

# Magnetism and Superconductivity

David J. Singh  
Oak Ridge National Laboratory

“Oh, East is East, and West is West, and never the twain shall meet” (Rudyard Kipling)

Main co-worker: Igor I. Mazin

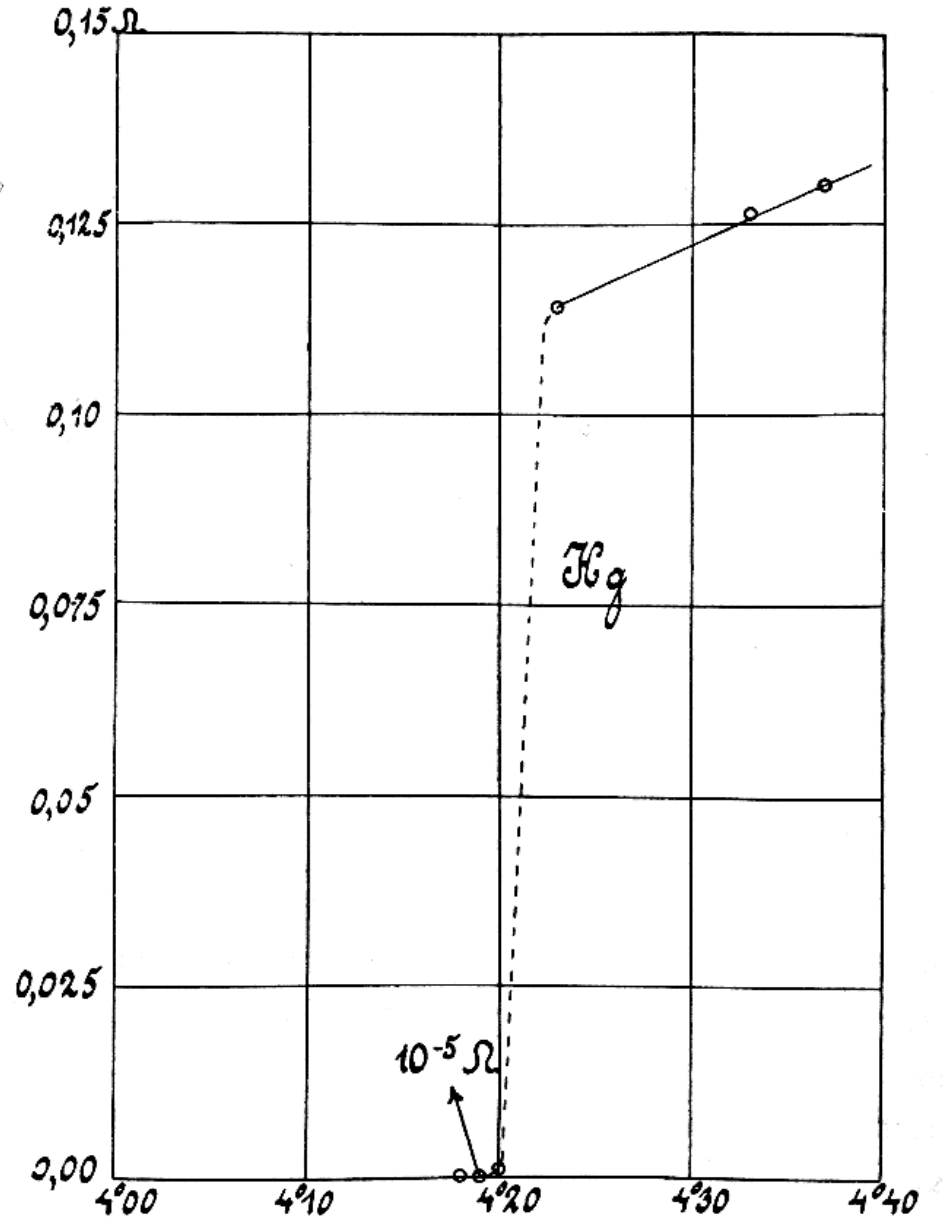


Supported by DOE, BES, Materials Sciences and Engineering and the S3TEC EFRC.

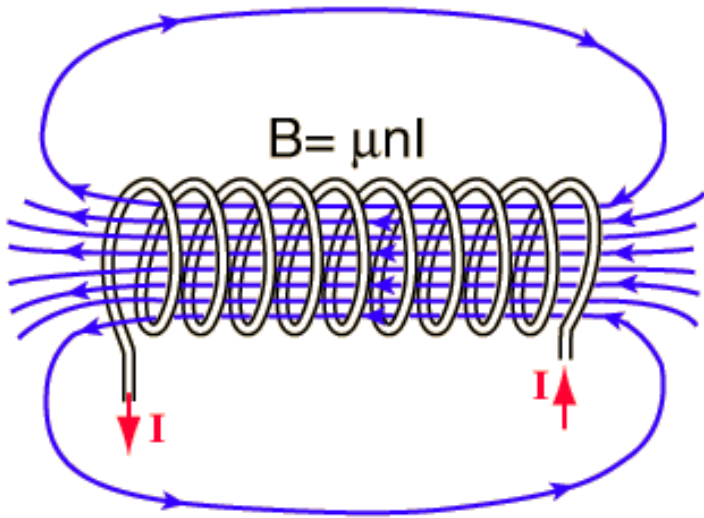
# Superconductivity - 1911



H. Kamerlingh Onnes



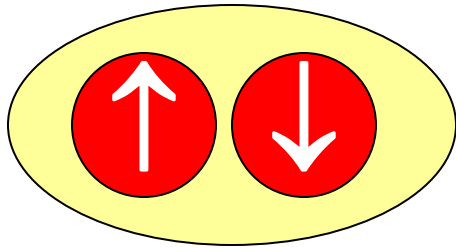
# Uses



Limited by critical field, critical current, critical temperature

# Bardeen Cooper Schrieffer - 1957

Singlet ( $s, d$ )



electron - polarization - electron

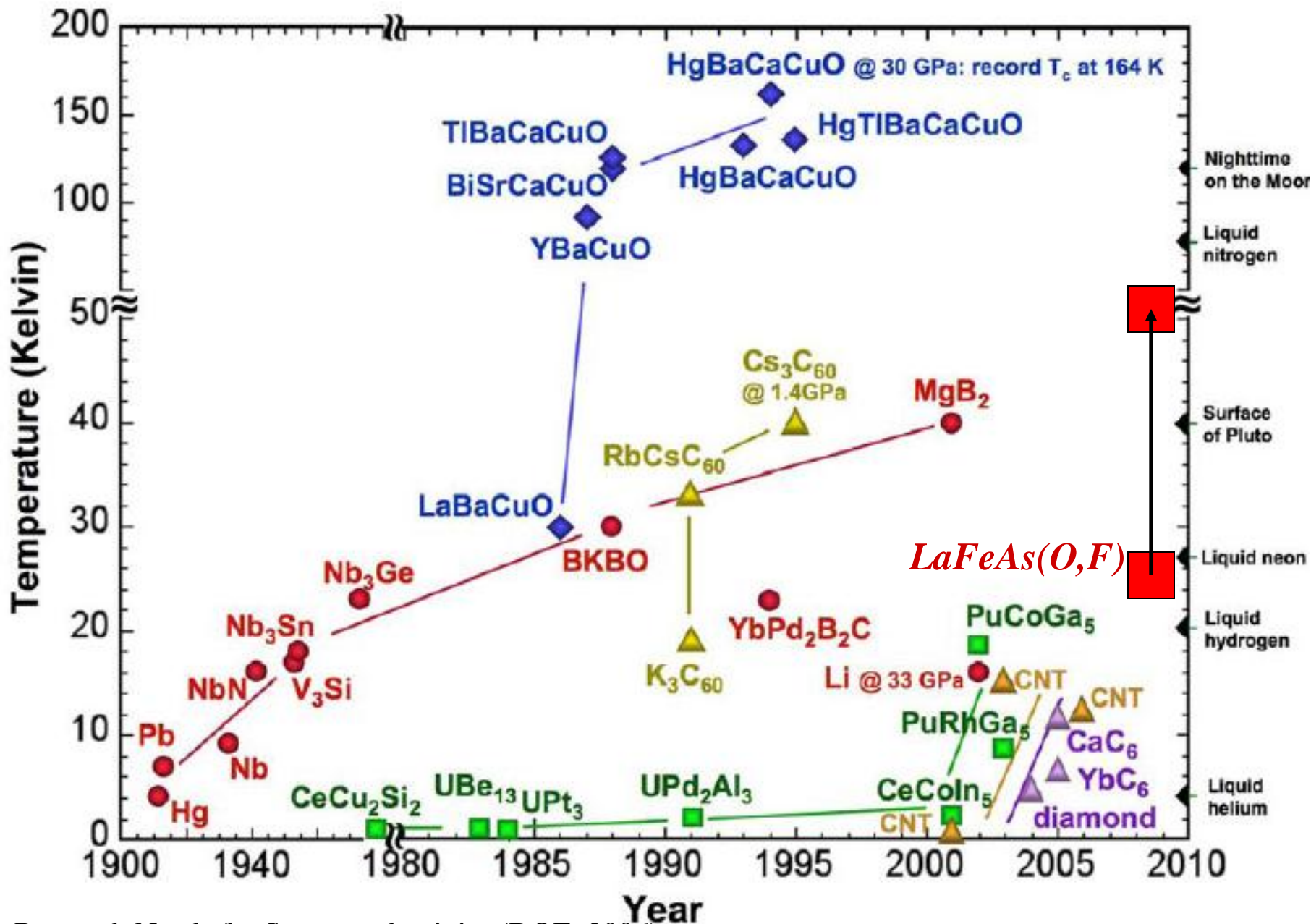
Hg, Pb, Cuprates

*Singlet Channel:*

*Charge fluctuations (phonons) are attractive.  
Ferromagnetic fluctuations are pair breaking  
Spin fluctuations in general are repulsive.*

Since electron phonon is always attractive the  $s$ -wave channel is most favored by it.

# Materials



<sup>4</sup>P. W. Anderson and A. H. Dayem, Phys. Rev. Letters 13, 195 (1964). See also J. Lambe, A. H. Silver, J. E. Mercereau, and R. C. Jaklevic, Phys. Letters 11, 16 (1964).

<sup>5</sup>A. H. Dayem and C. C. Grimes, Appl. Phys. Letters 9, 47 (1966).

<sup>6</sup>P. L. Richards, J. Opt. Soc. Am. 54, 1474 (1964).

<sup>7</sup>E. Riedel, Z. Naturforsch. 19a, 1634 (1964).

<sup>8</sup>N. R. Werthamer, Phys. Rev. 147, 255 (1966).

<sup>9</sup>I. K. Yanson, V. M. Svistunov, and I. M. Dmitrenko, Zh. Eksperim. i Teor. Fiz. 48, 976 (1965) [translation: Soviet Phys.—JETP 21, 650 (1965)]; D. N. Langenberg, D. J. Scalapino, B. N. Taylor, and R. E. Eck, Phys. Rev. Letters 15, 294, 842(E) (1965); D. N. Langenberg, D. J. Scalapino, and B. N. Taylor, Proc. IEEE 54, 560 (1966).

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#### EFFECT OF FERROMAGNETIC SPIN CORRELATIONS ON SUPERCONDUCTIVITY\*

N. F. Berk and J. R. Schrieffer

Department of Physics, University of Pennsylvania, Philadelphia, Pennsylvania

(Received 24 June 1966)

*Pd is not a superconductor because  
of nearness to ferromagnetism.*

# Inferred Phase Diagram

*Competition of superconductivity  
and magnetism.*

$T$

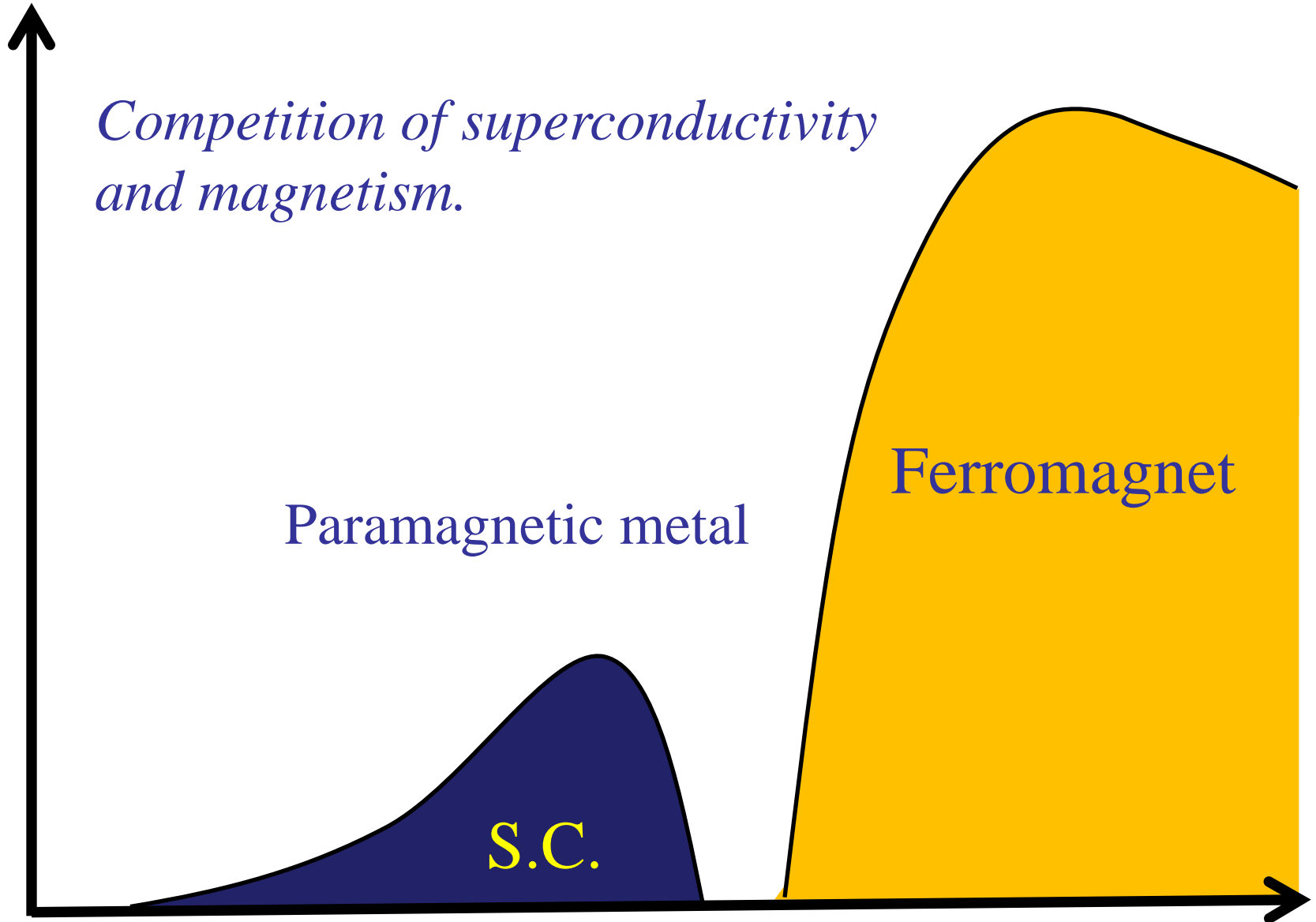
Paramagnetic metal

Ferromagnet

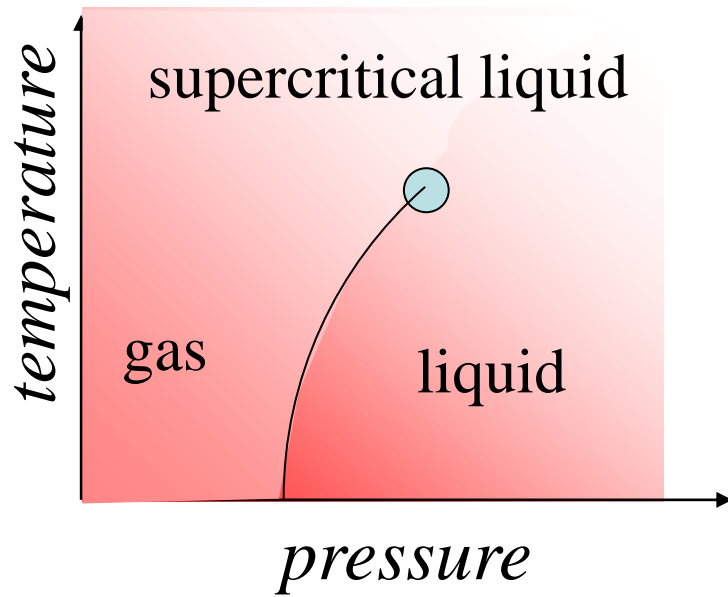
S.C.

