perpendicular to the wavefront

Using micro lenses we can have an idea on the "local" tilt of the wavefront

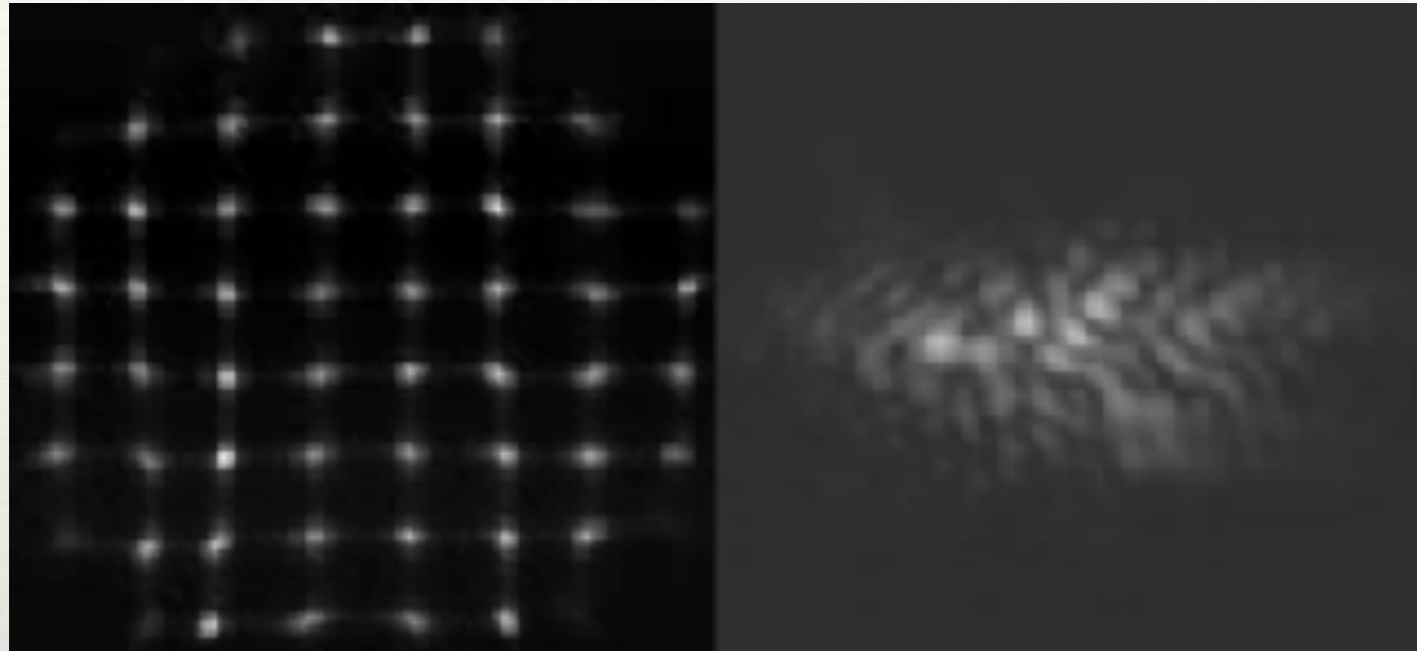


High Order Wavefront Measurement

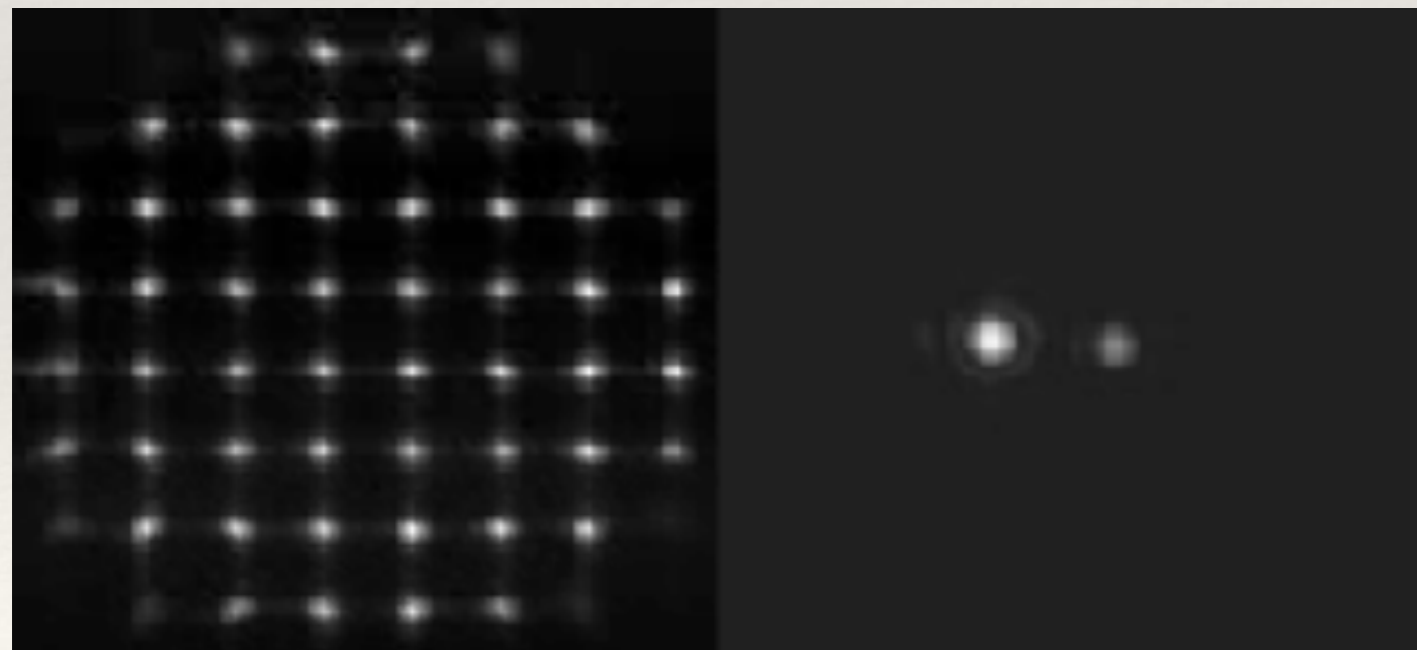
How to perform High-Order WFSensing? The basic idea is **to split the incoming wavefront in several part** to check which are the aberrations in that small portion

- The higher the number of sub-apertures, the better the sampling, but:
- The higher the number of sub-apertures, the lower the light for each subaperture
- A limit is imposed also from the number of actuators of the DM
- Of course the scientific wavelength is important to select the n of sub-apertures being r_0 dependent on the wavelength

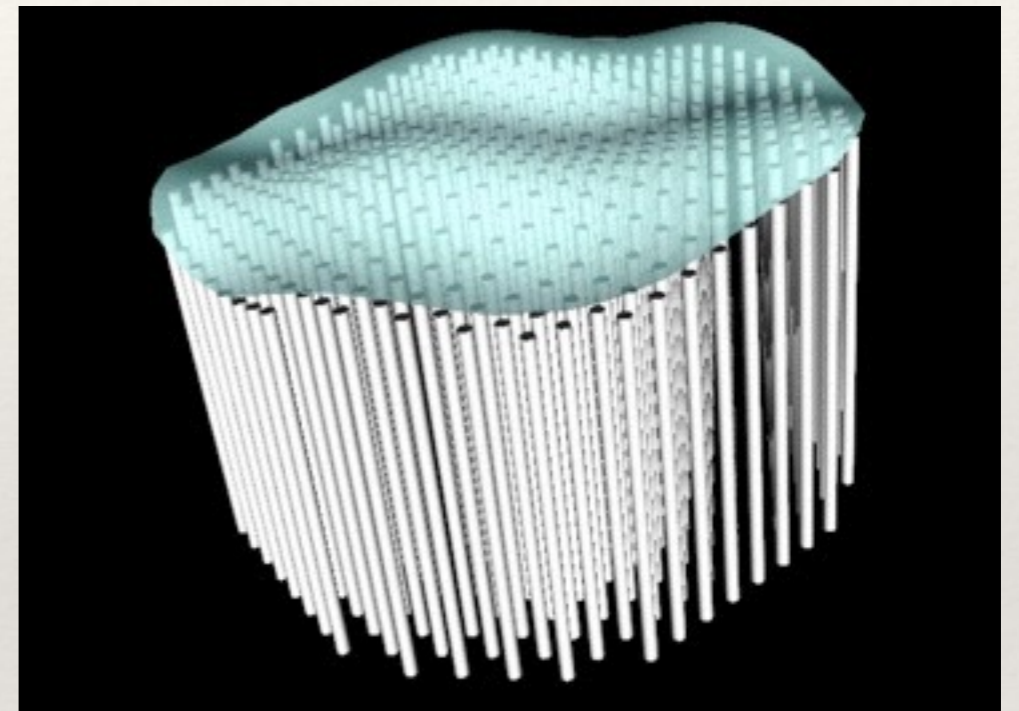
WAVEFRONT ANALYSIS



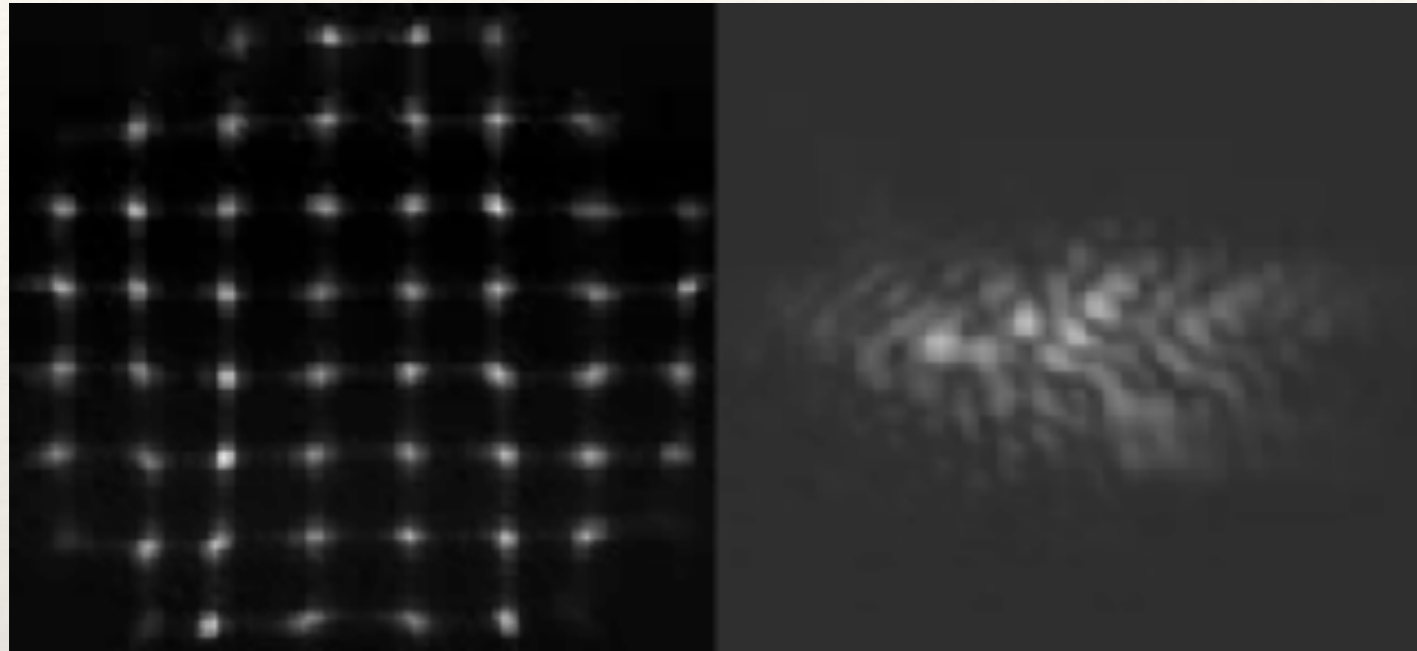
Open Loop



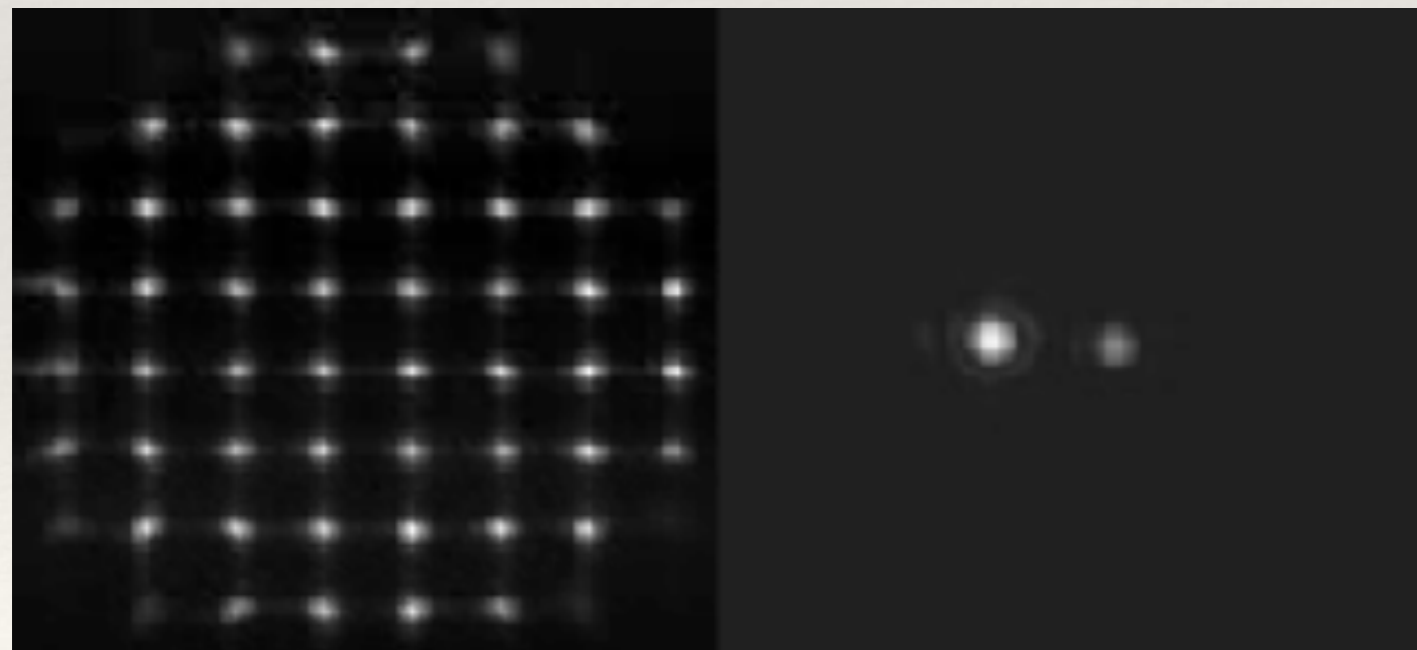
Close Loop



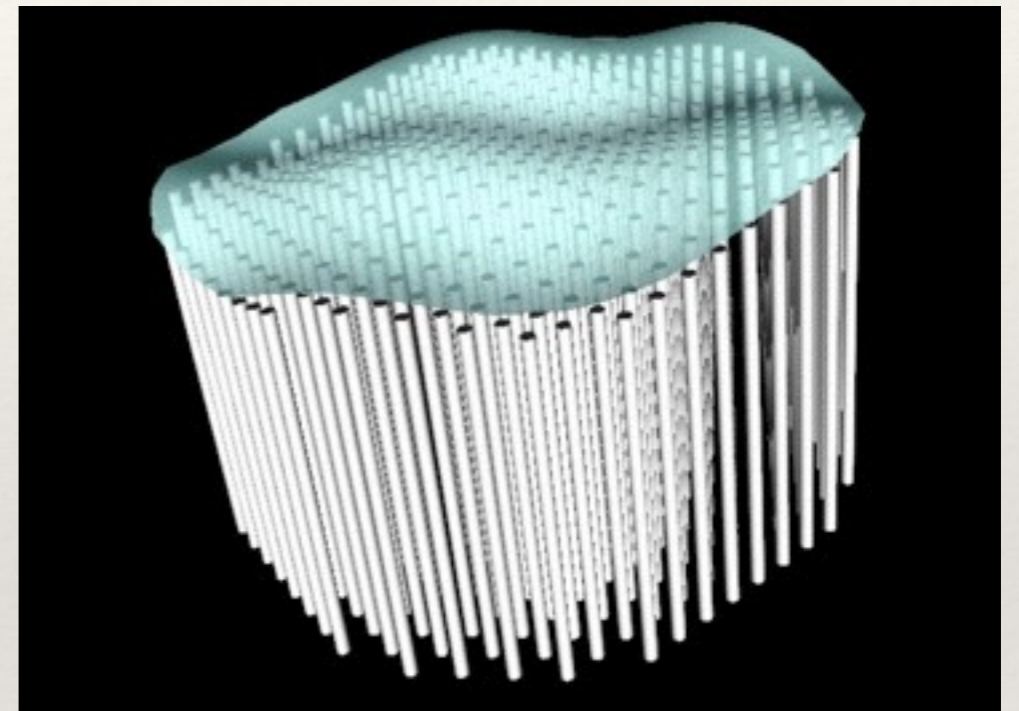
WAVEFRONT ANALYSIS



Open Loop

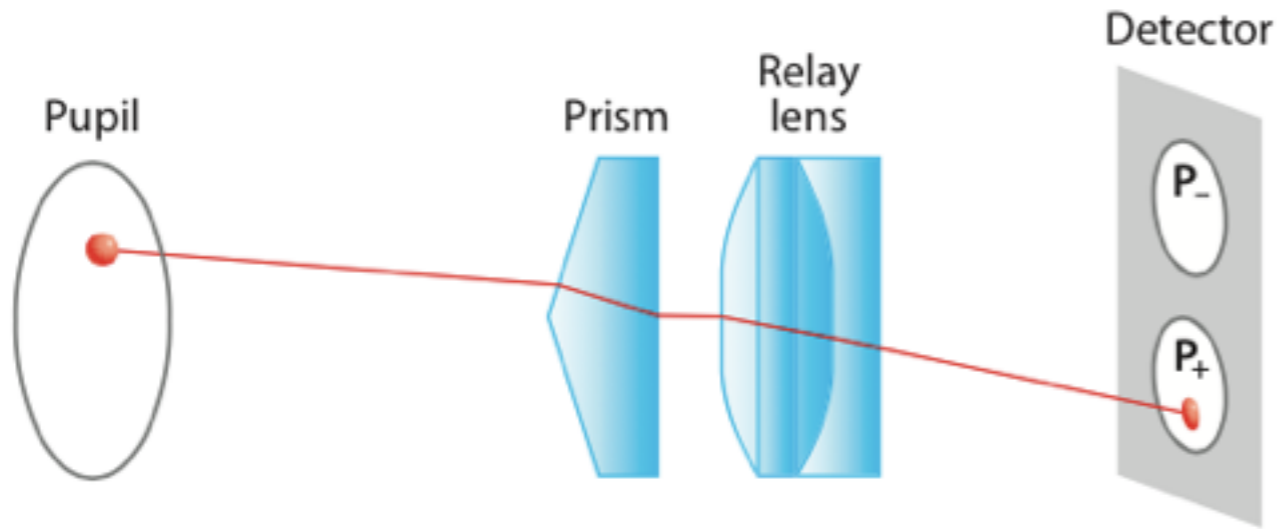


Close Loop

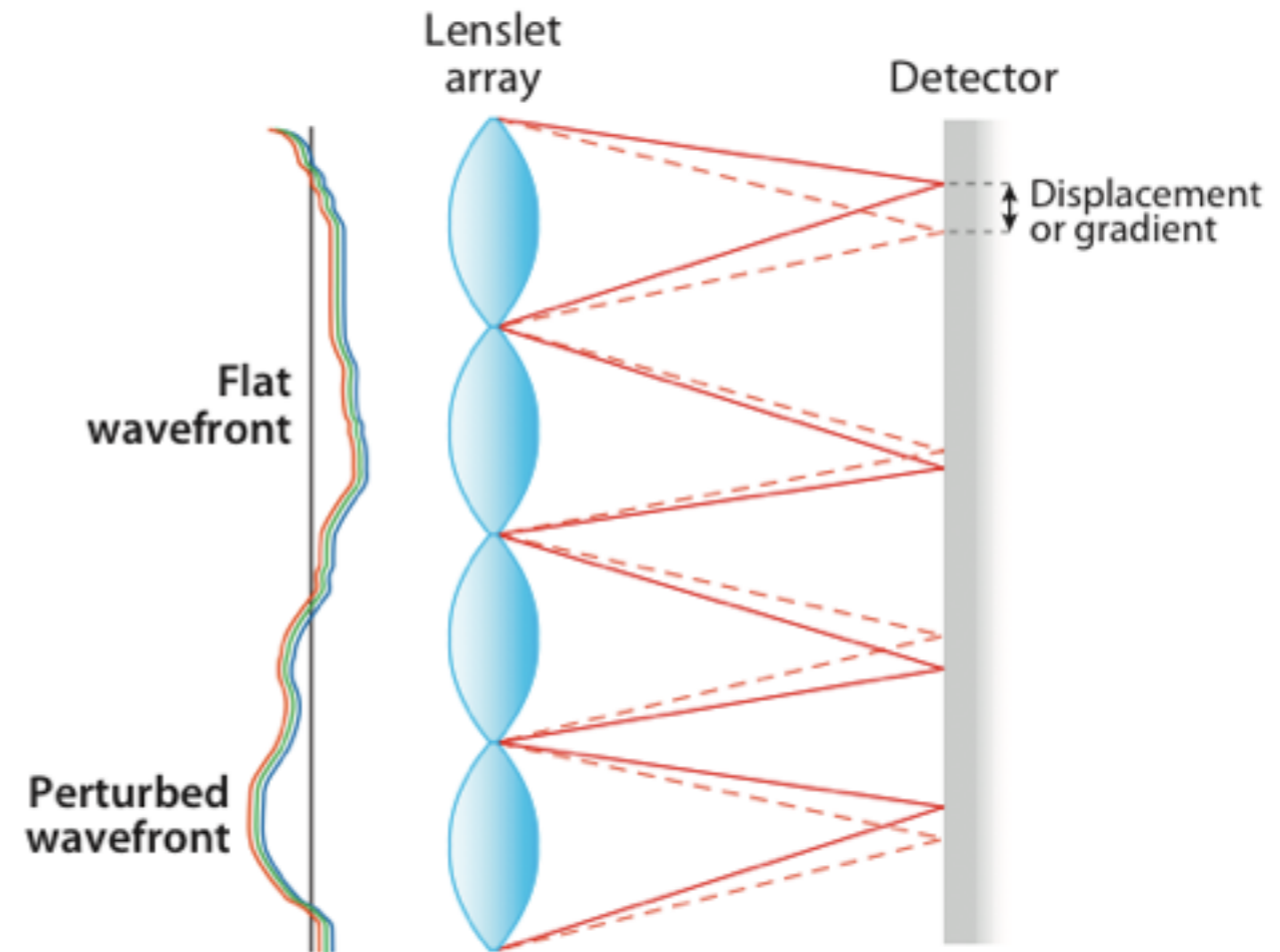


Wave Front Sensors

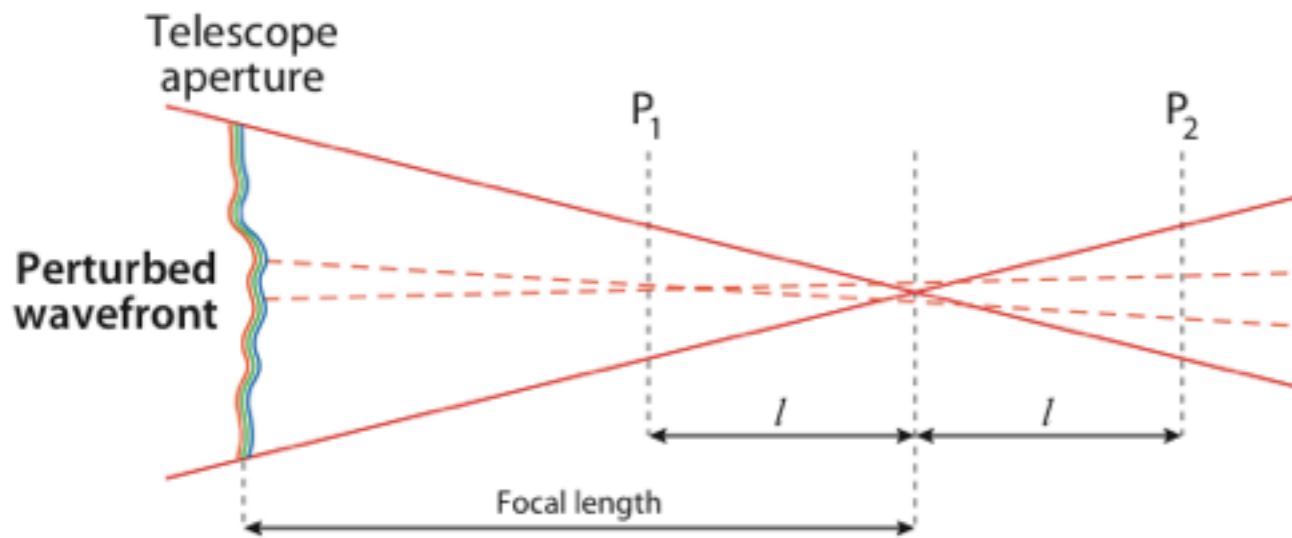
Pyramid WFS



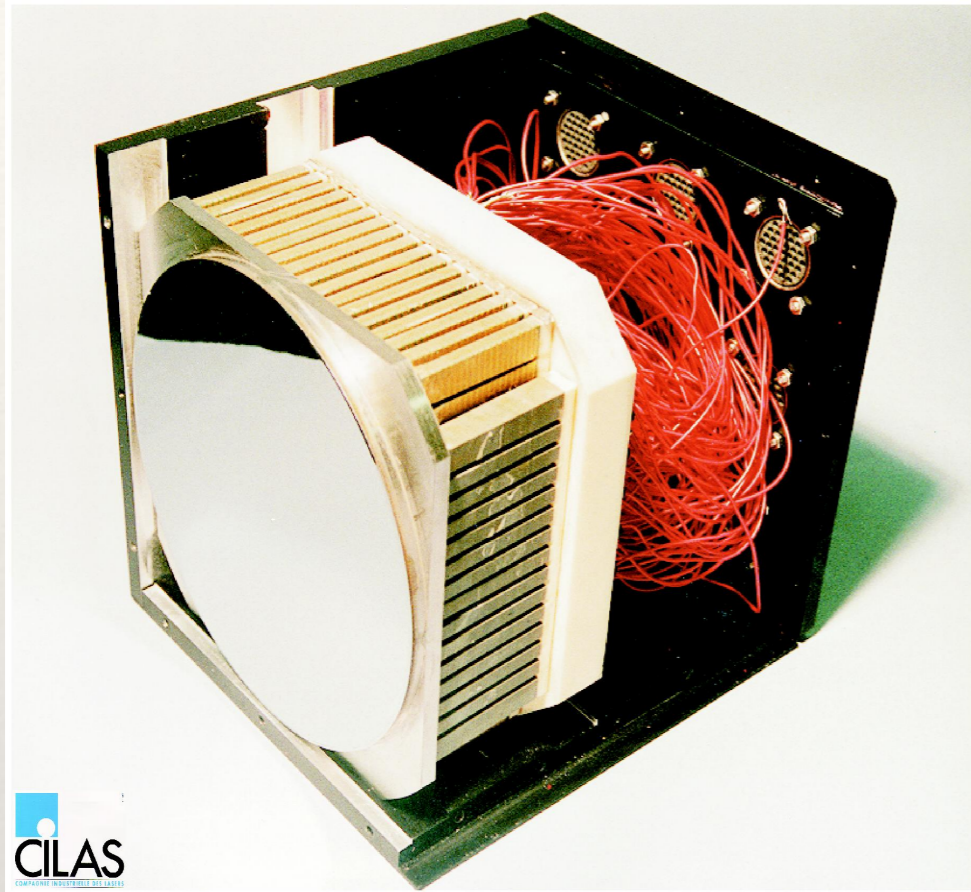
Shack-Hartmann WFS