$N(E_F)I$

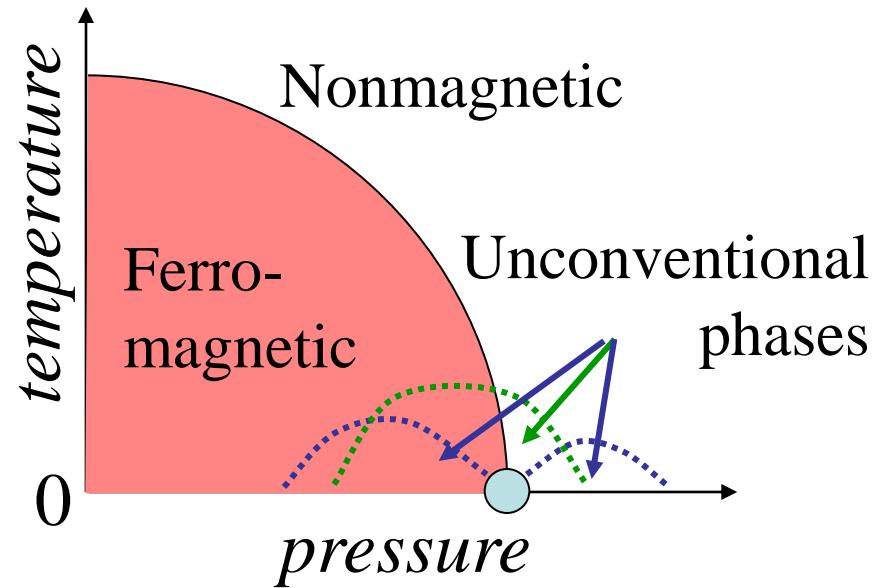
1.0



# Metals Near Quantum Critical Points



Classical criticality: Thermal density fluctuations grow indefinitely close to the Critical Point (CP).

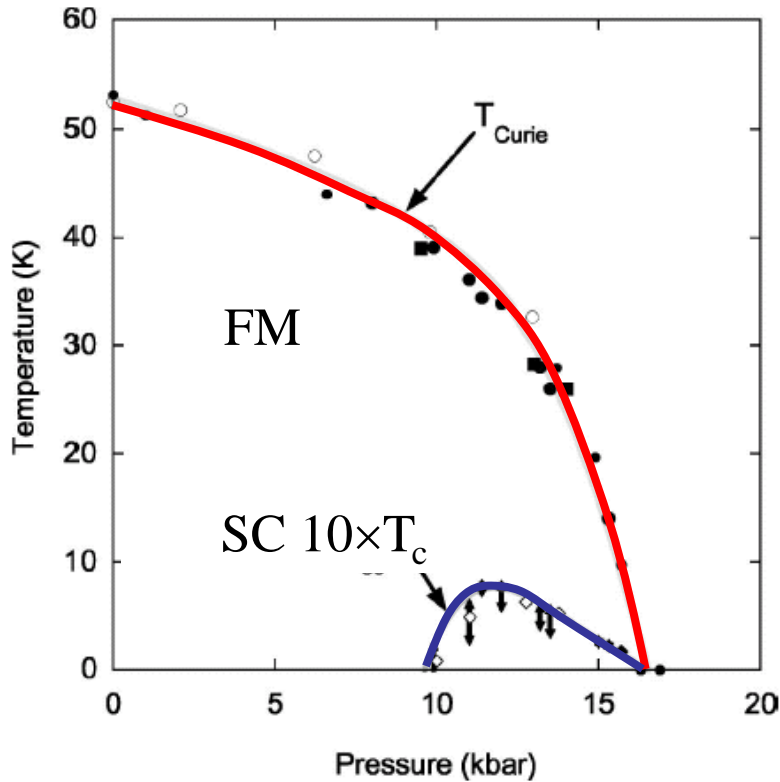


Quantum criticality: Quantum density fluctuations grow indefinitely close to the Quantum Critical Point (QCP).

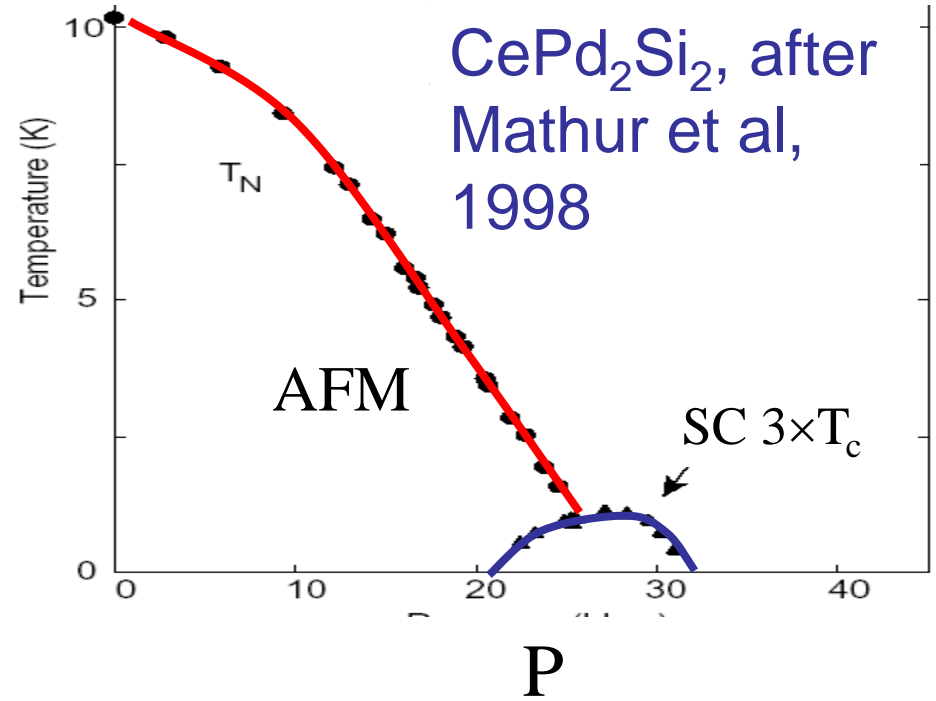
Interesting things happen near critical points: In this region fluctuations are important and DFT does badly.



# Something Different?



$\text{UGe}_2$ , after Huxley et al, 2001  
and Saxena et al, 2000

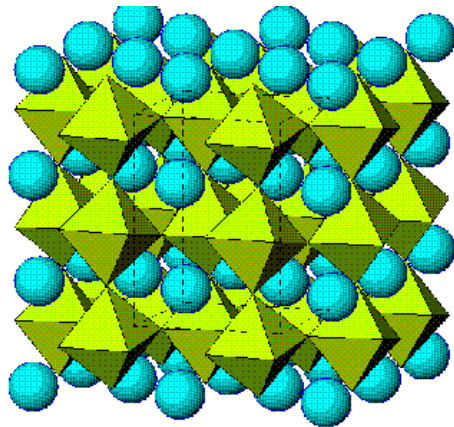


*Interesting things may happen near critical points: In this region fluctuations are important and DFT does badly.*

# “Strontium Ruthenate”

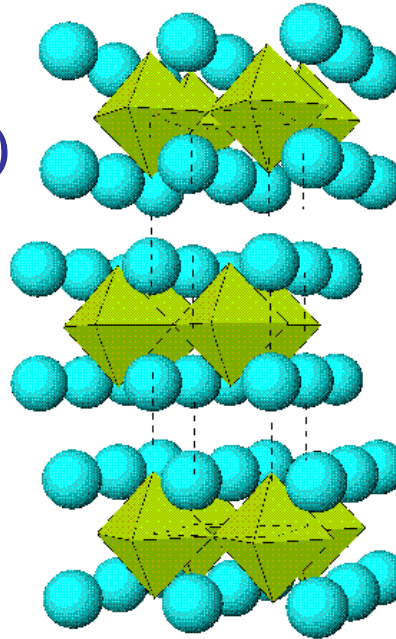


$\text{Ru}^{4+}$  (4 d-electrons)



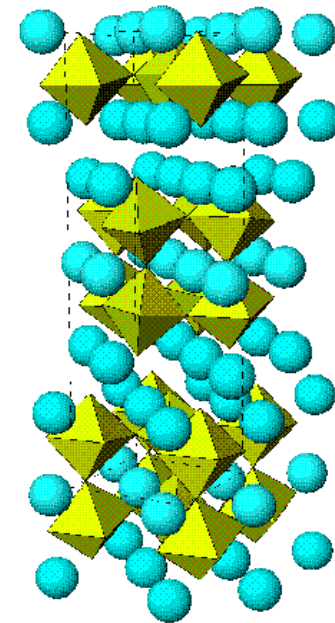
$n = \infty$

Ferromagnet



$n = 1$

Triplet  
superconductor



$n = 2$

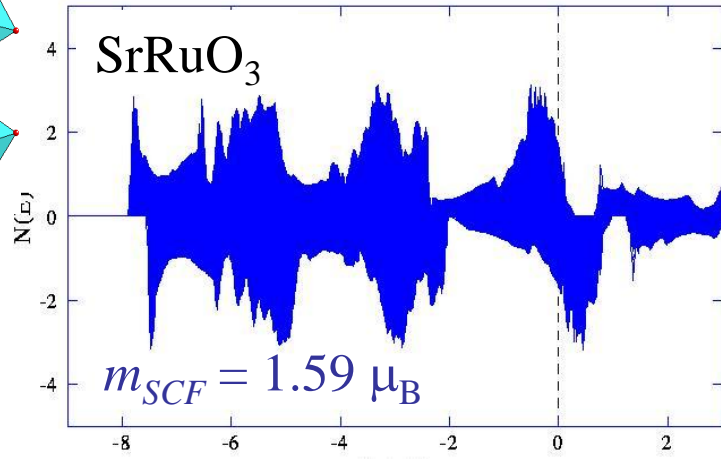
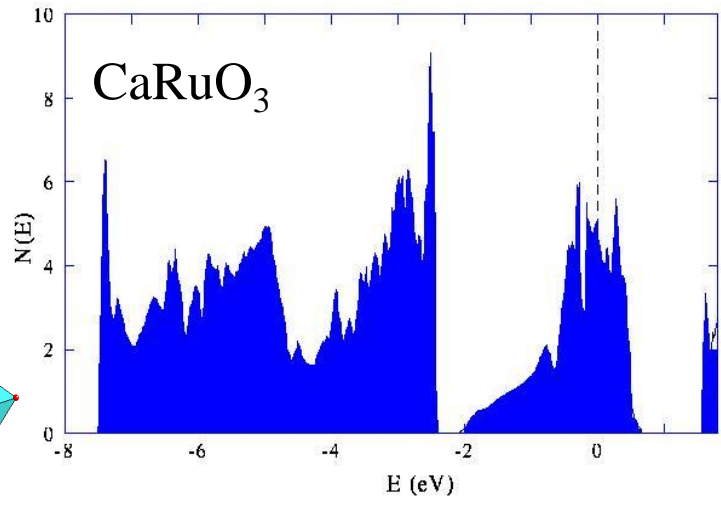
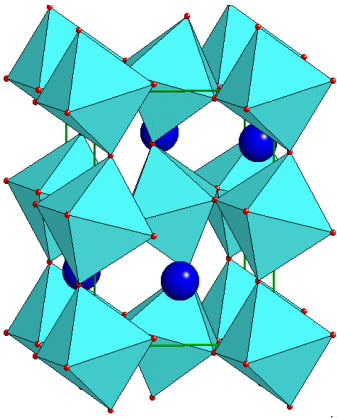
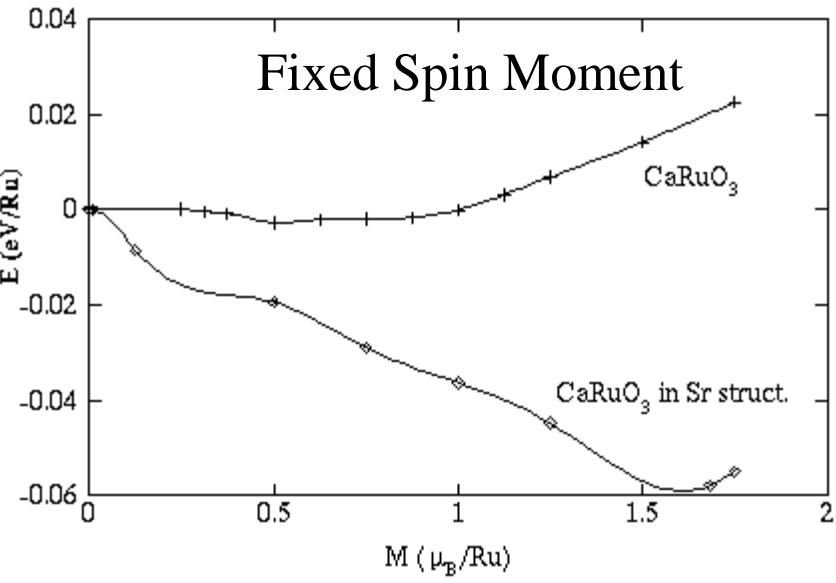
Metamagnetic  
quantum critical  
point

# Magnetic Order in $\text{Sr}_{1-x}\text{Ca}_x\text{RuO}_3$

## Experiment:

- $\text{SrRuO}_3$  is FM  $T_C \sim 165\text{K}$ .
- $T_C$  fall smoothly with  $x$ , reaching 0 near  $x=1$ .
- $\text{CaRuO}_3$  was reported AFM, but now thought PM.

## LSDA: Octahedral Tilt Broadens DOS.



*Itinerant Stoner Explanation*

# STONER PICTURE

$$\Delta E = \frac{1}{2} \int_0^m [m' dm' / N(m')] - I_{TOT} m^2 / 4$$

$$\Delta E = - I_{TOT} m^2 / 4 = - \sum_{\alpha} I_{\alpha} m_{\alpha}^2 / 4$$

$$\text{with } I_{TOT} = \sum_{\alpha} I_{\alpha} v_{\alpha}^2$$

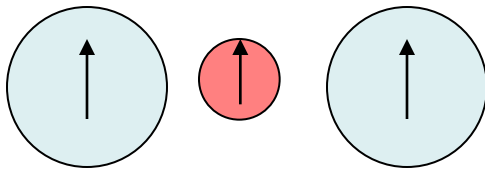
$$\text{and } N = \sum_{\alpha} N_{\alpha} v_{\alpha}$$

For SrRuO<sub>3</sub>

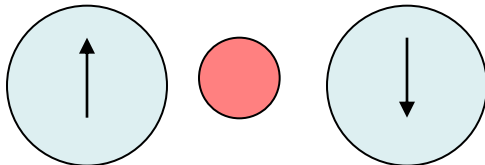
- $I_{TOT} = 0.41 \text{ eV}$

- $I_{Ru} = 0.35 \text{ eV}$

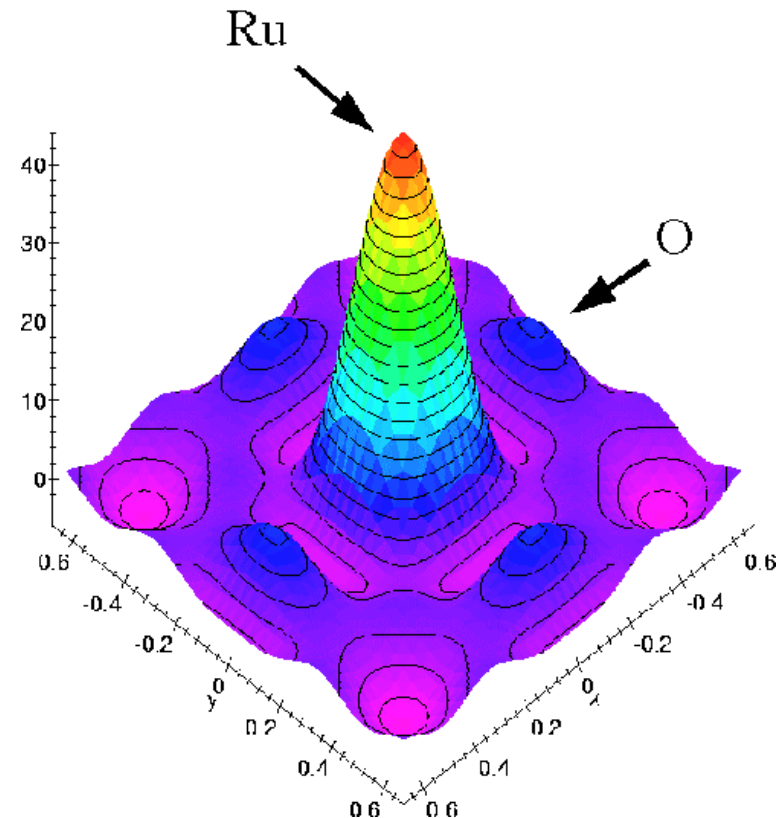
→ Significant on-site O contribution  
- Favors Ferromagnetism.