Curvature WFS



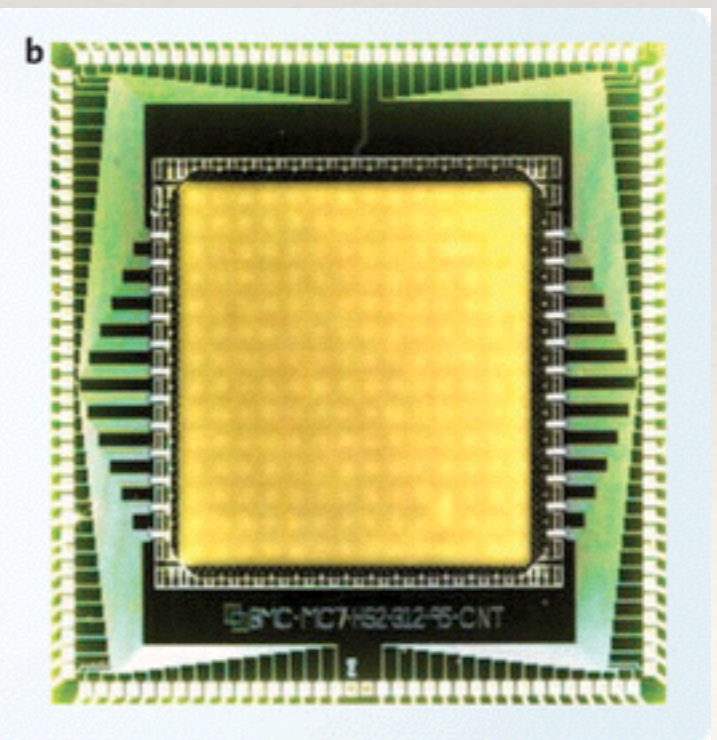
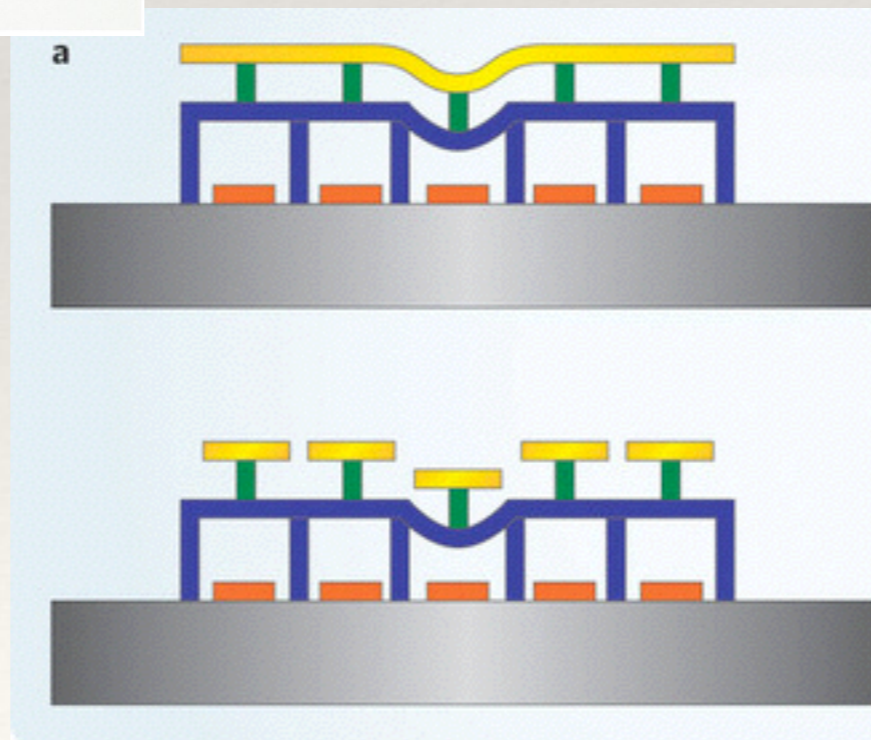
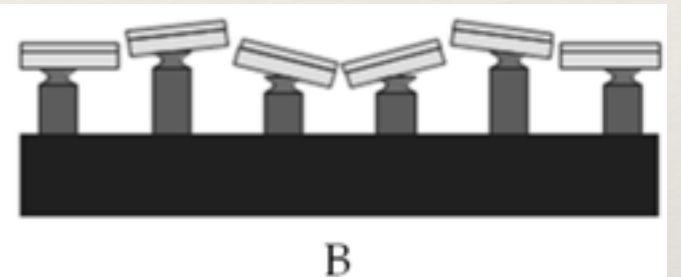
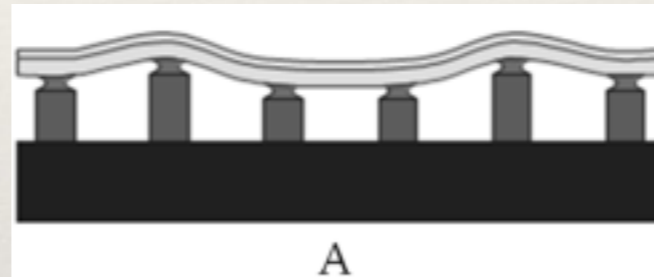
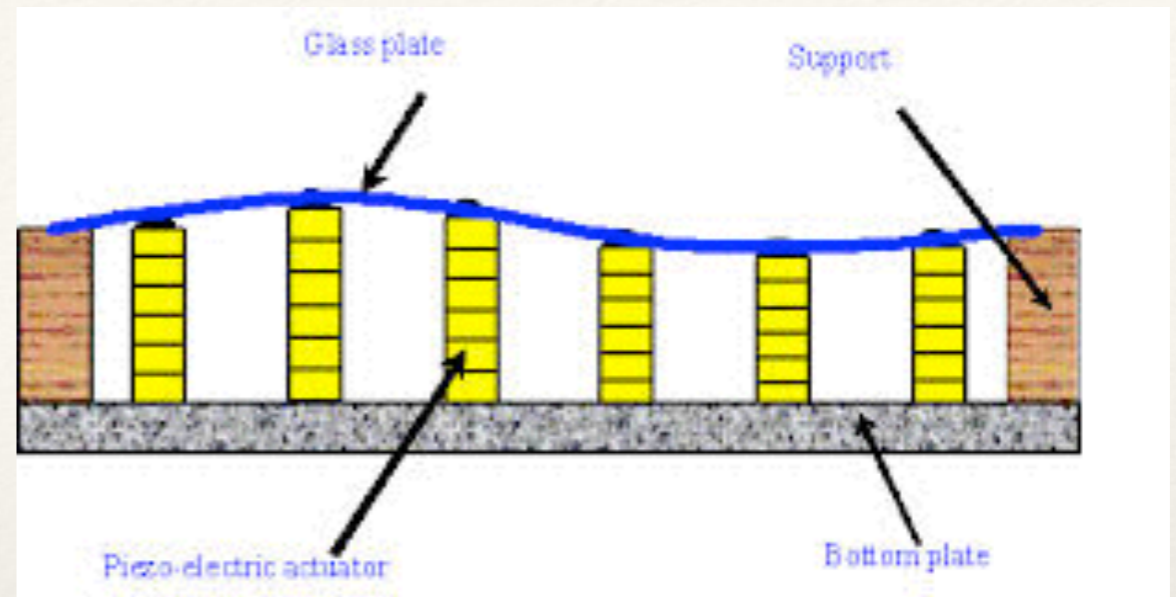
DEFORMABLE MIRRORs



Deformable mirror by CILAS
17 x 17 actuators

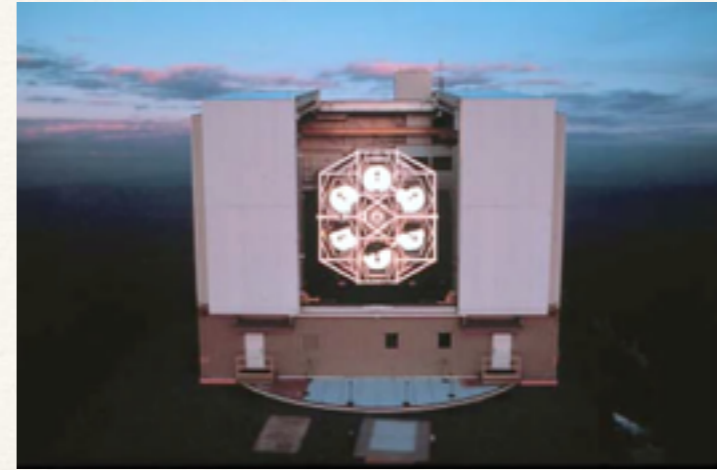
Several technologies ...

- piezo-electric
- micro mirror
- membranes

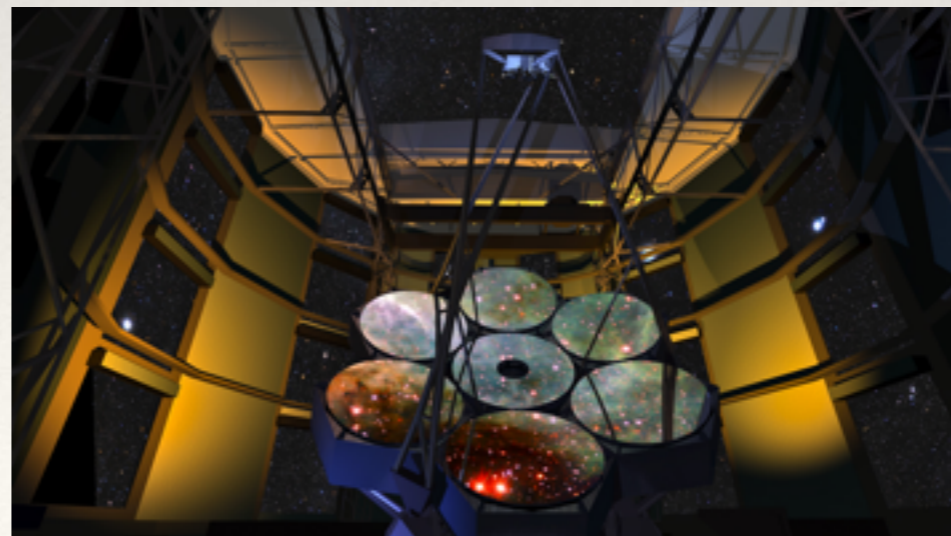


DEFORMABLE MIRRORS_s

Three main technologies:



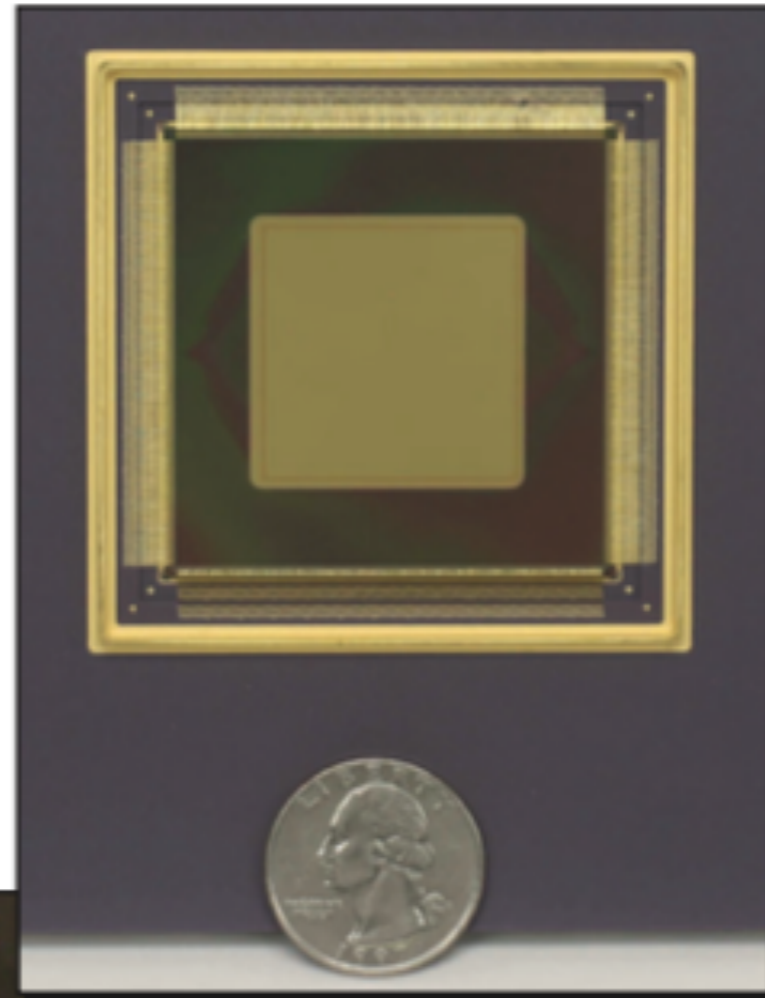
- Adaptive Secondary Mirrors (MMT; LBT; GMT; VLT)
- Piezo Deformable Mirrors (more common)
- Micro Optical Electrical Mechanical Systems (MOEMS)



Lab testing of the Large Binocular Telescope's adaptive secondary mirror system with 672 actuators



A 4,096-actuator micro-optical-electrical-mechanical system (MOEMS) DM



Piezo high-order 1,377-actuator DM for SPHERE

DEFORMABLE MIRRORS

DMs correct optical path difference (OPD) by advancing or retarding reflected beam:

- **same SHAPE of the WF**
- **1/2 amplitude of the WF**

Features:

- **# actuators: matching sub-aperture to avoid over or under-sampling**

- **update rate: accordingly to f_G**

$$f = 20-100 f_G$$

- **dynamic range (mechanical stroke)**

$$s = 0.15(D/r_0)^{5/6} \lambda$$

DM Classes

	Astronomy (10m class)	Astronomy (30m class)
Stroke	5 μm	10-15 μm
# actuators	350-2500	7000-10000
Frequency response	1-5 kHz	1-5 kHz
Mirror-Surface Errors (rms)	30 nm	30 nm
Aperture Size	1-15 cm	2-30 cm

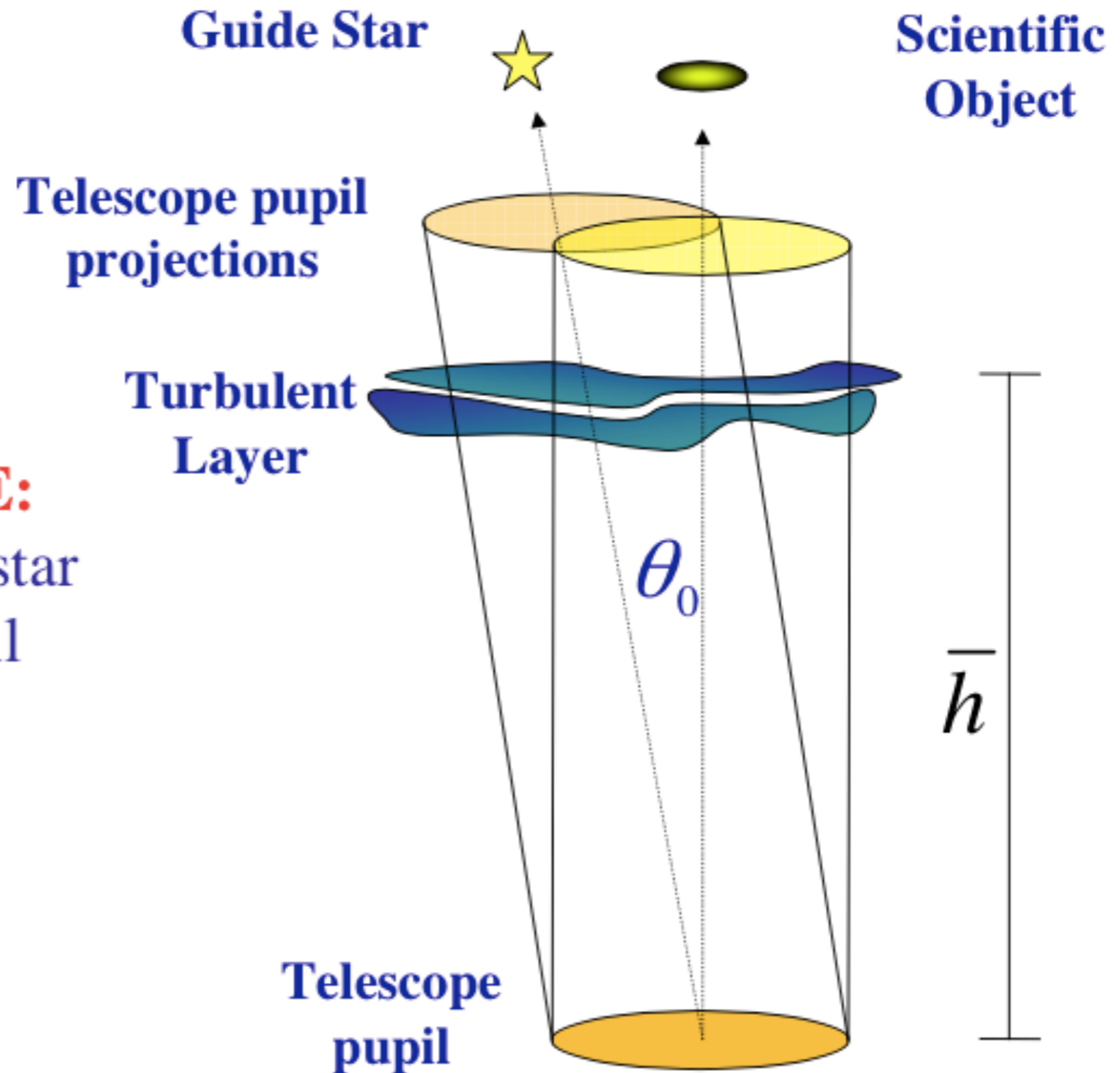
A Reference is needed

single-conjugate adaptive optics (SCAO)

ISOPLANATIC ANGLE:

Angle from the reference star where the correction is still effective

$$\theta_0 \propto r_0 / \bar{h}$$

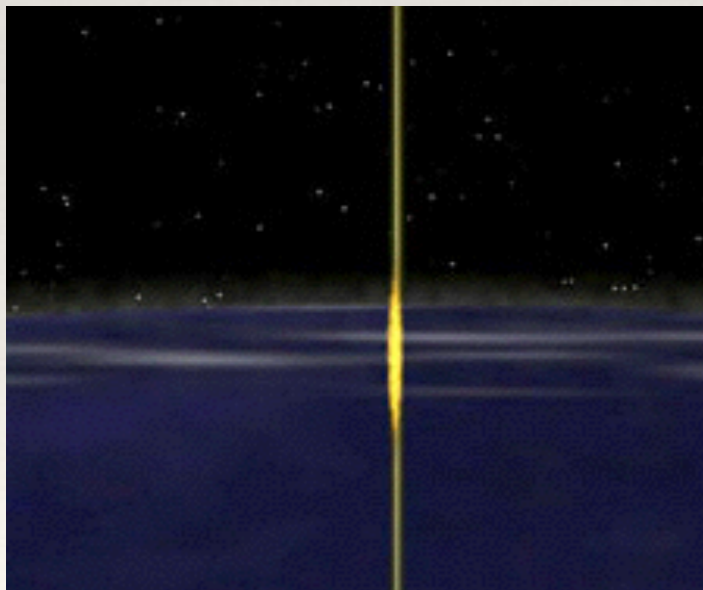
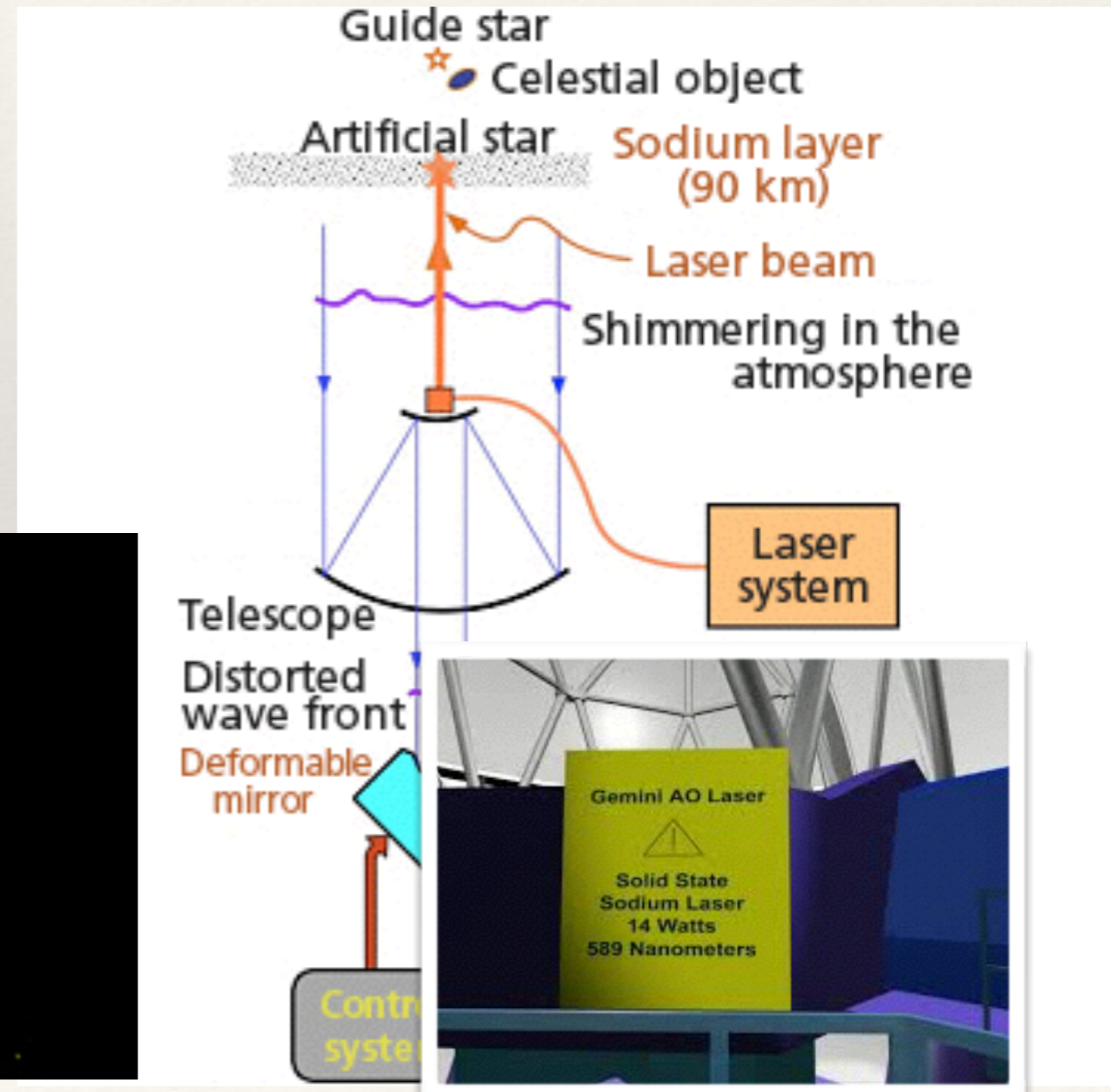