- Over Antiferromagnetism.



Also band KE.



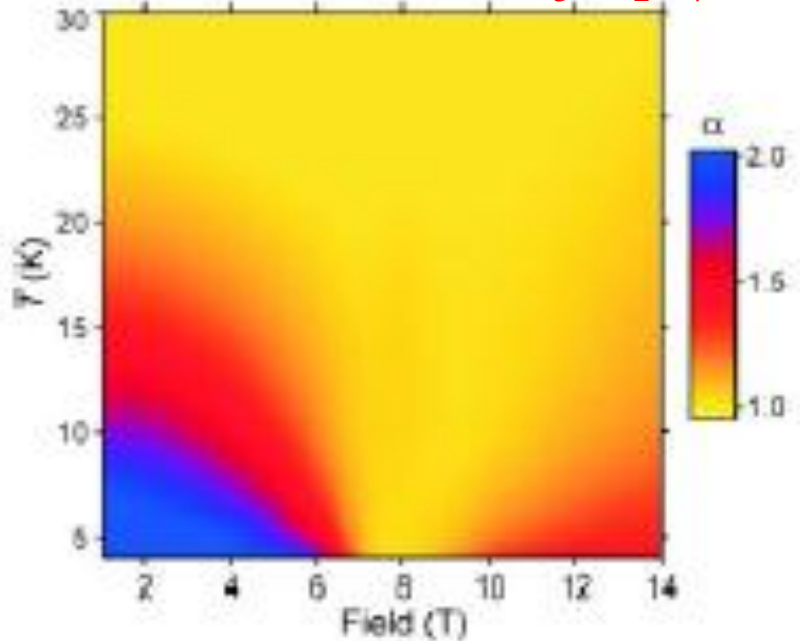
Nagler and Chakoumakos, ORNL

# Quantum Critical Points and the LDA

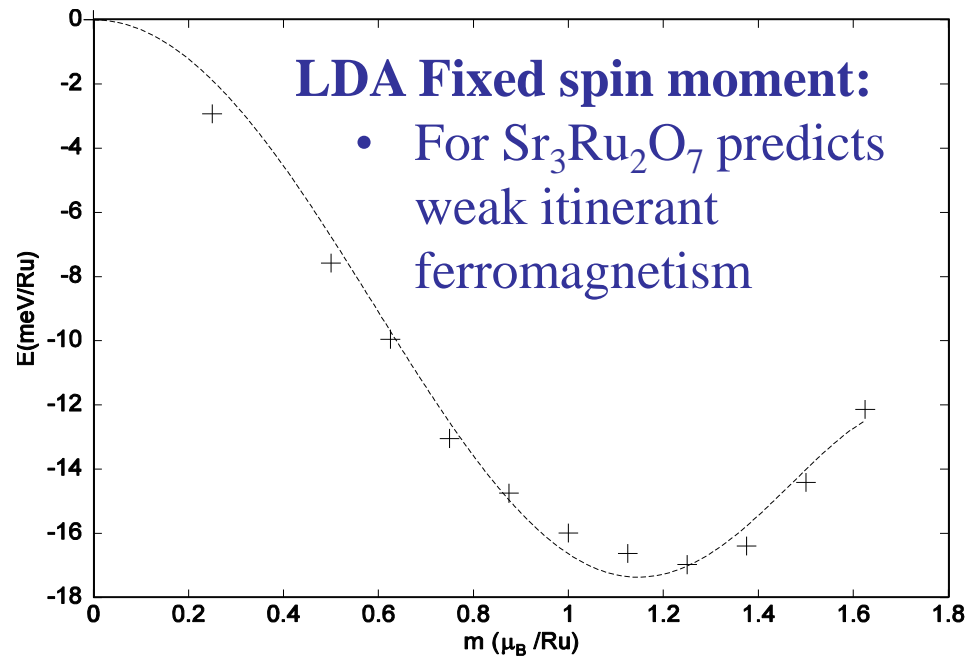
**Density Functional Theory:** LDA & GGA are widely used for first principles calculations but have problems:

- Mott-Hubbard: Well known poor treatment of on-site Coulomb correlations.
- Based on uniform electron gas. Give mean field treatment of magnetism: Fluctuations missing (generally small, but important near quantum critical points)

## Resistivity exponent in $\text{Sr}_3\text{Ru}_2\text{O}_7$



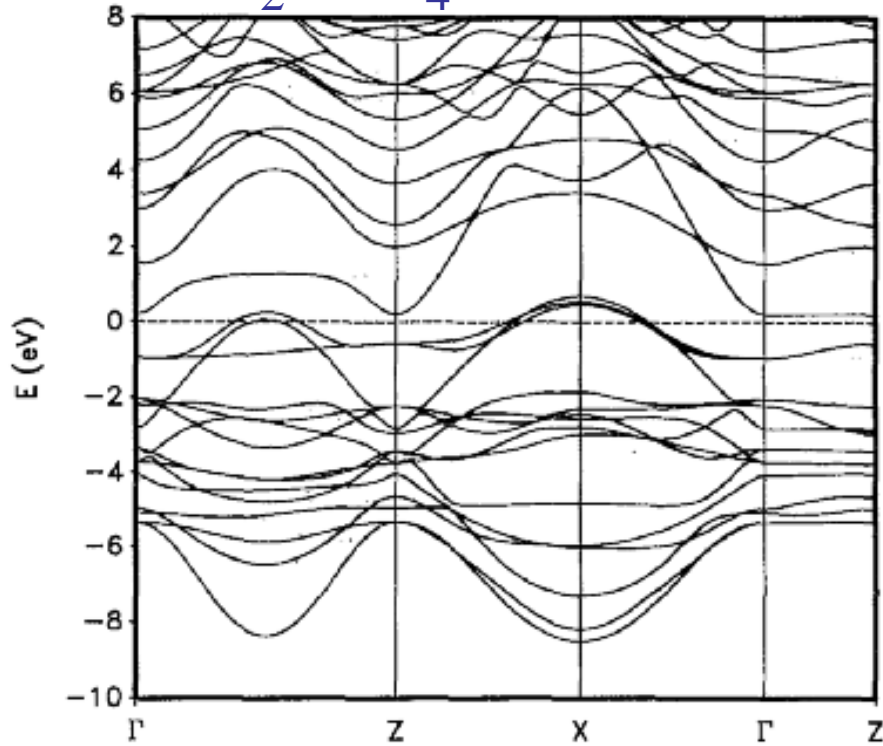
Grigera *et al.*, Science (2001).



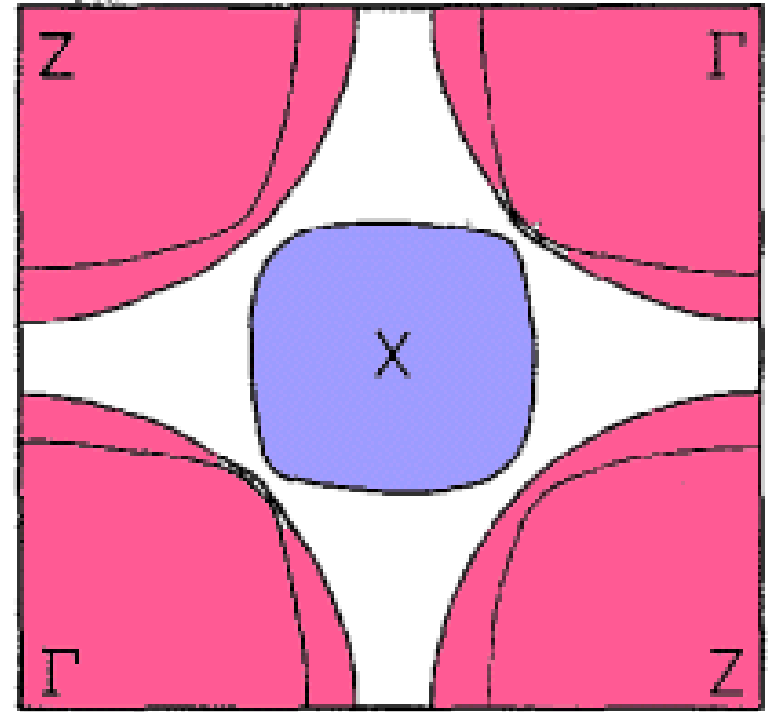
**LDA overestimate of ferromagnetic tendency is a signature of quantum critical fluctuations – neglected fluctuations suppress magnetism**

# Electronic Structure of $\text{Sr}_2\text{RuO}_4$

$\text{Sr}_2\text{RuO}_4$  -  $I4/mmm$



• 3  $t_{2g}$  derived bands at  $E_F$ :  $d_{xy}$ ,  $d_{xz}$ ,  $d_{yz}$ .



- Highly 2D electronic structure.
- FS agrees in detail with dHvA.
- Mass renormalizations  $\sim 4$

What are the pairing interactions on the FS? Unconventional symmetry  $\rightarrow$  not electron-phonon.

$\rightarrow$  Spin-fluctuations?

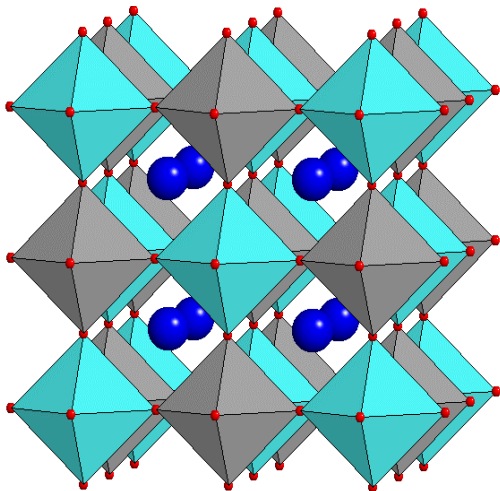
# SPIN-FLUCTUATIONS

## Ingredients:

### 1. On-Site Stoner (O) - Ru-O hybridization

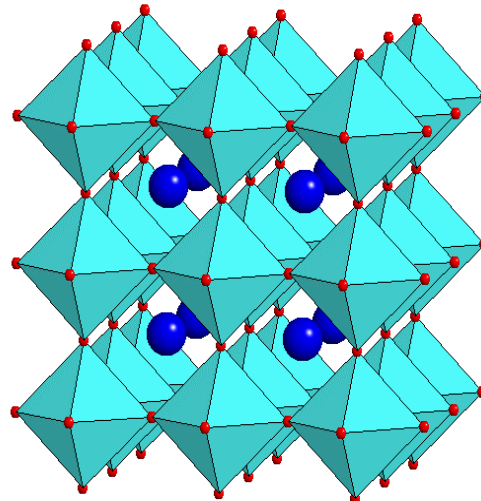
$\text{Sr}_2\text{YRuO}_6$  - no shared O

→ AFM



$\text{SrRuO}_3$  - shared O

→ FM



$\text{Sr}_2\text{RuO}_4$  - shared O

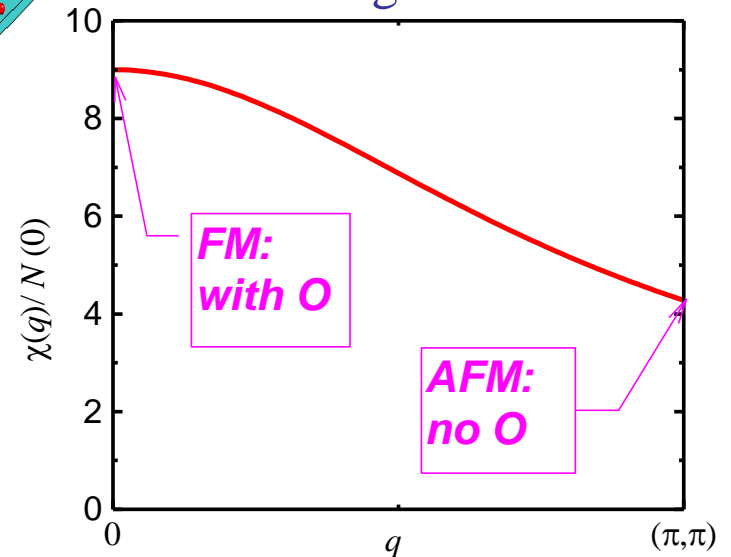
→ FM fluct.

- Shared O in  $\text{RuO}_2$  planes will favor FM fluctuations.

- Can model by smooth background using calculations of

- $I_{Ru}$  and  $I_O$ .
- Projections of  $N(E_F)$ .
- Taking full O contribution at  $\mathbf{k}=(0,0)$  and no O contribution at  $\mathbf{k}=(\frac{1}{2},\frac{1}{2})$ .

### Ferromagnetic Part



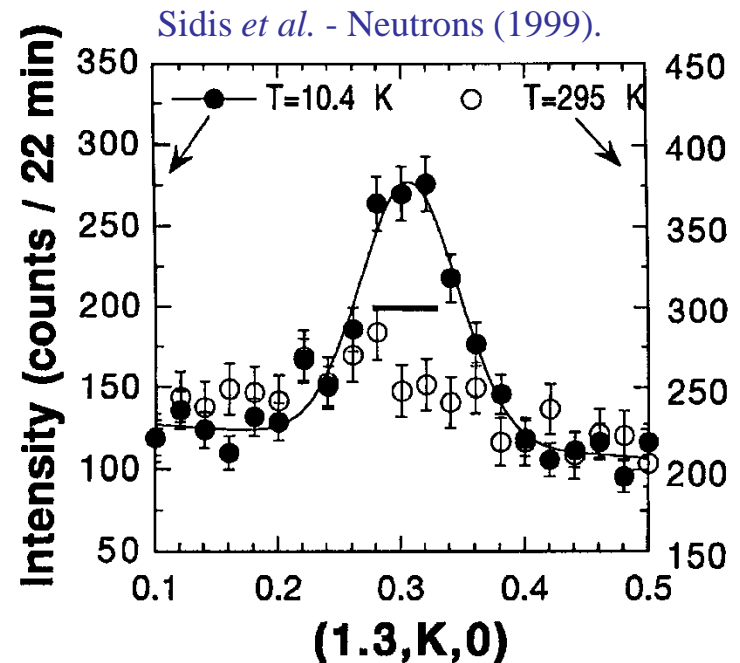
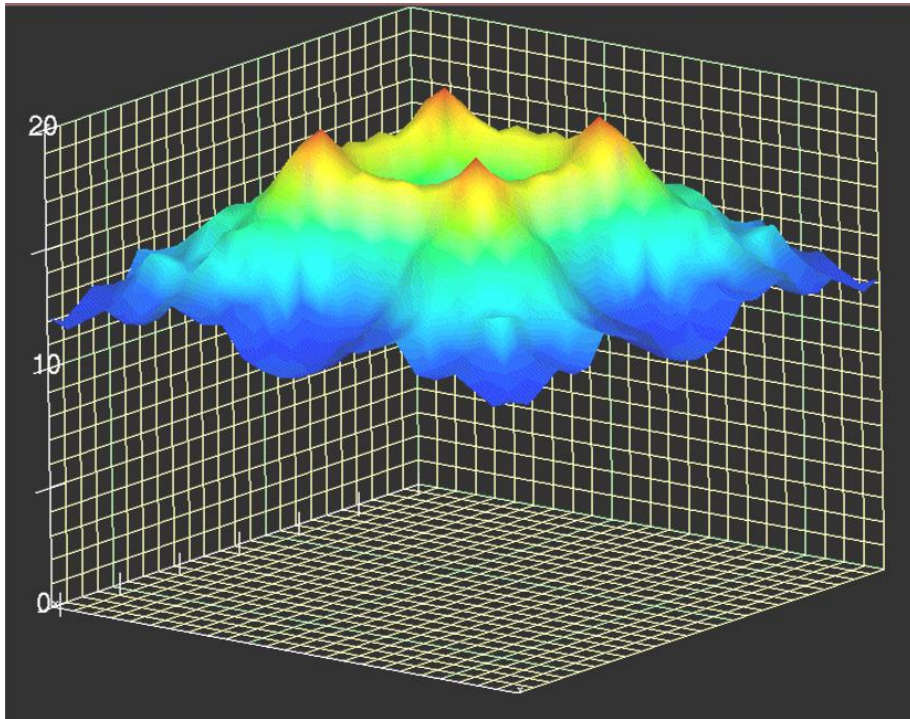
# SPIN-FLUCTUATIONS (CON'T)

## 2. Nesting:

$$\chi(\mathbf{q}) = \frac{\chi_0(\mathbf{q})}{1 - I(\mathbf{q})\chi_0(\mathbf{q})}$$

Previous slide had  $I(q)$  from Stoner but no  $\mathbf{q}$  dependence in  $\chi_0$

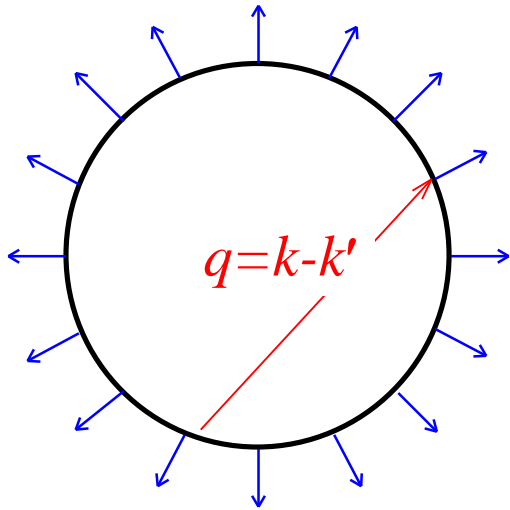
Fermi Surfaces: Simple and 2-dimensional  $\rightarrow$  strong nesting.