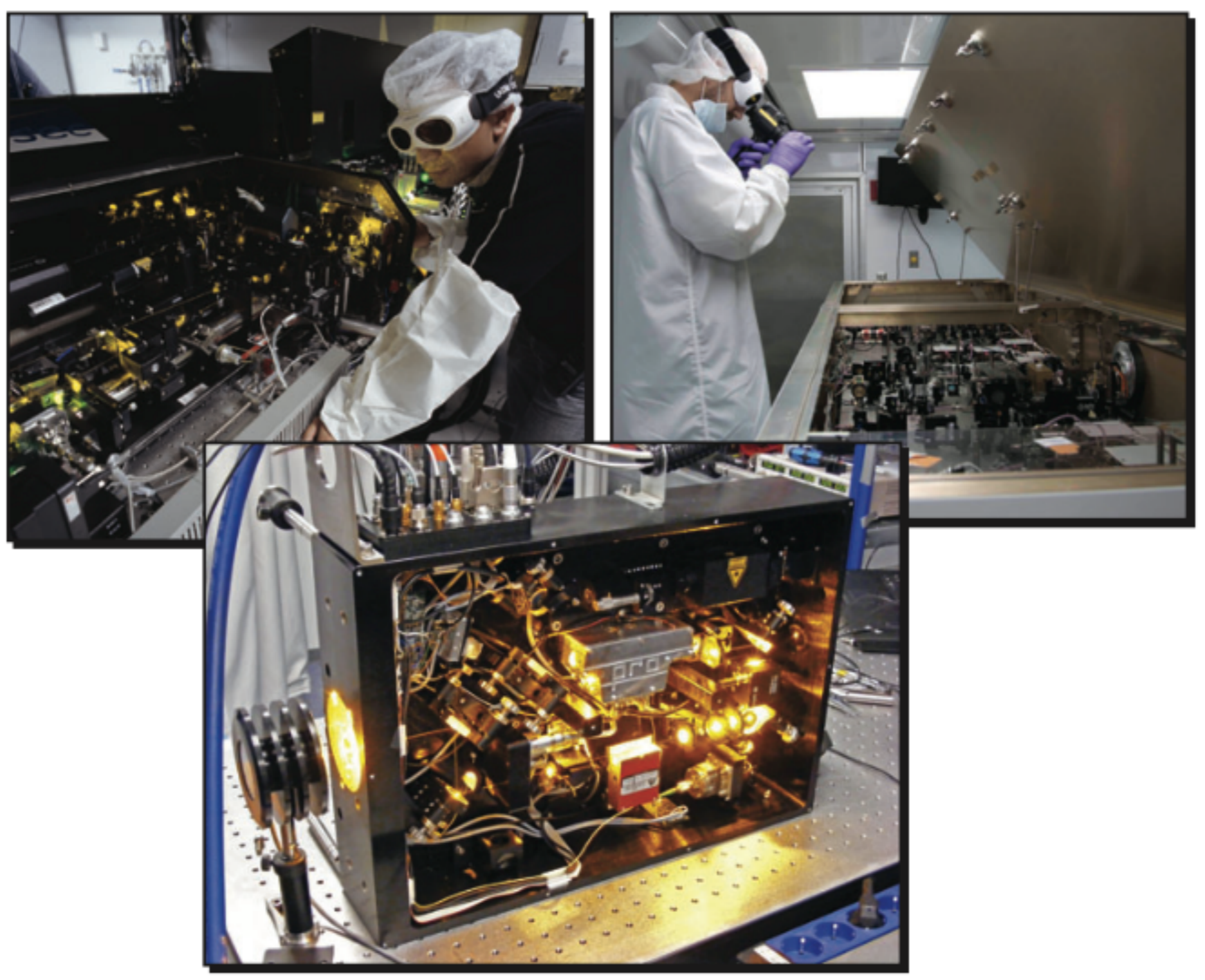
Laser Guide Star (LGS)

For a reasonable correction performance, AO systems need sufficiently bright (~ 15 mag) guide stars within θ_0 of the astronomical target.

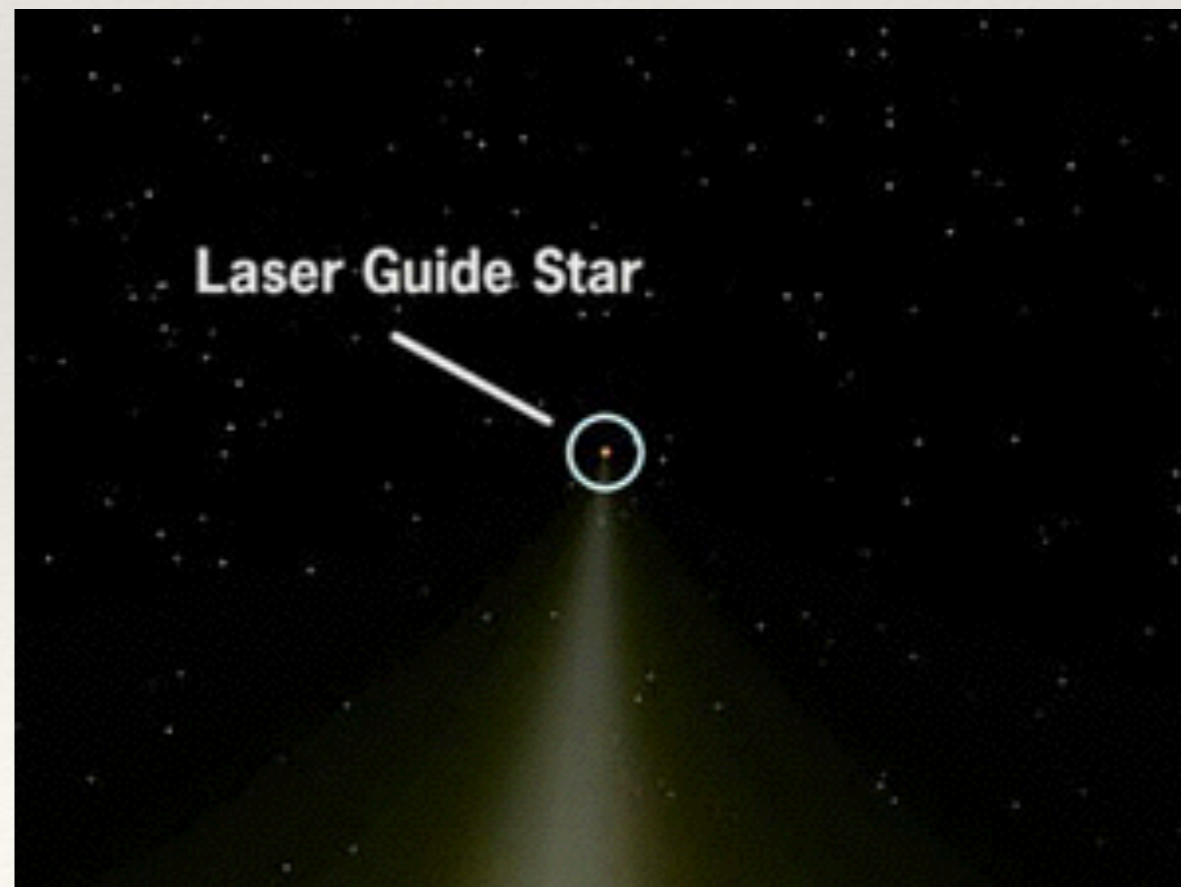
- ☑ Rayleigh Scattering (30km)
- ☑ Resonance fluorescence of sodium atoms (90km)



Laser Guide Star (LGS)