# SUPERCONDUCTIVITY

e.g.



Triplet works in BCS gap equation provided that the pairing at small  $\mathbf{q}$  is dominant (s.f. are attractive for triplet).

- Non- $s$  depends on  $q$  dependence in  $V(q)$ .
- Generally higher  $\ell$  needs more structure in  $V(q)$ .
- The details of the Fermi surface and  $V(q)$  are crucial.

Singlet:

$$V(\mathbf{q}) = - \frac{I^2(q)\chi_0(\mathbf{q})}{1 - I^2(\mathbf{q})\chi_0(\mathbf{q})}$$

Triplet:

$$V(\mathbf{q}) = \frac{I^2(q)\chi_0(\mathbf{q})}{1 - I^2(\mathbf{q})\chi_0(\mathbf{q})}$$

Note signs

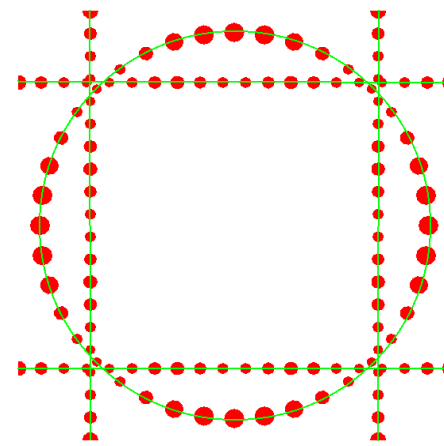
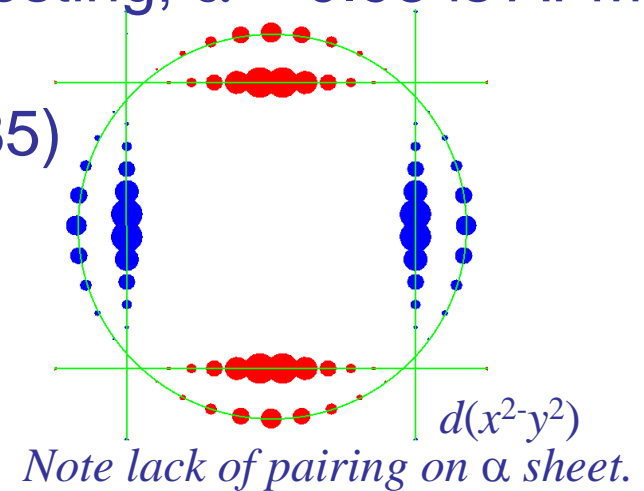
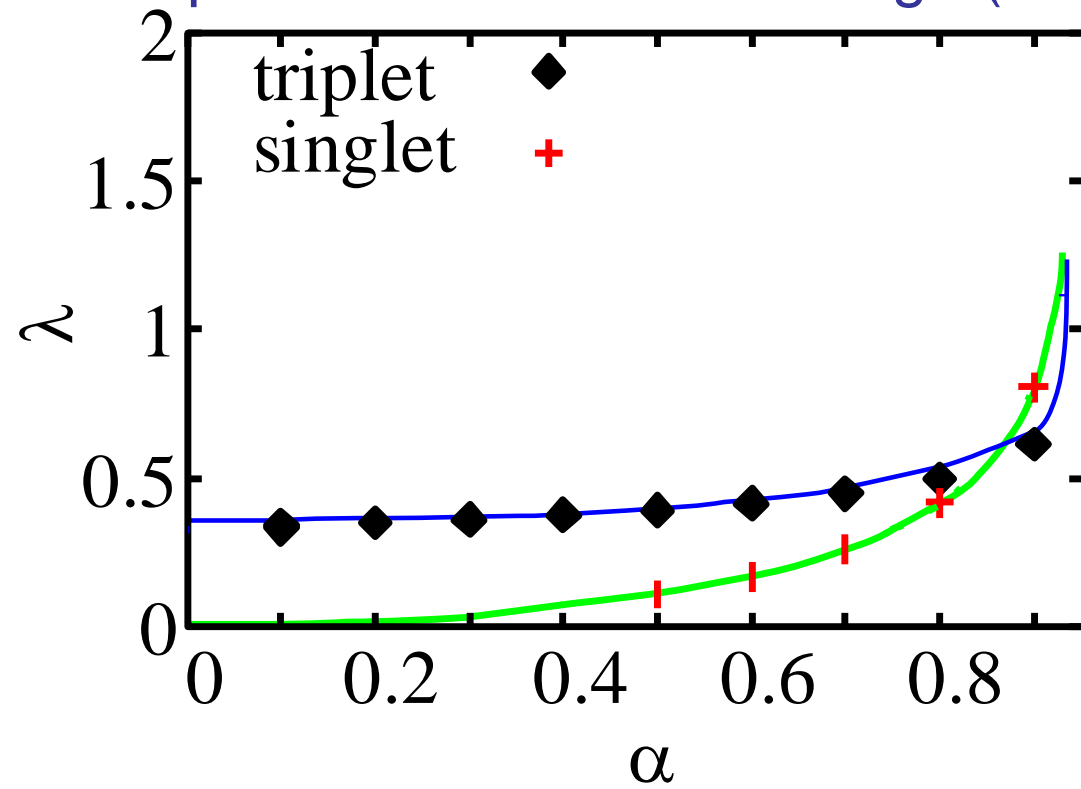
# SUPERCONDUCTIVITY (Con't)

What we did:

- Calculate matrix elements  $V_{\mathbf{k},\mathbf{k}'}$  for a set of  $\mathbf{k},\mathbf{k}'$  on the FS.
- Set-up gap equation -- diagonalize  $V$ .
- Use  $\chi_0(q) = N(0) + \alpha\chi_{\text{nesting}}(\mathbf{q})$ . -- *i.e.* FM Stoner + adjustable strength nesting --  $\alpha = 0$  means no nesting;  $\alpha = 0.98$  is AFM.

Result:

- Triplet wins over a wide range ( $\alpha < .85$ )



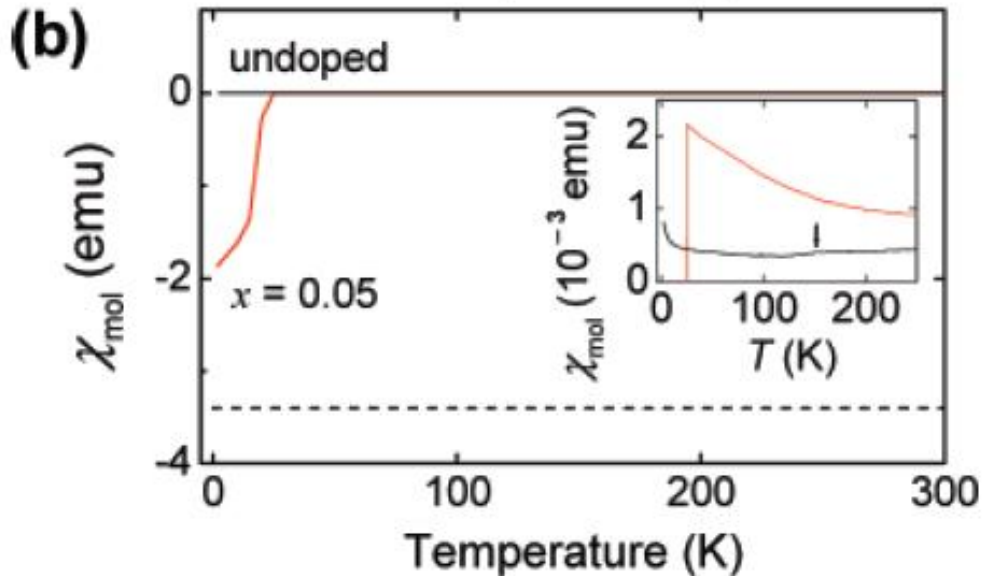
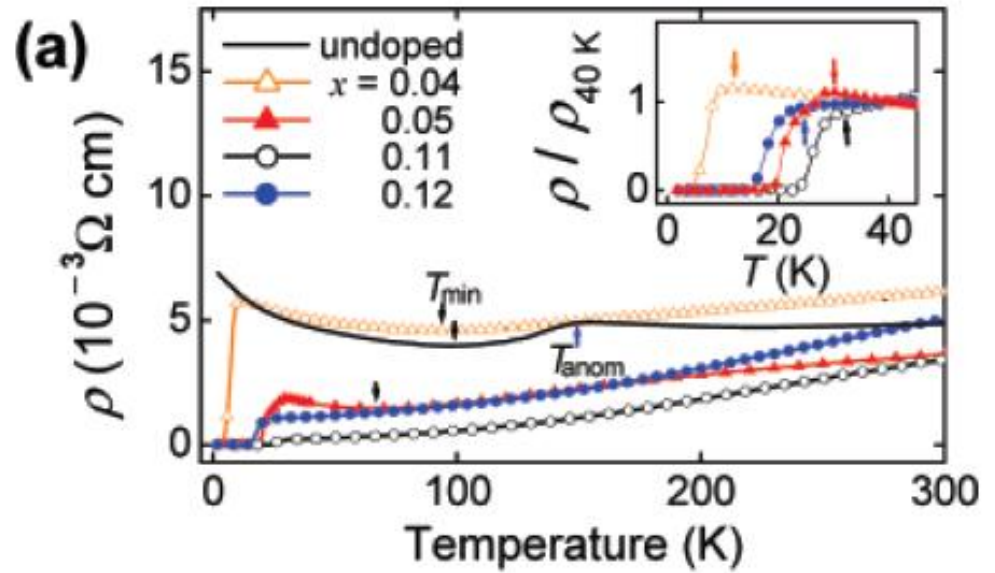
# Discovery of Superconductivity in Fe-As Compounds

Kamihara *et al.*, JACS, 2006

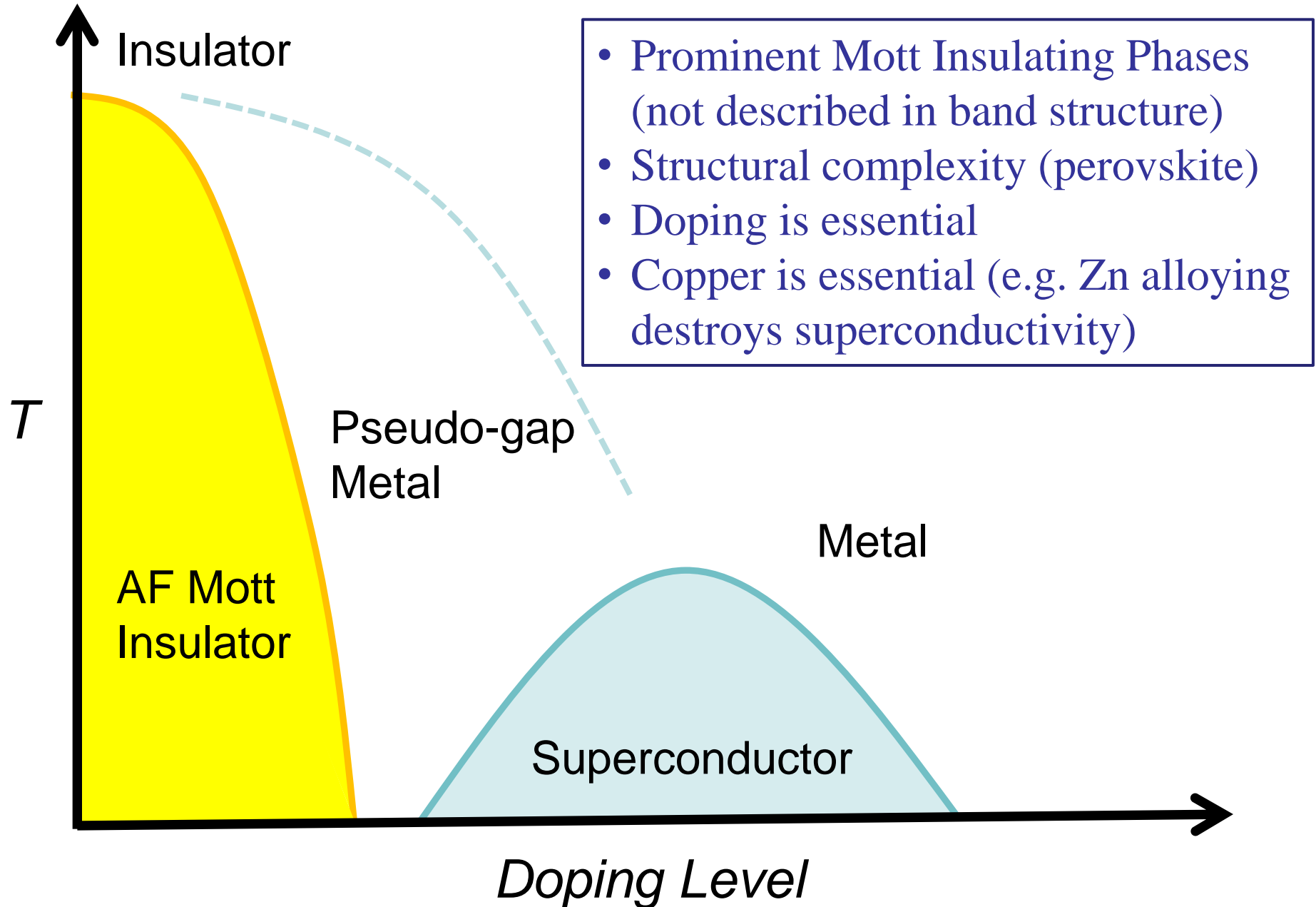
LaFePO,  $T_c \sim 4\text{K}$

Kamihara, Watanabe and Hosono, JACS, Feb. 2008

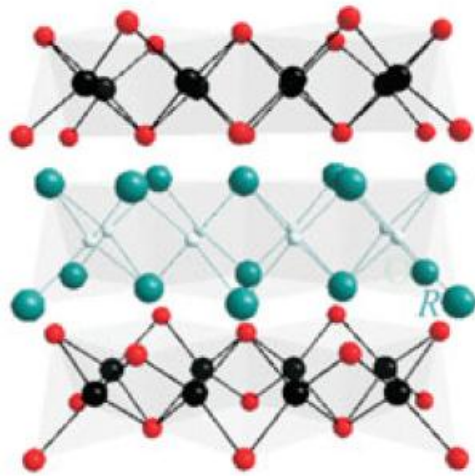
LaFeAsO<sub>1-x</sub>F<sub>x</sub>  $T_c=26\text{K}$



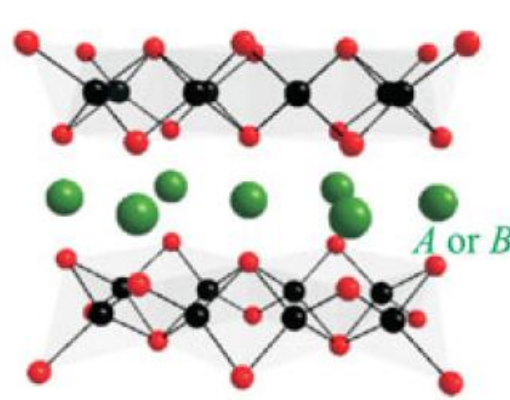
# A Brief Introduction to Cuprates



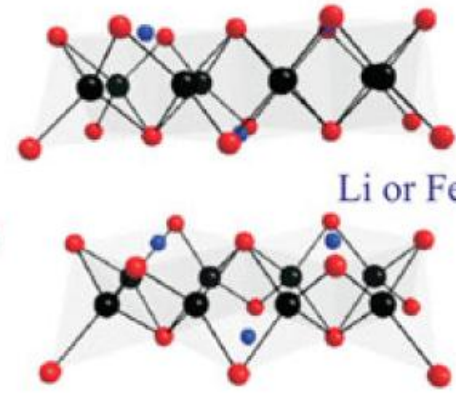
# A Big Family of High $T_c$ Superconductors



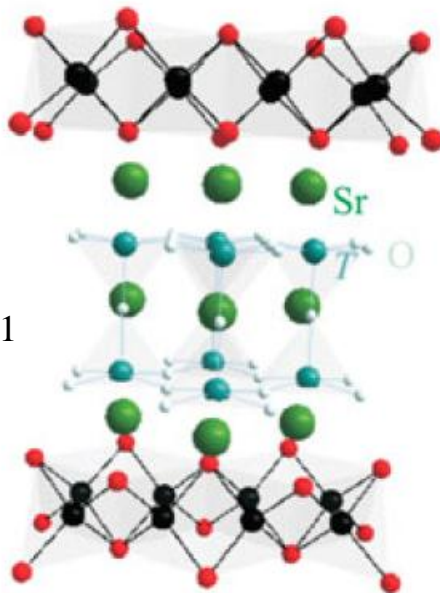
1111



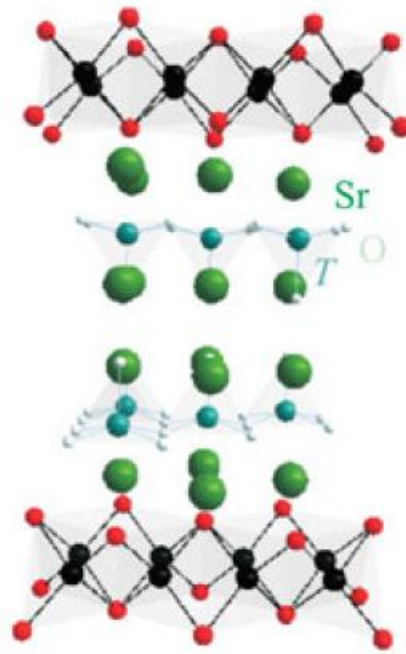
122



111, 11



32522



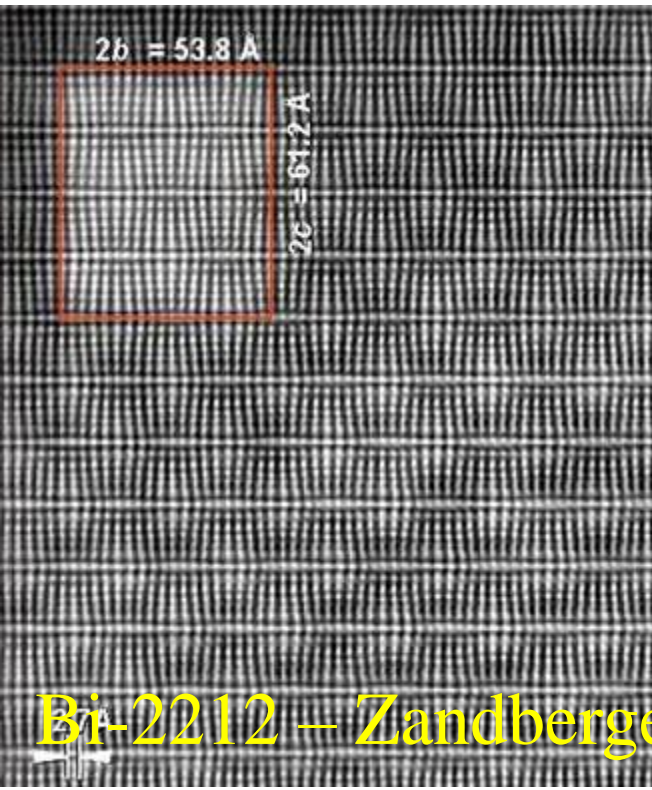
42622

## Common Features:

- High  $T_c$ .
- Near magnetism.
- Fe square lattice.
- Near divalent Fe.
- Tetrahedral coordination.

# A Word About Structure

- Large size of  $\text{As}^{3-}$ ,  $\text{Se}^{2-}$  relative to  $\text{Fe}^{2+}$  leads to tetrahedral structures with anion contact (edge shared tetrahedra). Tendency to high symmetry, small unit cells without structural distortion.
- Cuprates, etc. are based on corner shared units, with resulting tendency to complex structure distortions. The interplay with properties greatly complicates the physics.



PRL 96, 107007 (2006)

PHYSICAL REVIEW LETTERS

week ending  
17 MARCH 2006

## Experimental Proof of a Structural Origin for the Shadow Fermi Surface of $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$

A. Mans,<sup>1</sup> I. Santoso,<sup>1</sup> Y. Huang,<sup>1</sup> W. K. Siu,<sup>1</sup> S. Tavaddod,<sup>1</sup> V. Arpiainen,<sup>2</sup> M. Lindroos,<sup>2</sup> H. Berger,<sup>3</sup> V. N. Strocov,<sup>4</sup> M. Shi,<sup>4</sup> L. Patthey,<sup>4</sup> and M. S. Golden<sup>1</sup>

<sup>1</sup>*van der Waals-Zeeman Institute, University of Amsterdam, NL-1018XE Amsterdam, The Netherlands*

<sup>2</sup>*Department of Physics, Tampere University of Technology, PO Box 692, FIN-33101 Tampere, Finland*

<sup>3</sup>*Ecole Polytechnique Fédérale de Lausanne, Institut de Physique de la Matière Complexe EPFL Bt. PH CH-1015*

<sup>4</sup>*Swiss Light Source, Paul Scherrer Institute, CH-5232 Villigen, Switzerland*

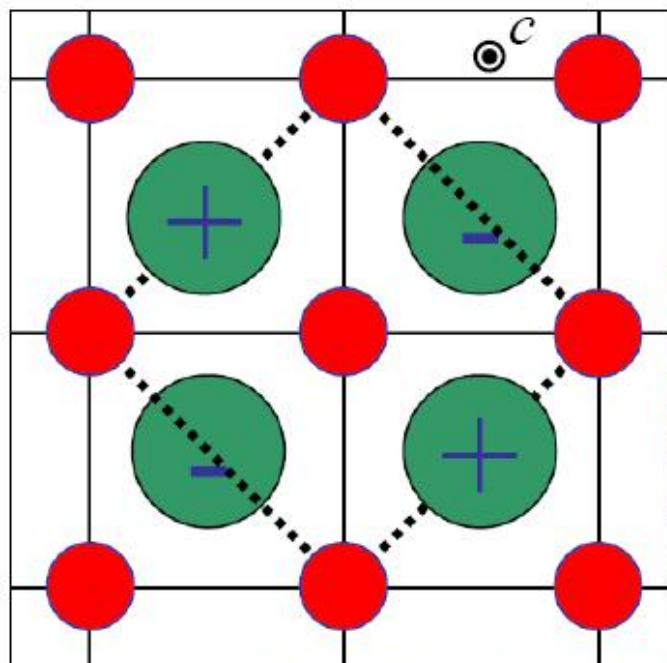
(Received 3 August 2005; published 16 March 2006)

In summary, by proving the microscopic structural origins of the shadow bands in the  $\text{Bi}2212$  and  $\text{Bi}2201$  families of cuprate superconductors, we have finally been able to close this chapter in the rich and complex tale of the high  $T_c$  superconductors.

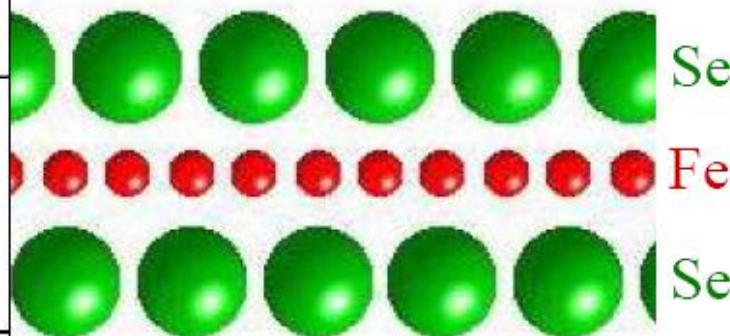
Bi-2212 – Zandbergen et al.

# FeSe - The “Simplest” Fe-Superconductor

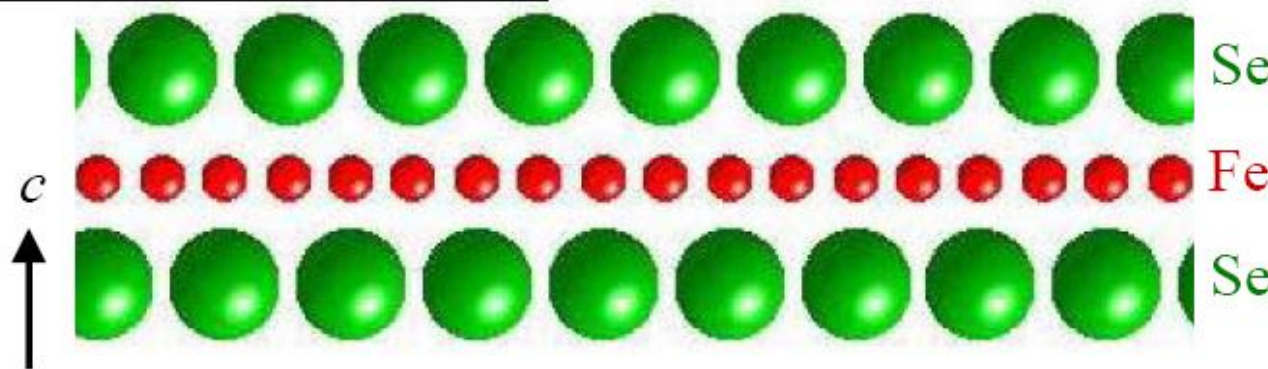
- Simple tetragonal structure, four atoms per unit cell (Hagg and Kindstrom, Z. Phys. Chem. (1933)).



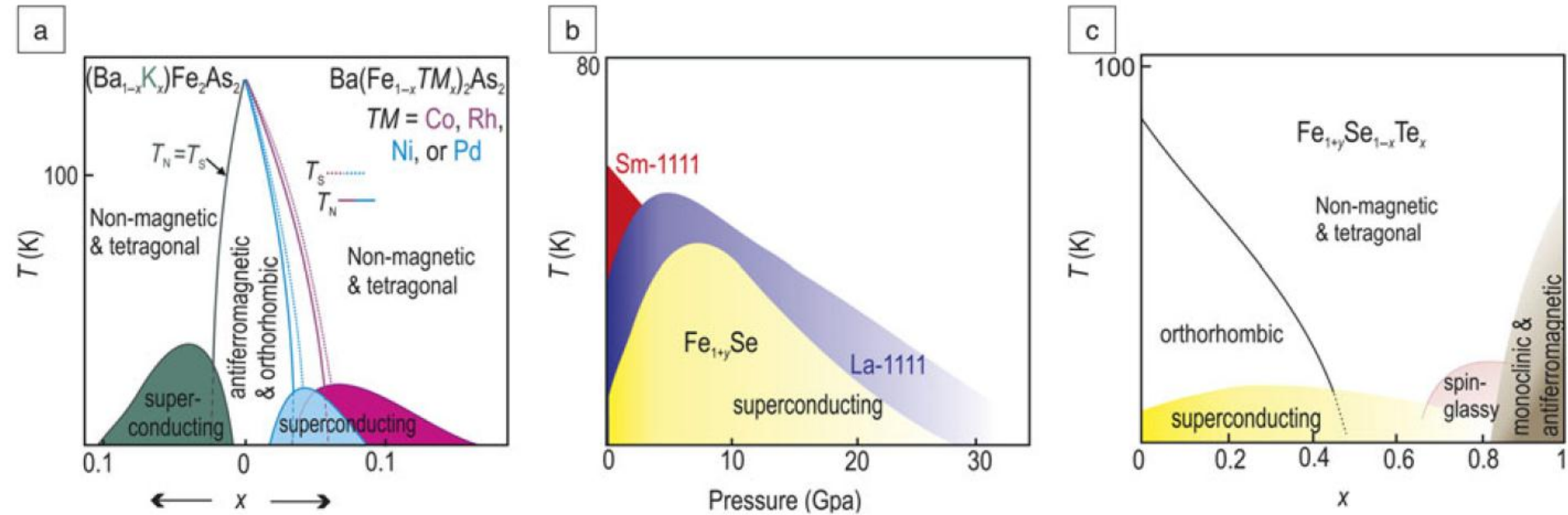
- Actual material is  $\text{Fe}_{1+x}\text{Se}$ , with extra Fe in holes of Se lattice.
- $\text{LiFeAs}$  is similar, but extra sites are filled with Li.



$$d_{\text{Fe-Fe}} = 2.66 \text{ \AA}$$



# Some Phase Diagrams



Sefat *et al.*, MRS Bull. **36**, 216 (2011)

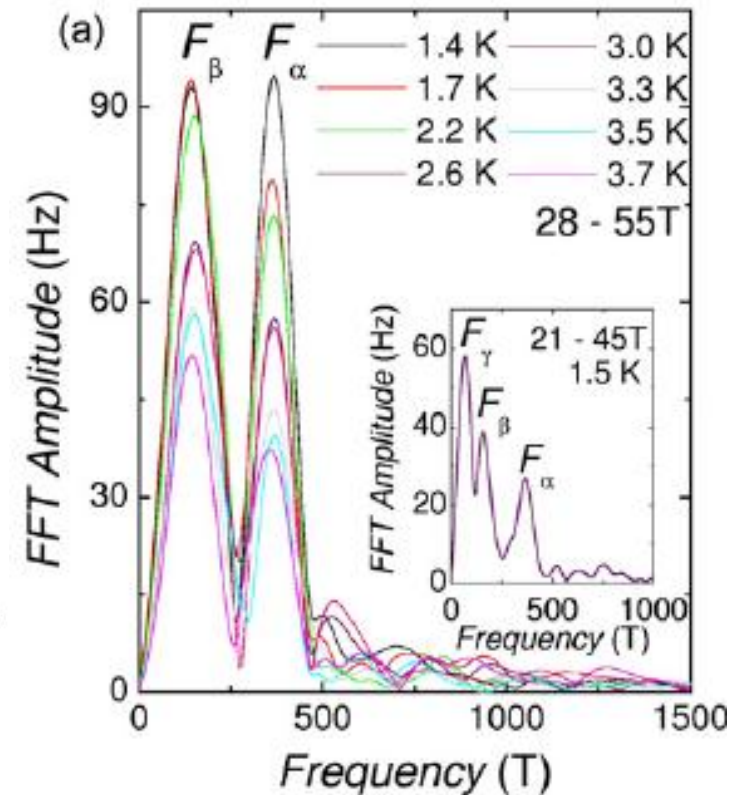
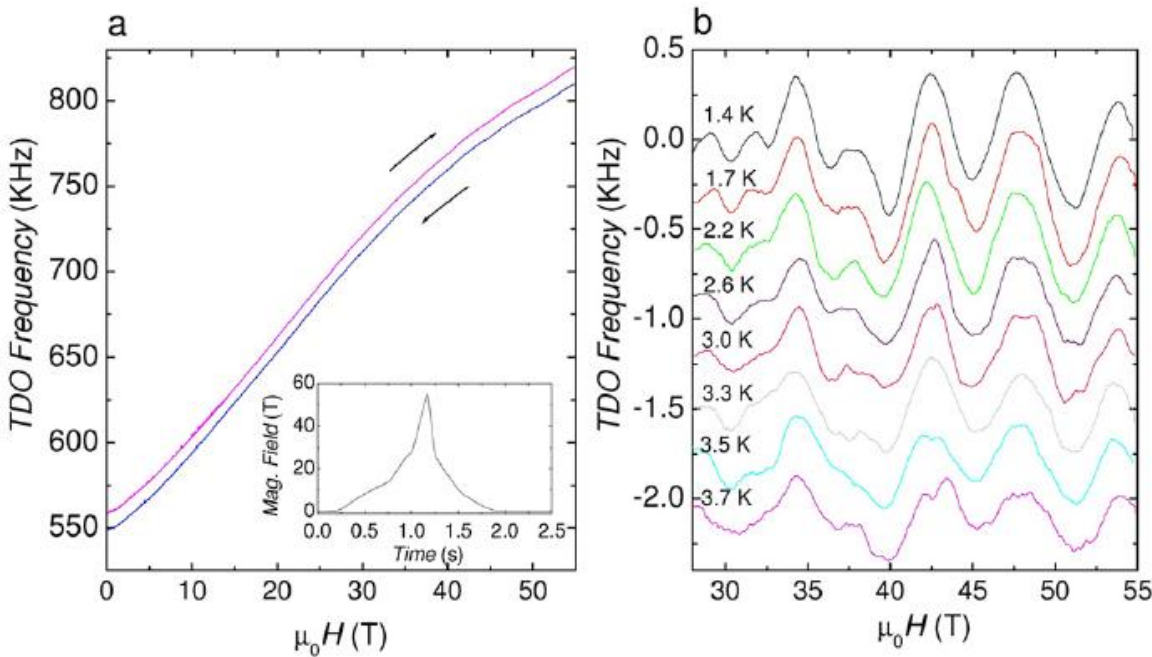
## Not List:

- Doping is not essential.
- Not in proximity to Mott phases.
- Magnetic order & superconductivity not incompatible (compete).
- Orthorhombicity occurs without magnetic order, but not always, and highest  $T_c$  is tetragonal (but large orthorhombic regions).
- Maximum  $T_c$  in different families is not so different (factor of  $\sim 2$ ).