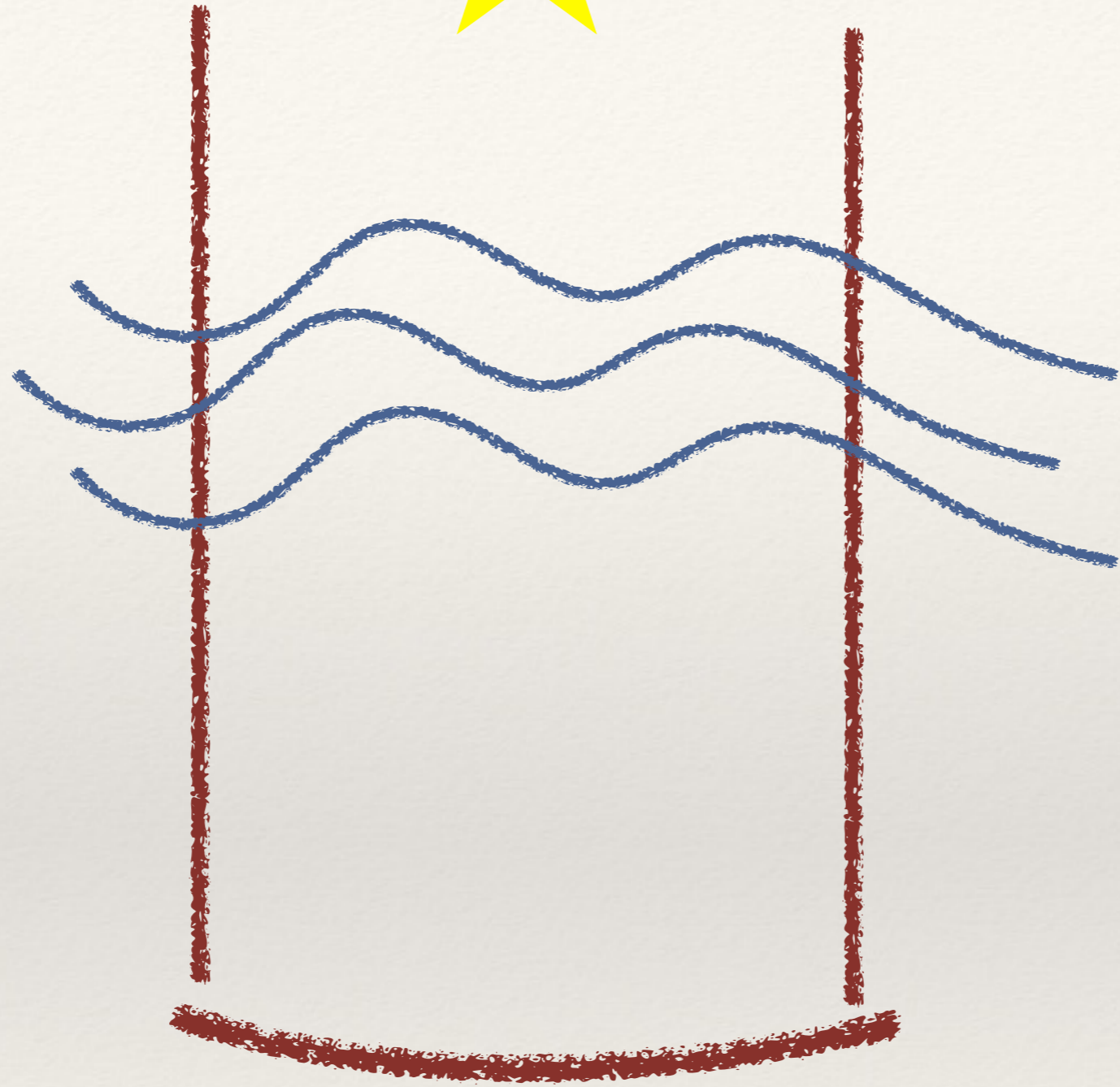


Davies & Kasper, 2012



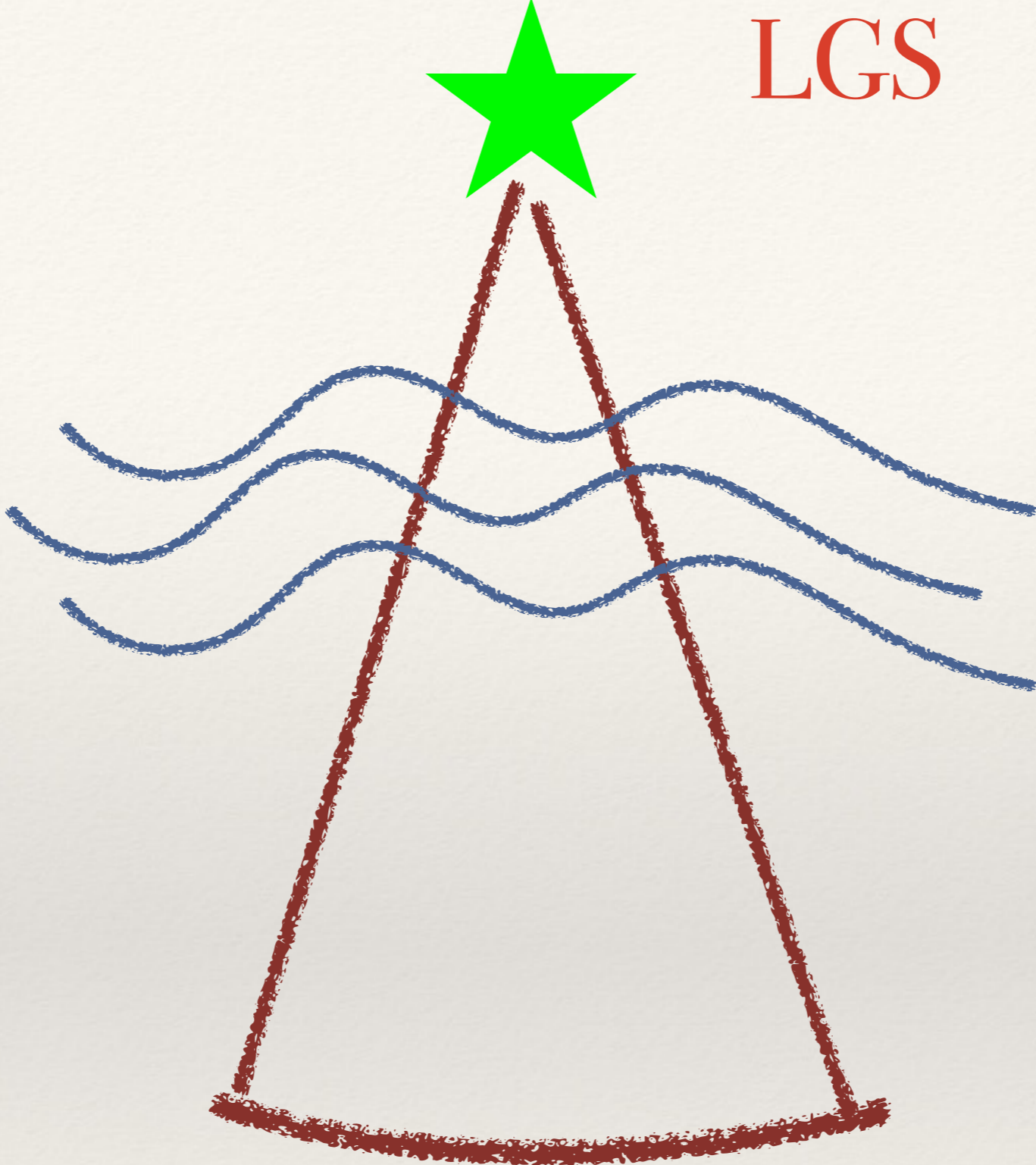


NGS



Mirror

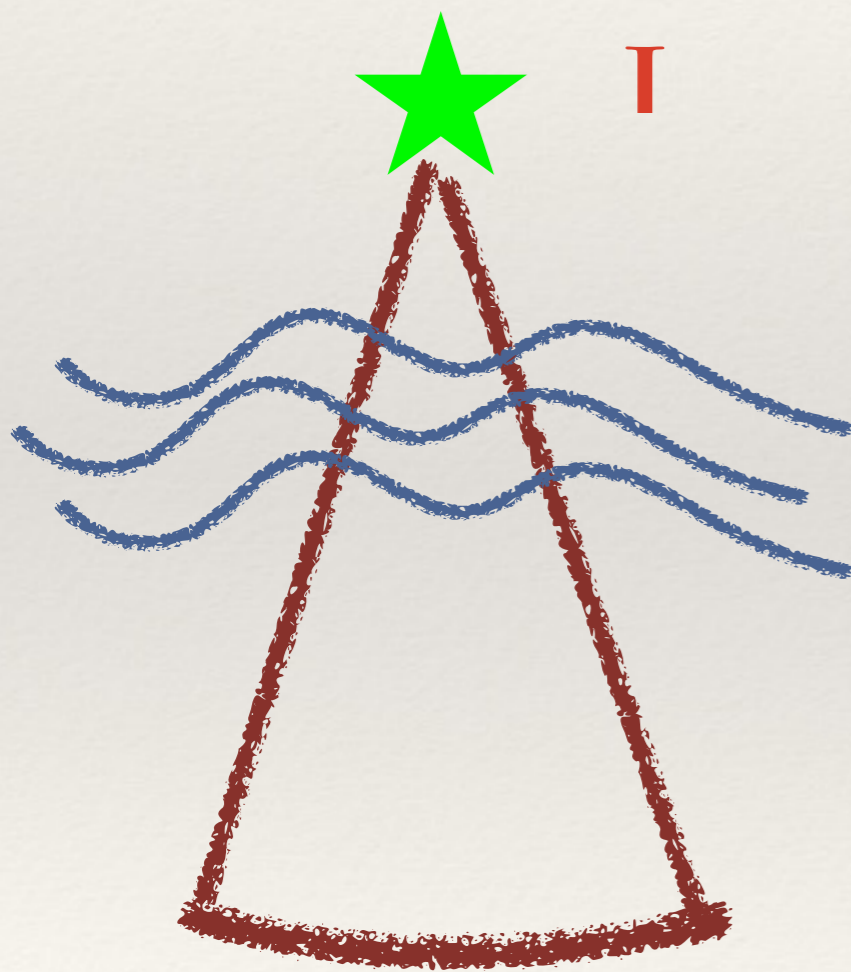
LGS



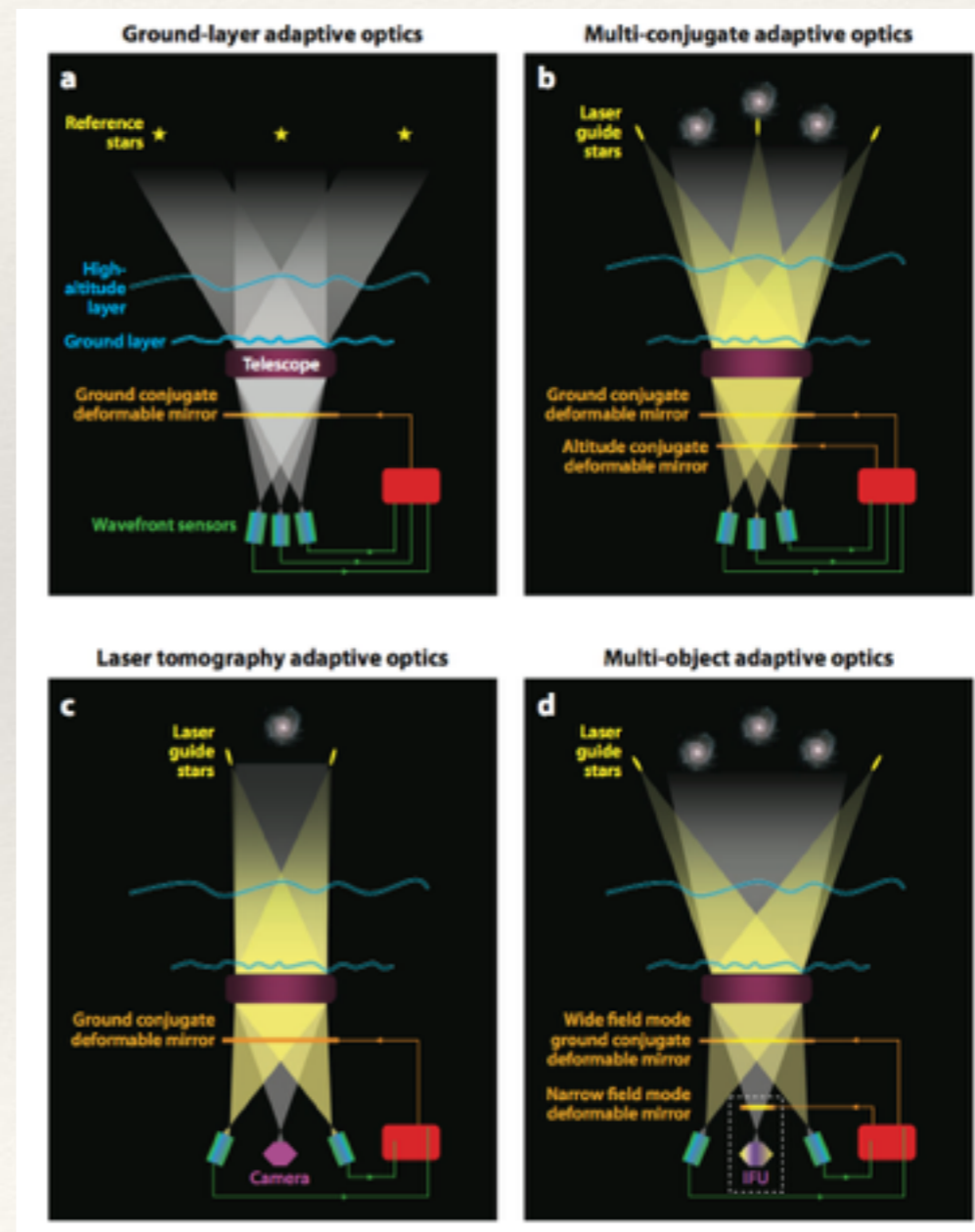
Mirror

CONE EFFECT

on telescope of 8 m could reduce the Strehl ratio of a factor of 0.6 in J and 0.85 in K

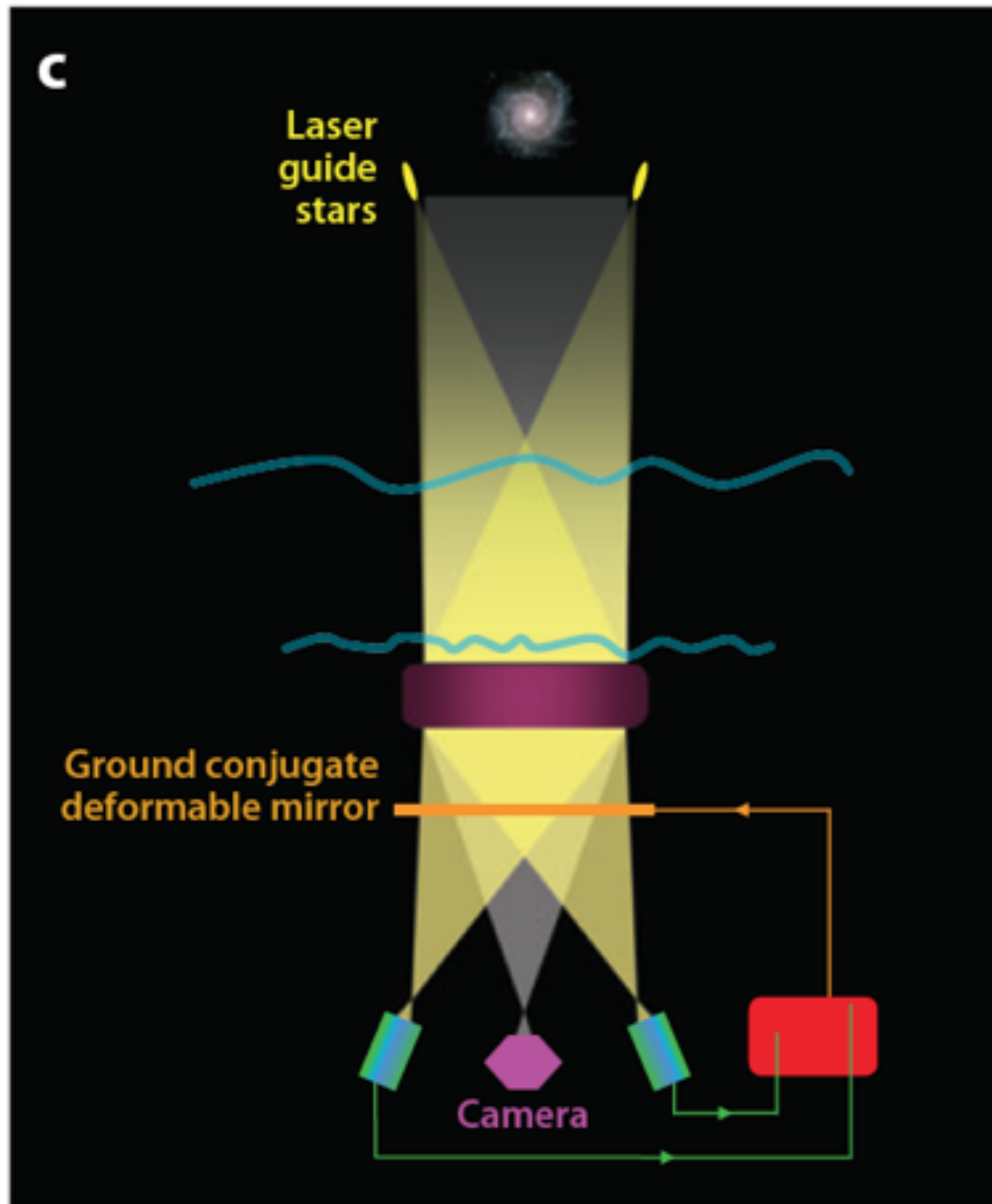


Mir



Laser Tomography Adaptive Optics

Laser tomography adaptive optics

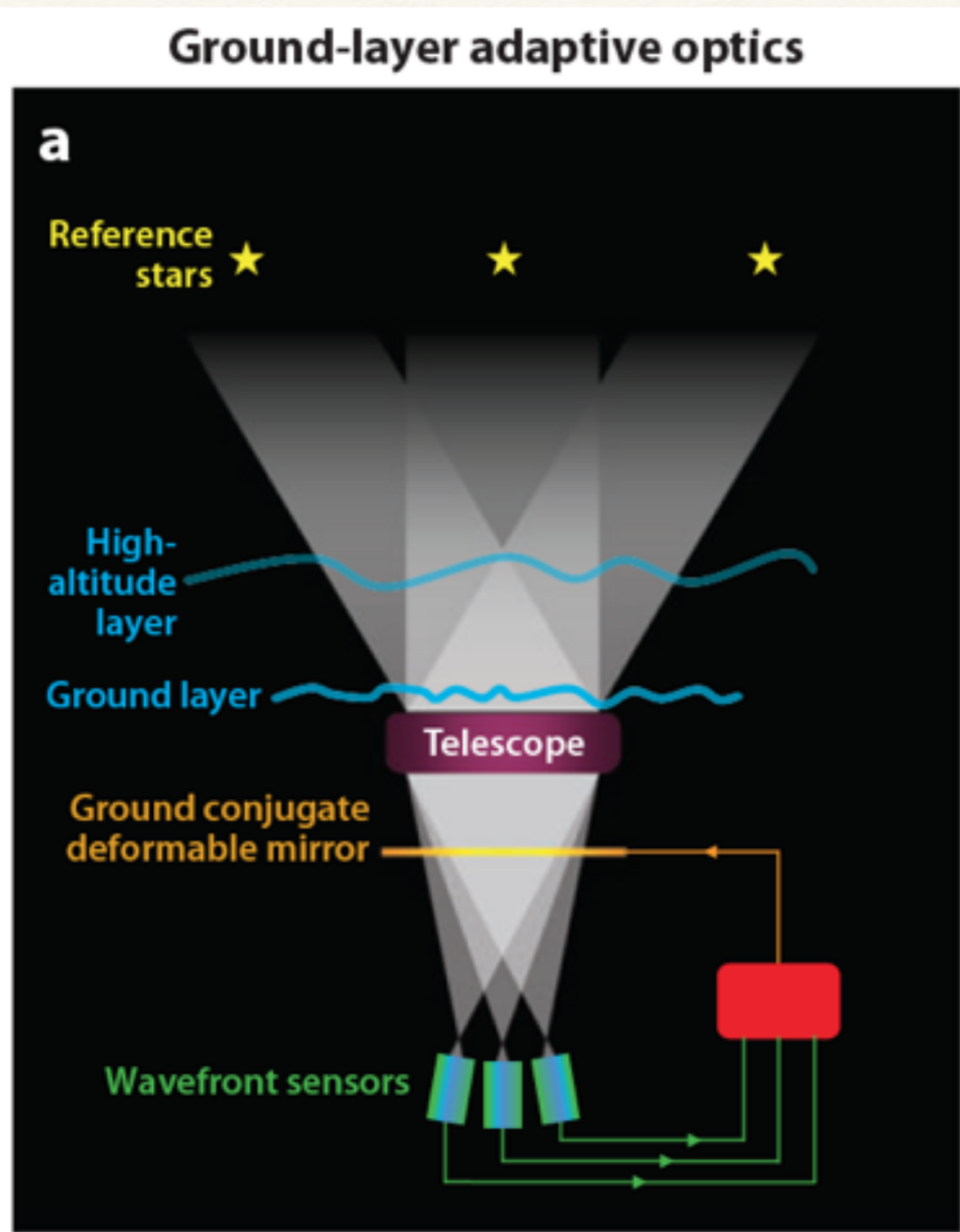


In order to contrast the Cone Effect Different LGSs are used.