# Metallic Antiferromagnetic State

SrFe<sub>2</sub>As<sub>2</sub> (Sebastian *et al.*)

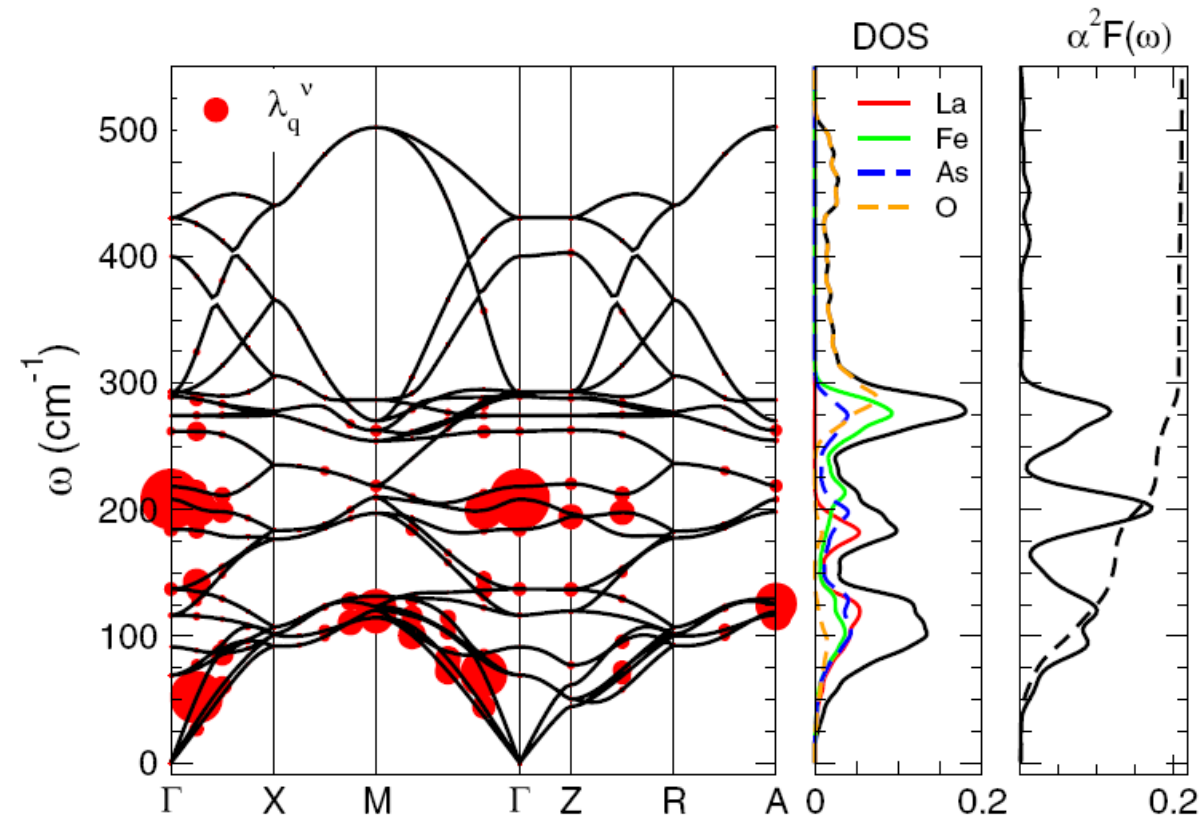


Shubnikov – de Hass measured by tunnel diode method.

SDW state has quantum oscillations reflecting a Fermi surface and is therefore a metal.

# Phonons and Electron-Phonon Interaction

- First principles calculations allow direct calculation of pairing interaction, and almost first principles calculation of  $T_c$ .
- Calculations show weak coupling, no superconductivity ( $\lambda_{ep} \sim 0.2$ ).



- Fe/As phonons are below  $300 \text{ cm}^{-1}$ .
- Corresponding Ni compounds,  $\text{LaNiPO}$ ,  $\text{LaNiAsO}$ ,  $\text{BaNi}_2\text{As}_2$  ... are electron-phonon superconductors!
- Fe compounds are not electron-phonon superconductors.

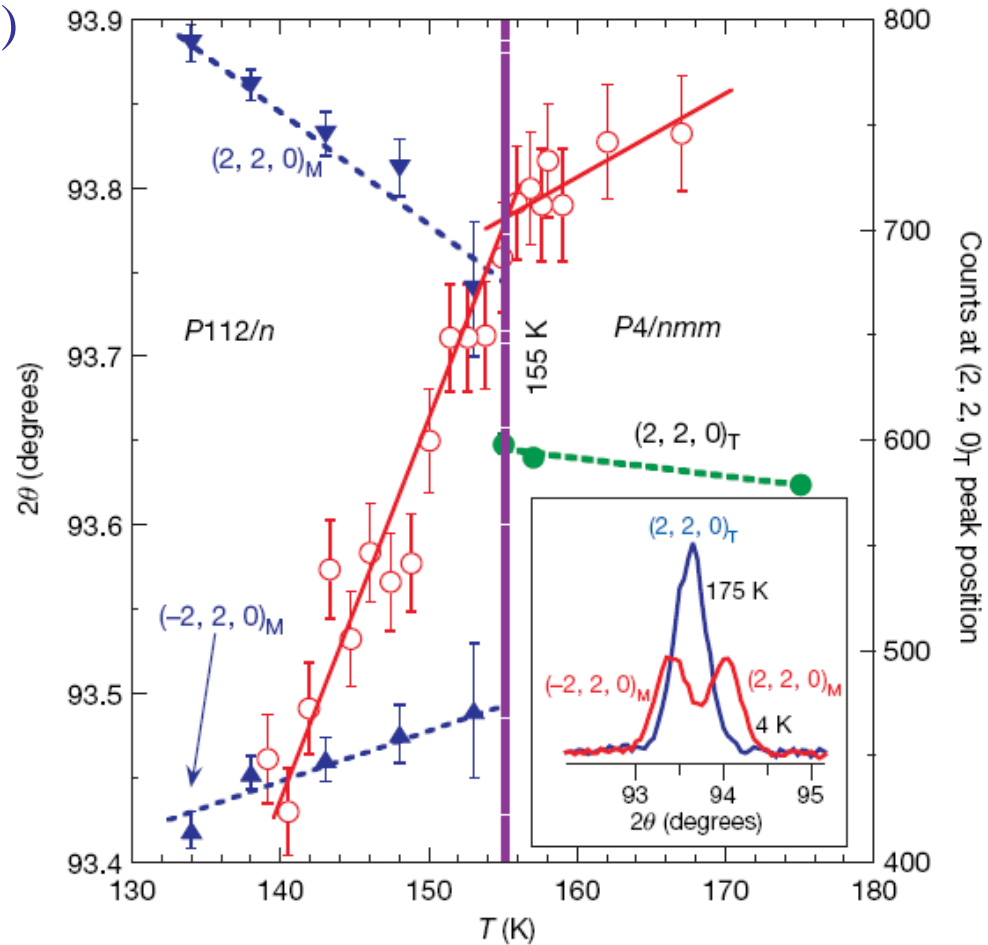
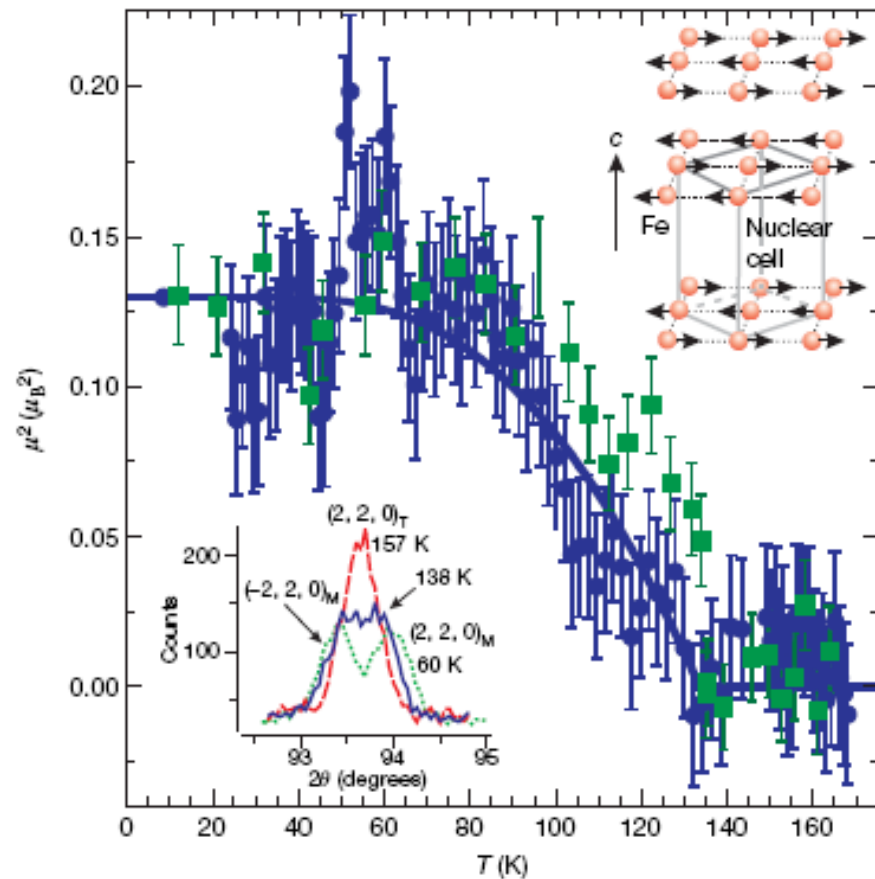
# Neutron Scattering – Magnetism & Structure

## LaFeAsO:

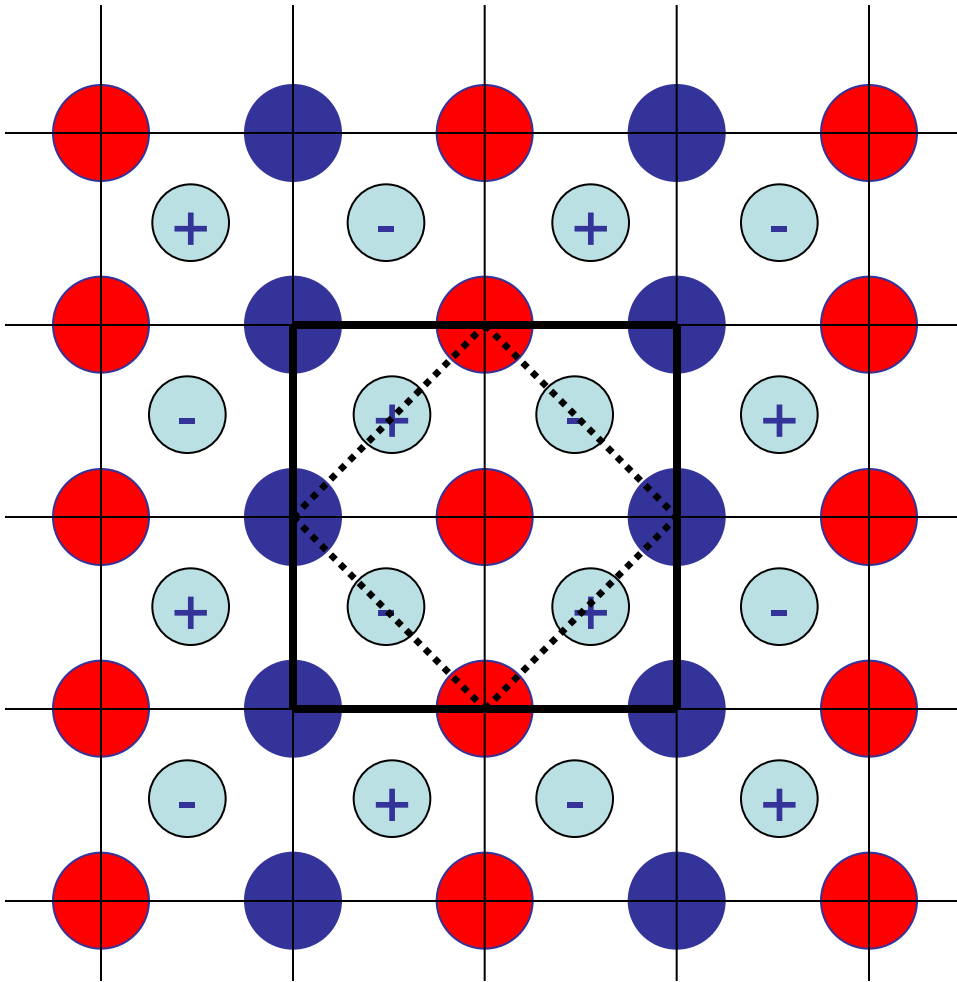
Ordered  $m(\text{Fe}) = 0.36 \mu_B$

(other compounds so far are between 0.3 and  $1 \mu_B$ )

C. de la Cruz et al., Nature **453**, 899 (2008)



# In-plane SDW structure



1 D Chains of parallel spin Fe atoms.

# Hund's Coupling

- Hund's coupling in 3d ions is strong (Stoner  $I \sim 0.8$  eV)
- Spin-fluctuations are then expected to couple to electronic states in the  $d$ -band going up to high energy (i.e. the  $d$ -band width) – may be observable in spectroscopy. Drude weight seems reduced in optics.