Very Important:

the two cones have to superimpose on the turbulent zone

Ground Layer Adaptive Optics



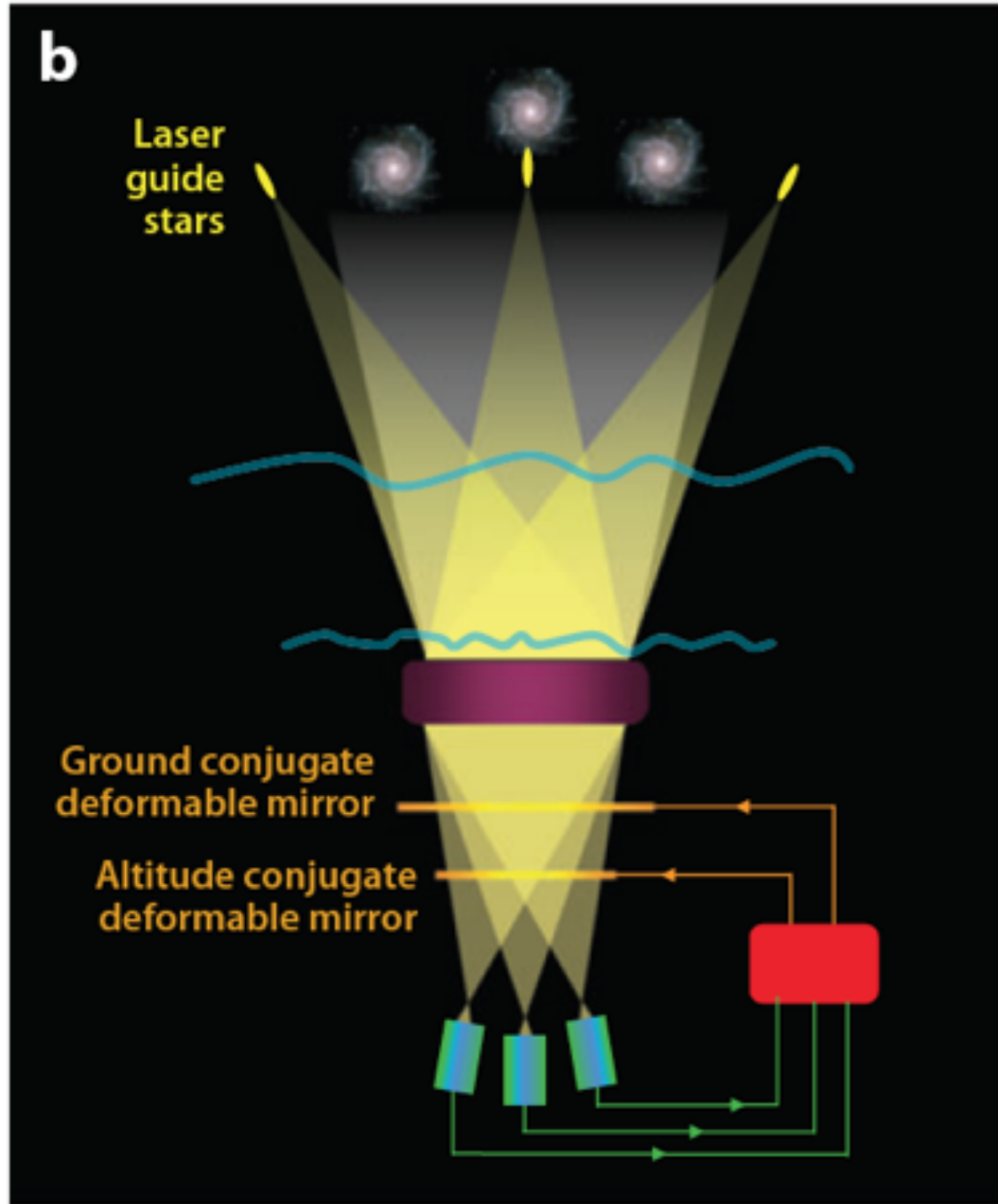
Correction only for the ground Layer. All rays (also those off axis) pass through this layer ...

Advantages:

- Larger Field of View
- correction is independent by the distance of Guide star

Multi Conjugate Adaptive Optics

Multi-conjugate adaptive optics



Several reference stars - Partial superimposition of cones on the turbulent layers and completely superimposed at lower height. Two or three different turbulent layers each conjugate with a deformable mirror

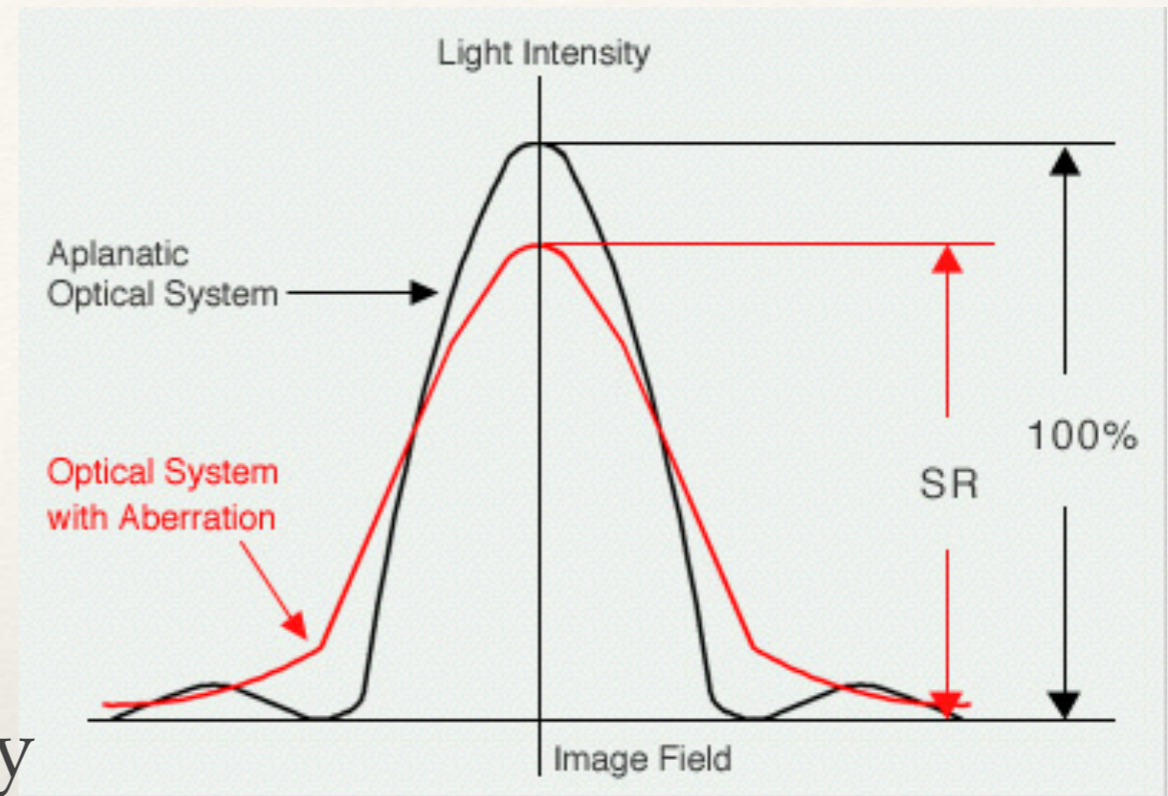
Strehl Ratio

The AO Correction is never perfect

The Strehl ratio (SR) is the ratio between the intensity of the central peak as given by AO and the diffraction peak

Residual Wavefront error (and SR) mainly depends on:

- ✓ Pupil Sampling (Fried radius)
- ✓ Temporal Sampling (coherence $t_0 \sim 2\text{ms}$)



Marechal approximation
 $SR = \exp[-(2\pi WFE / \lambda)^2]$



NACO

~ 200 Actuators ($\sim 3r_0$) WFE $\sim 250\text{nm}$

XAO (SPHERE)

~ 1400 Actuators (r_0) WFE $\sim 90\text{nm}$

Outer Working Angle

- ✓ The number of actuators limits the number of modes that are corrected
- ✓ Nyquist sampling limits the radius of the PSF region where correction is obtained (Outer working angle = OWA)
- ✓ OWA is given by the separation between actuators as projected on the telescope primary:

$$\text{OWA} \sim 1/2(\lambda/D) (n_{\text{actuators}})^{1/2}$$

- ✓ If $n_{\text{actuators}} \sim 1400$, $\text{OWA} \sim 20 \lambda/D$

Some Numbers

	lambda	SR (AO)	SR (XAO)	OWA
	(μm)	200 act.	1400 act.	(arcsec)
		NACO	SPHERE	
WFE (nm)		250	90	
R	0.64	0.00	0.46	0.31
I	0.79	0.02	0.60	0.38
z	0.95	0.07	0.70	0.46
J	1.25	0.21	0.82	0.60
H	1.65	0.40	0.89	0.79
K	2.20	0.60	0.94	1.06
L'	3.80	0.84	0.98	1.83

Adaptive Optics Science

SOLAR SYSTEM

SUN

ASTEROIDS

PLANETS

STELLAR FORMATION

STELLAR MULTIPLICITY

CIRCUMSTELLAR DISKS

EXOPLANETS

RESOLVED STELLAR POPULATIONS

THE GALACTIC CENTER

GALAXY NUCLEI AND ACTIVE GALAXIES

BLACK HOLE MASSES

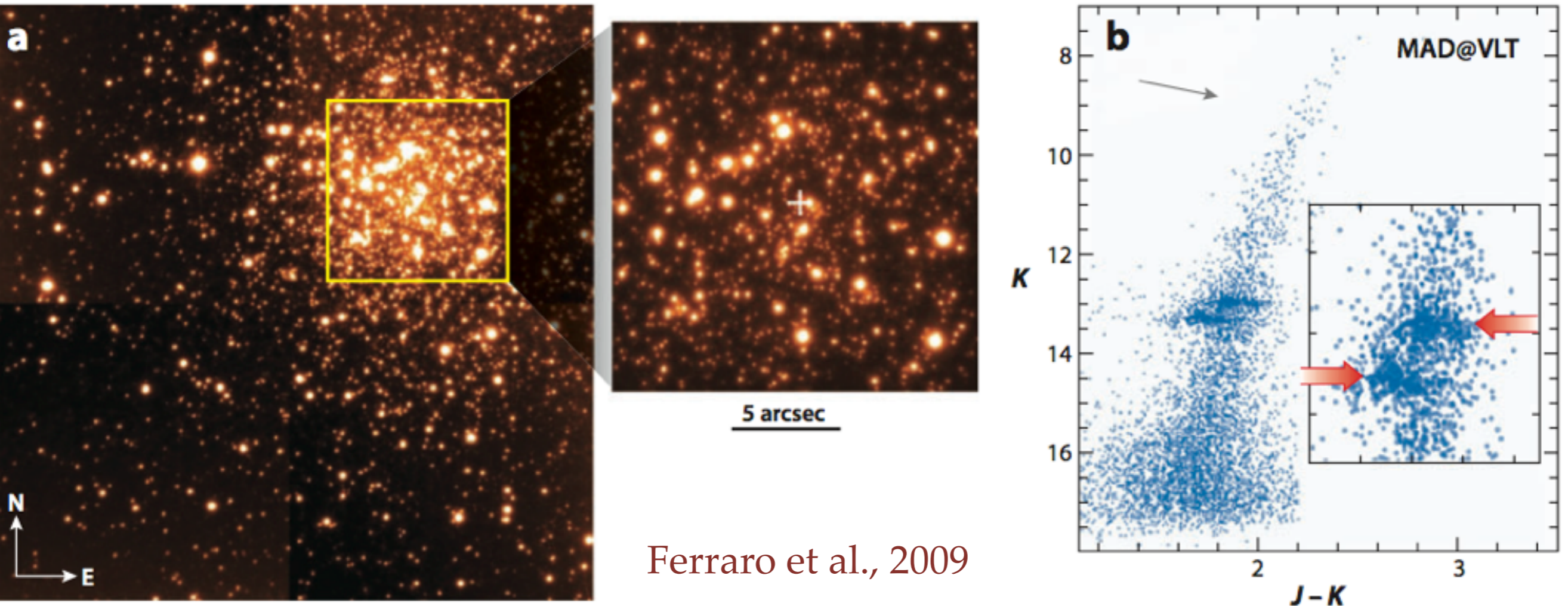
GAS INFLOW AND OUTFLOW

QUASAR AND MERGER

THE HIGH REDSHIFT UNIVERSE

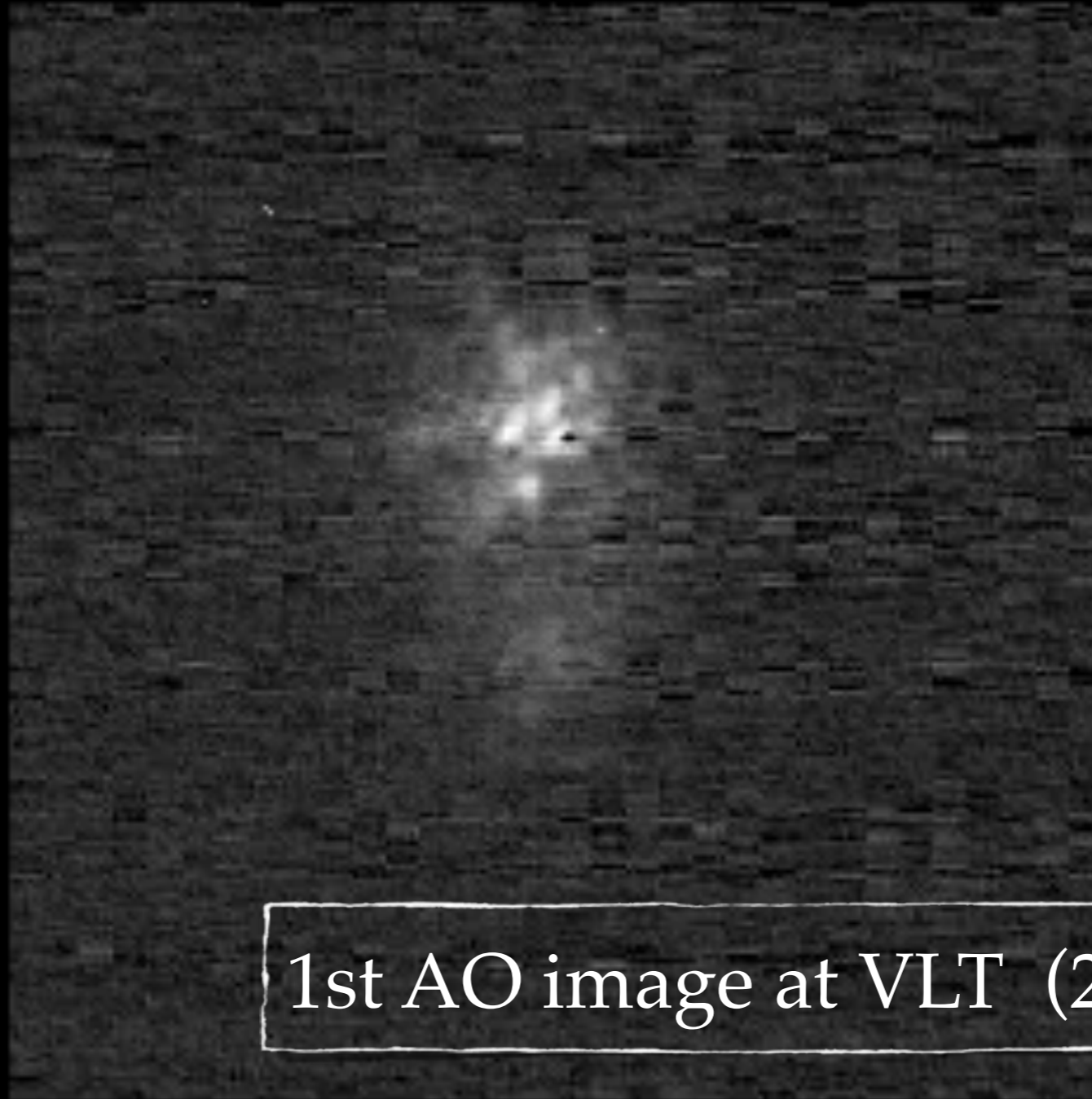
Globular Cluster: Terzan 5 with MAD

MAD (Multi conjugate AO Demonstrator) is designed to perform wide Field of View (FoV) adaptive optics correction in **K band** ($2.2 \mu\text{m}$) over **2 arcmin** on the sky by using relatively bright ($m_v < 14$) Natural Guide Stars (NGS).



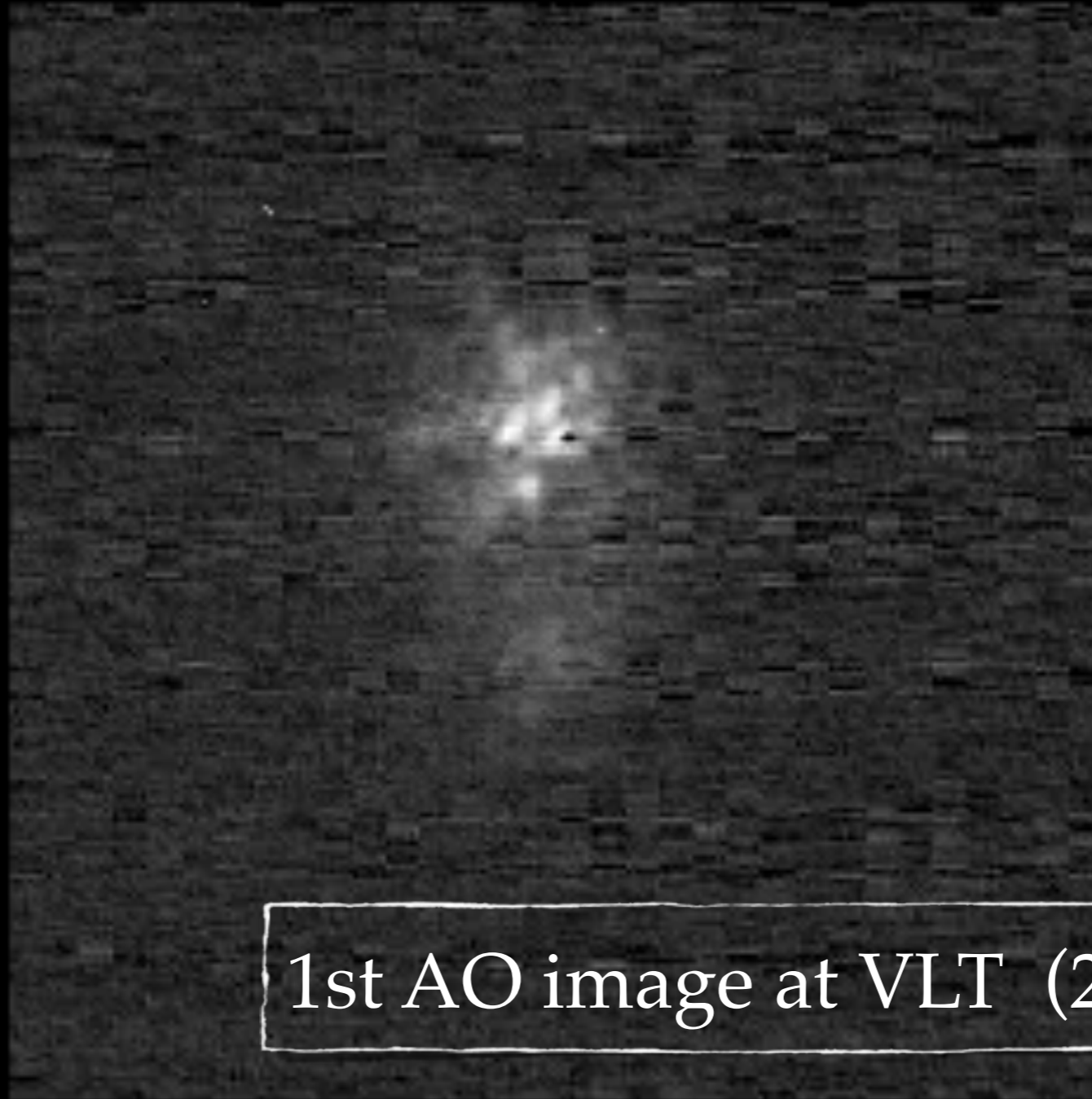
Resolution of 0.1 arcsecond on a FoV of 60 arc seconds

Adaptive Optics



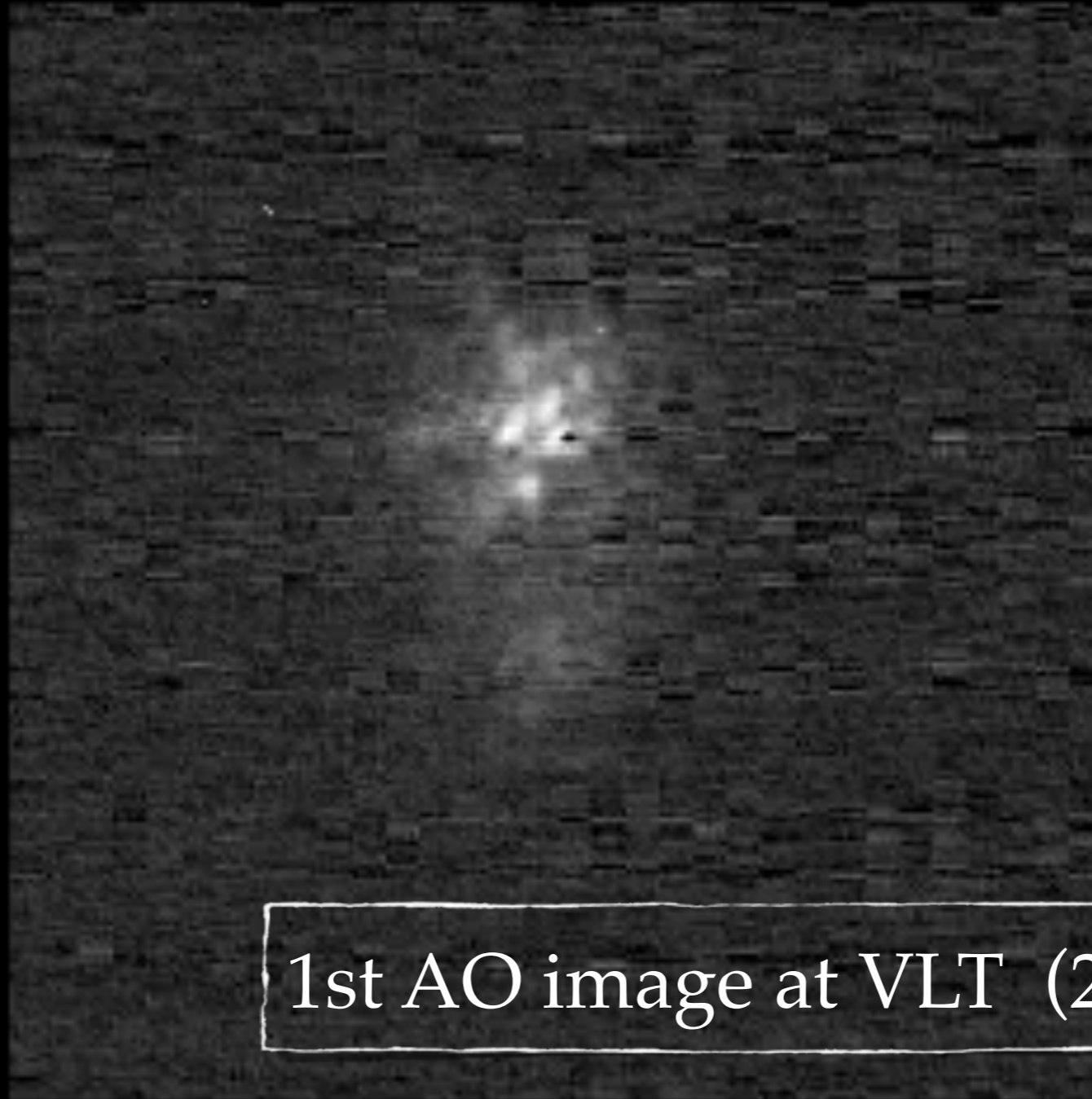
1st AO image at VLT (2001)

Adaptive Optics



1st AO image at VLT (2001)

Adaptive Optics



1st AO image at VLT (2001)