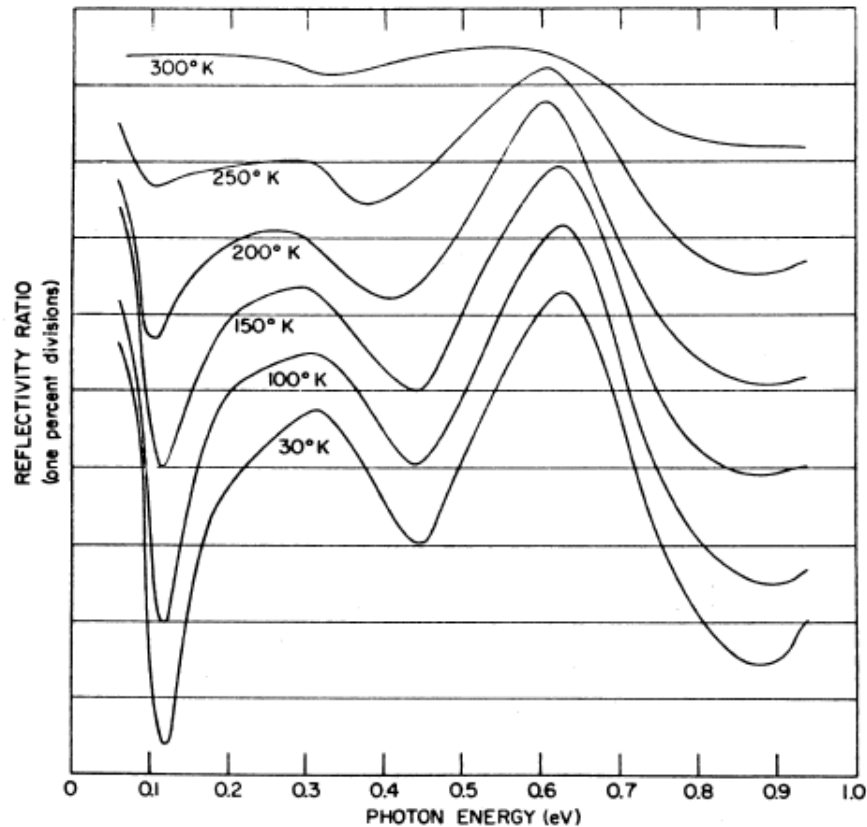
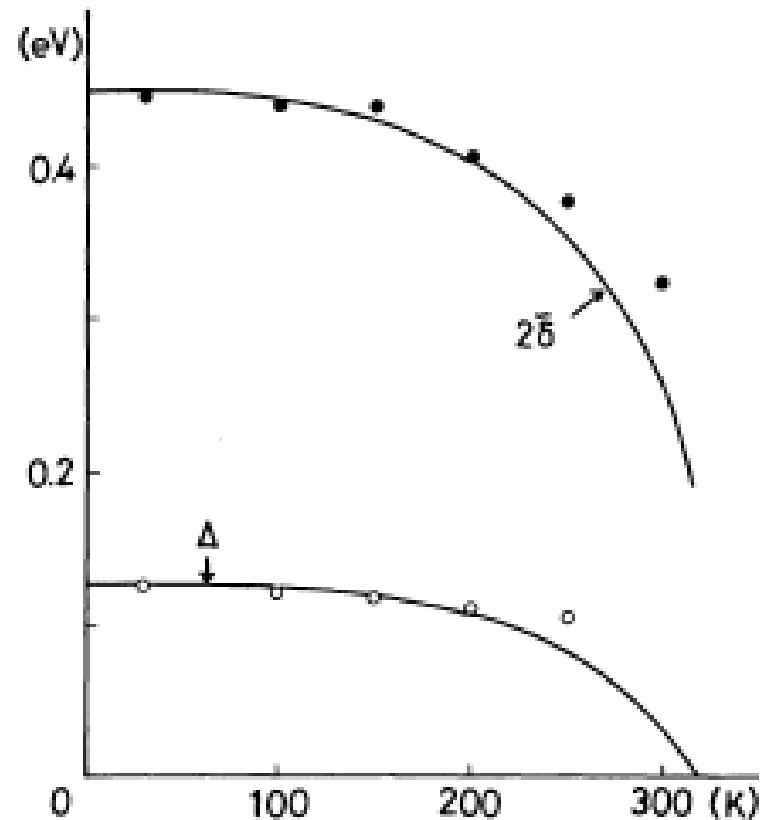


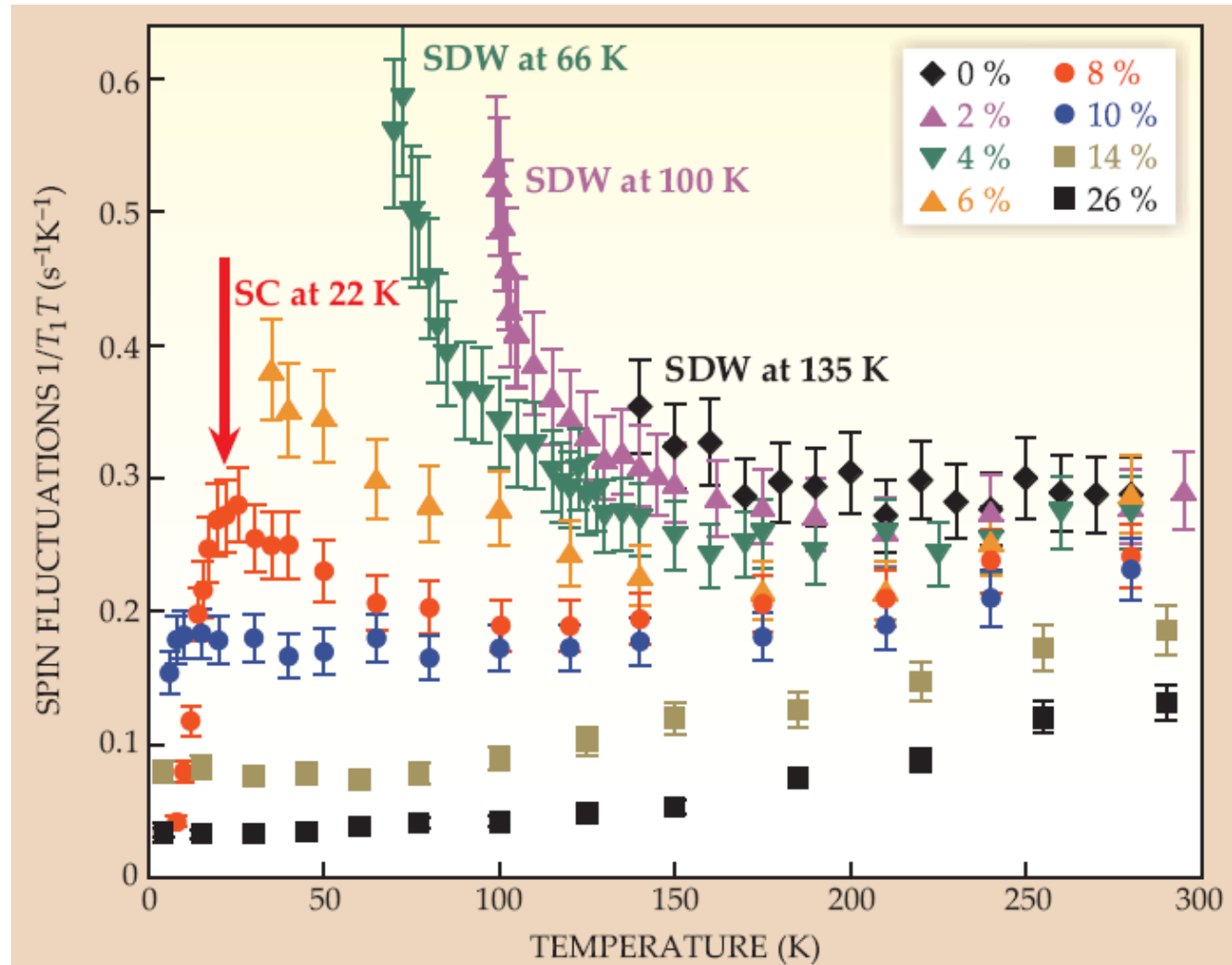
Fig. 3. The temperature dependent reflectivity of chromium normalized to  $T=400$  K.

Cr metal: Machida et al., JPSJ (1984).



# NMR: Connection of SDW and SC States

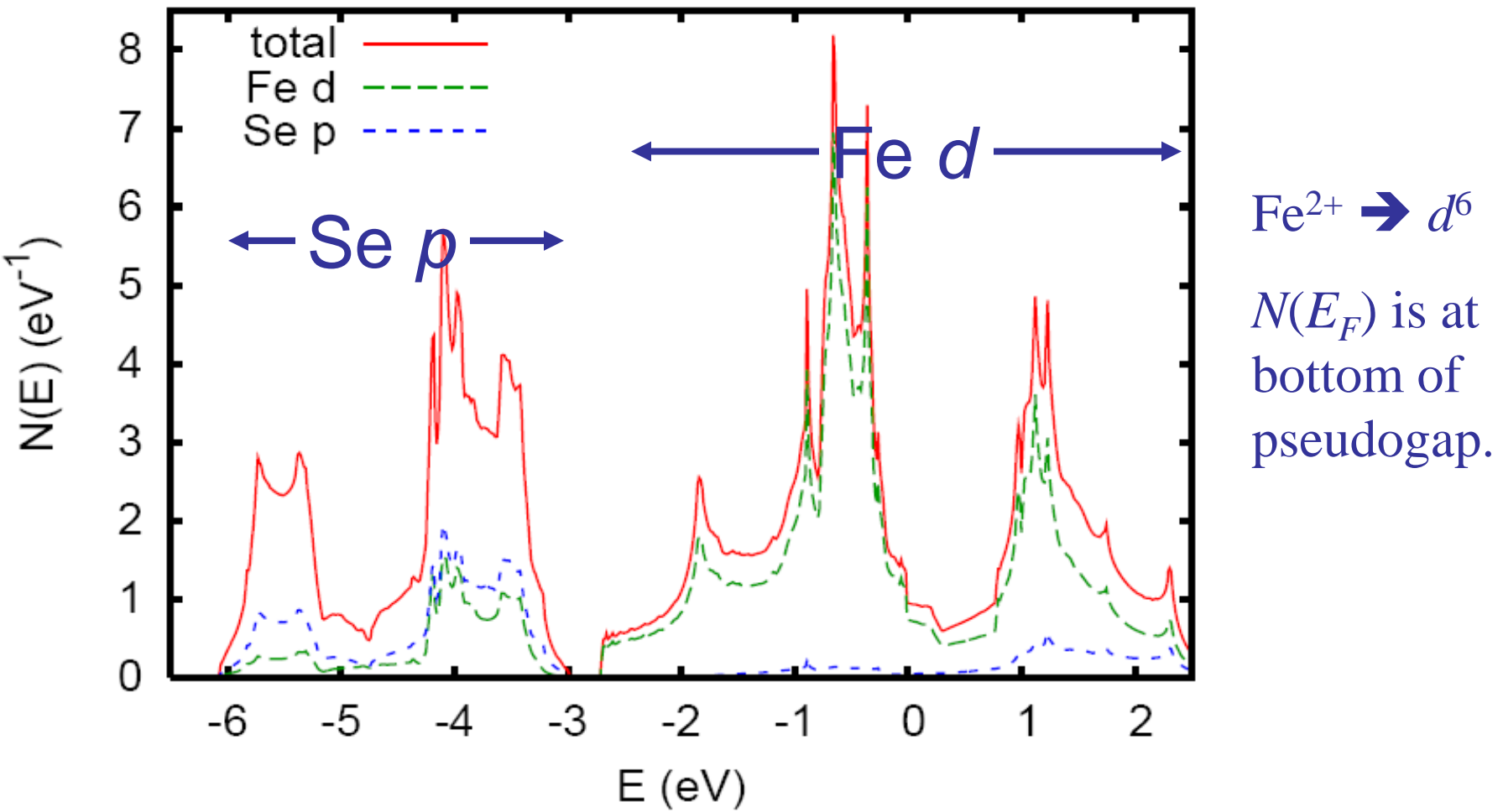
$1/T_1T$  shows strong spin fluctuations (constant for ordinary F.L.)



Ning, et al., JPSJ 78, 013711 (2009).

# LDA Electronic Structure of FeSe

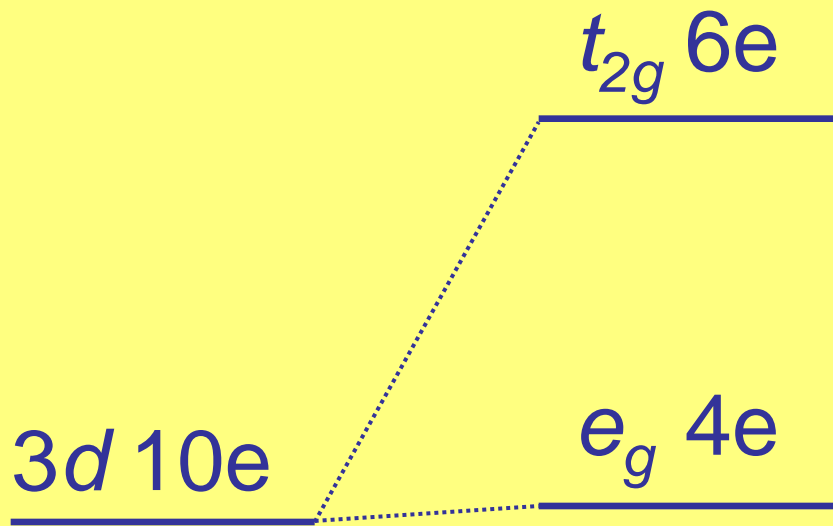
- A rather ionic material –  $\text{Fe}^{2+}$  and  $\text{Se}^{2-}$  with some hybridization, as in an oxide  $\rightarrow$  metallic sheets of  $\text{Fe}^{2+}$  modified by interaction of anions.
- Pauling electronegativities: Fe = 1.83; Se = 2.55; As = 2.18.



# Formation of Band Structure

- Bands from -2 eV to +2 eV are derived from  $\text{Fe}^{2+}$   $d$ -states.
- $\text{Fe}^{2+}$  has 6  $d$ -electrons.

## *Tetrahedral Crystal Field Scheme:*



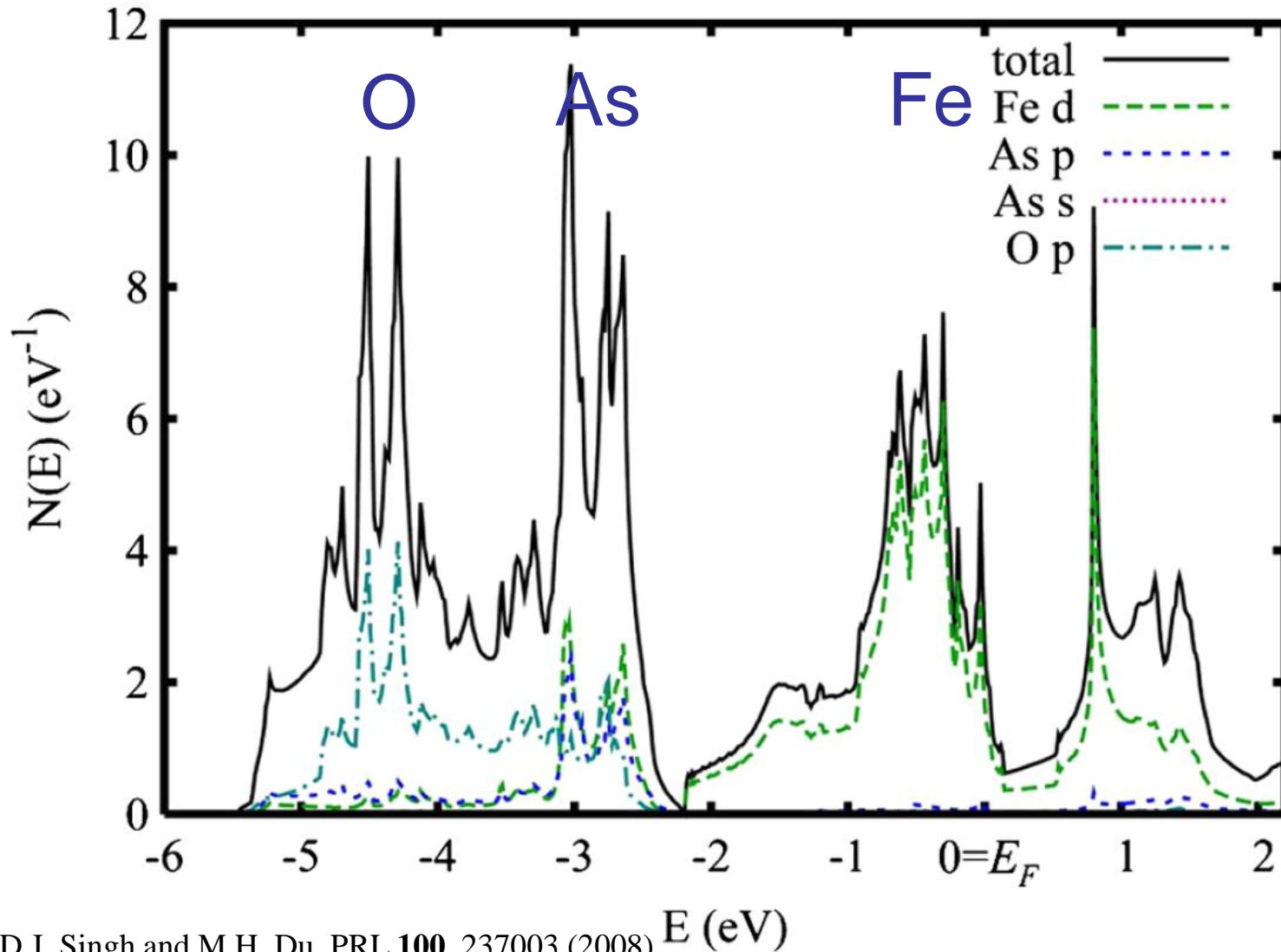
*Does not correspond to the calculated electronic structure.*

*Key is the short Fe-Fe bond length → direct Fe-Fe interactions.*



# Arsenide Electronic Structure: LaFeAsO

- LaFeAsO: Rather ionic electronic structure:  $O^{2-}$ ,  $As^{3-}$ ,  $La^{3+}$
- Bands near  $E_F$  are derived from Fe with little As admixture



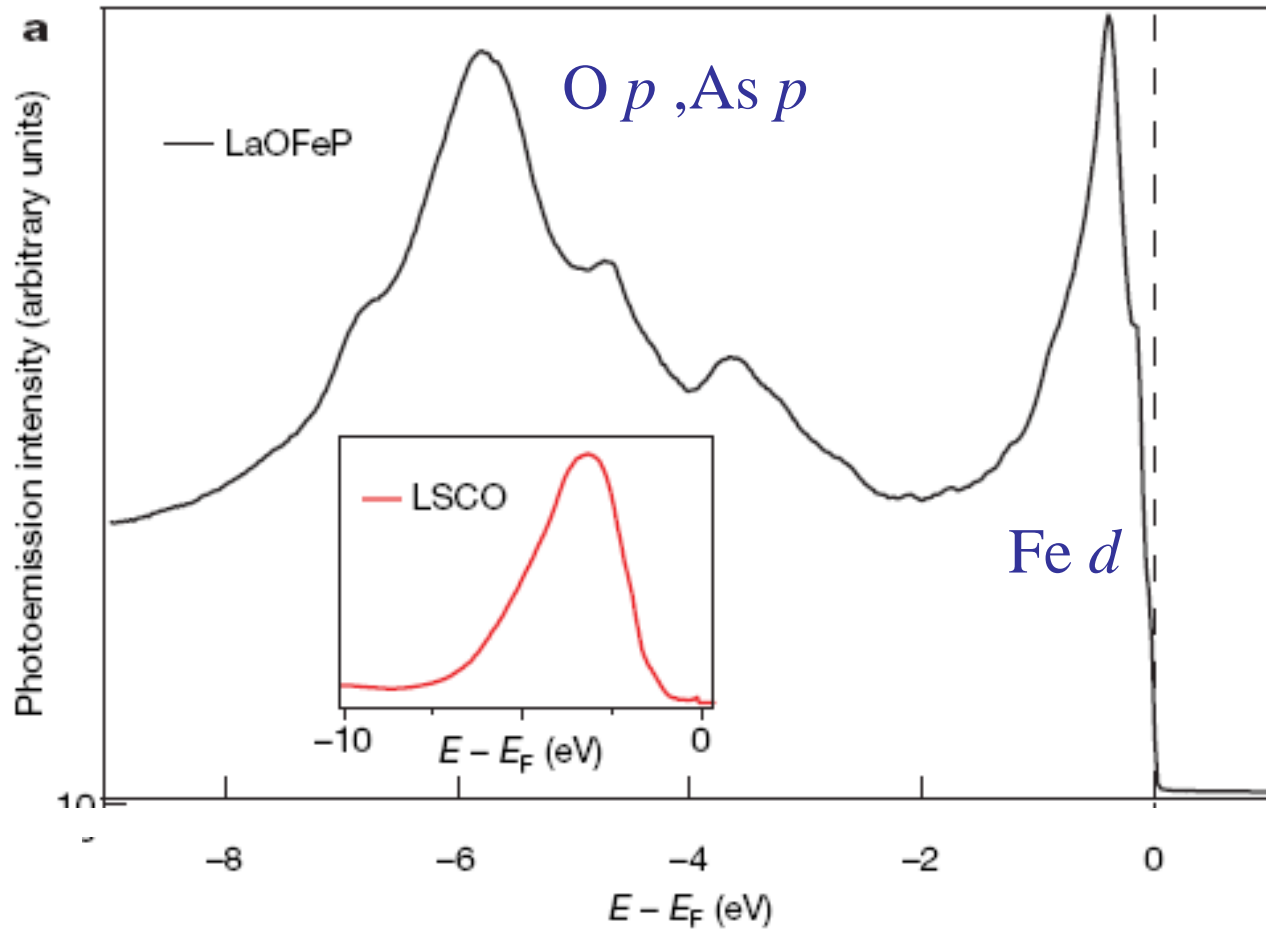
Metallic sheets of  $Fe^{2+}$

$E_F$  is at the bottom edge of a pseudogap

High  $N(E_F)$  → near magnetism

# Metallic Character

Photoemission: LaFePO (D.H. Lu et al.)

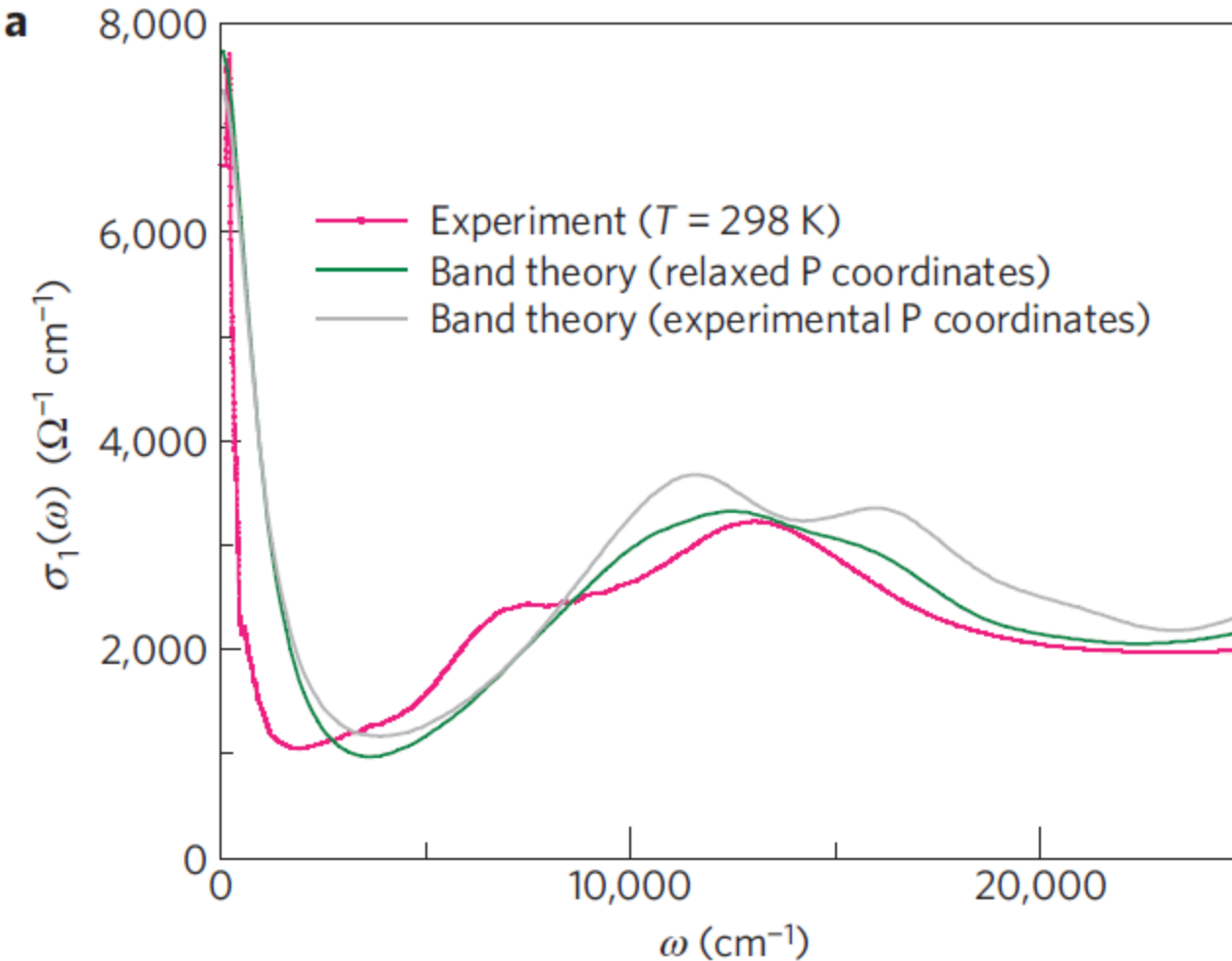


Very prominent  
Fermi edge (not  
like cuprates).

Fe d bands are  
narrower (by  $\sim 2$ )  
compared to LDA.

# Optics

LaFePO (M.M. Qazilbash et al.)



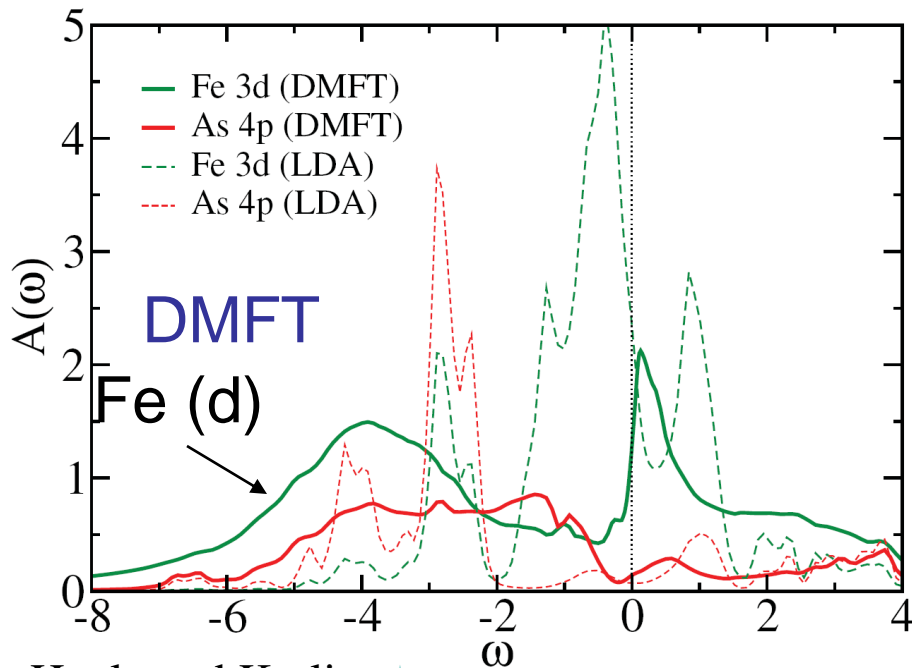
Drude has lower weight than in band calculation.

Re-distribution of spectral weight in d-bands.

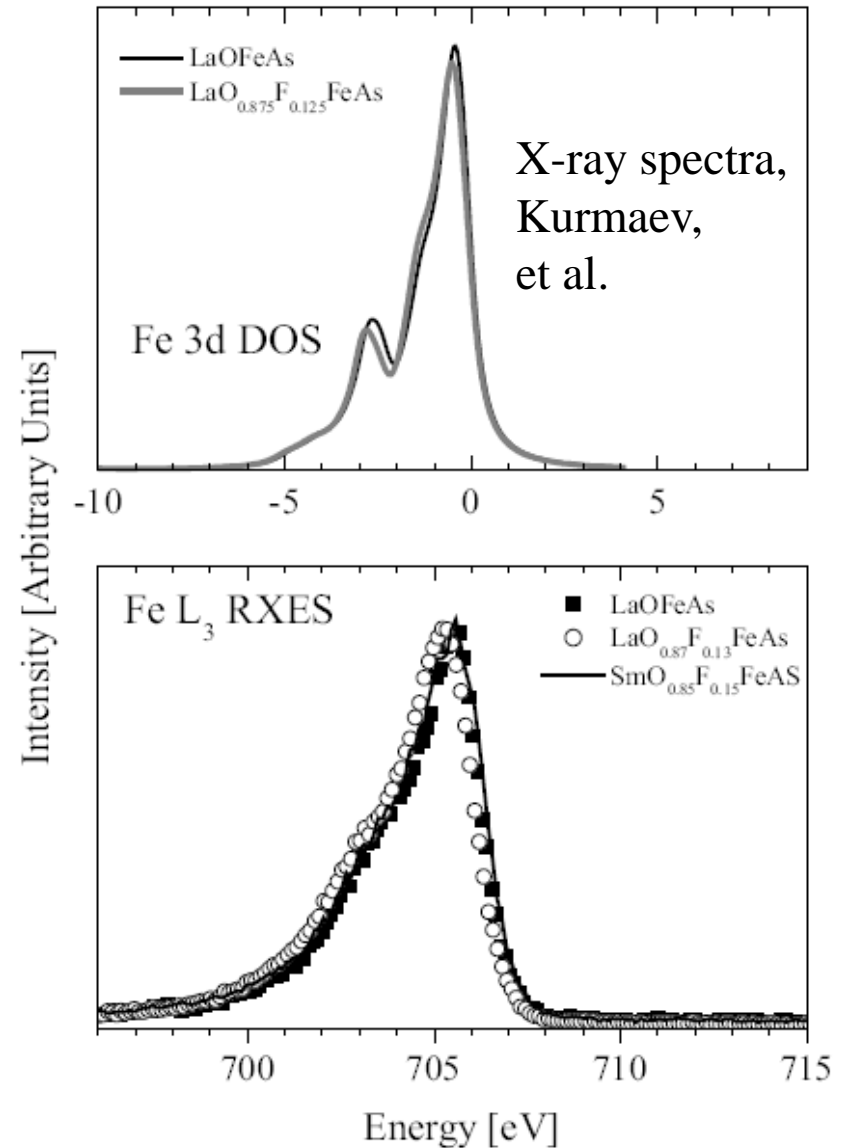
No Hubbard bands.

# Coulomb Correlations

- LDA and correlated approaches give different predictions.
- So far Hubbard bands are not seen; strong Fe d character is seen at Fermi edge.
- There is however a renormalization of  $\sim 2$  in band width c.f. LDA.



Haule and Kotliar

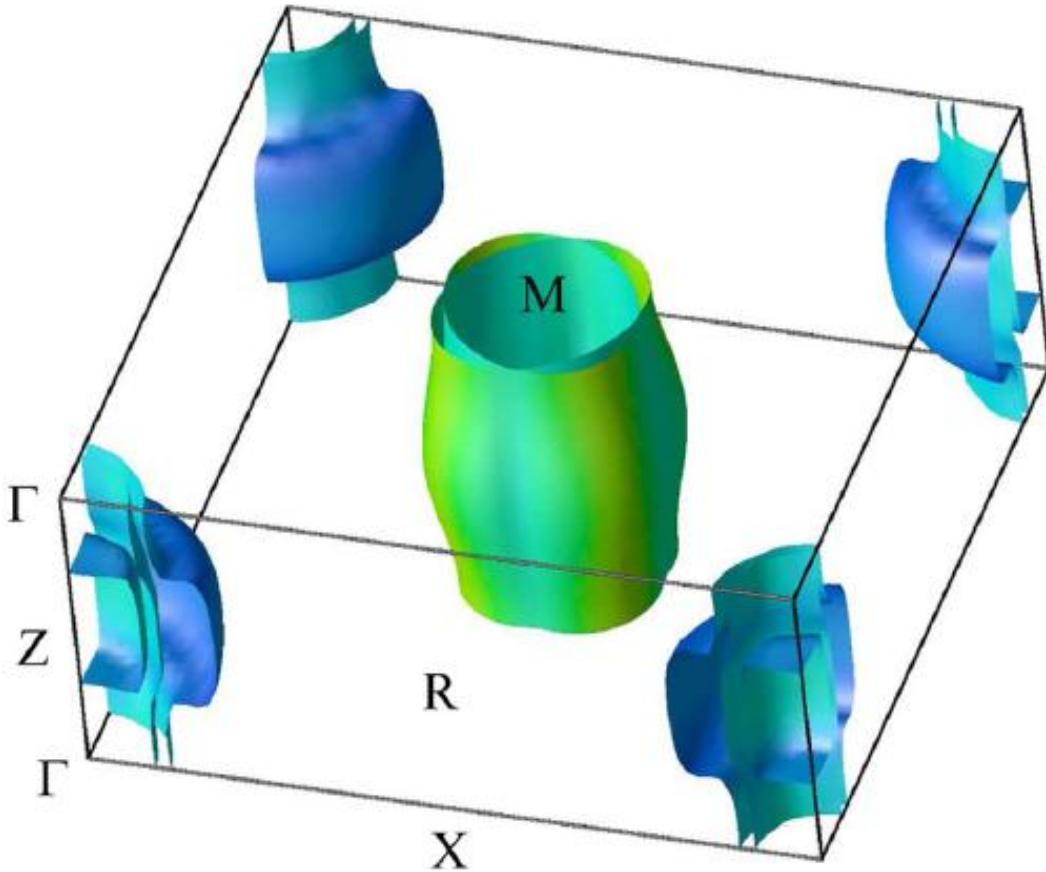


## Density Functional Study of $\text{LaFeAsO}_{1-x}\text{F}_x$ : A Low Carrier Density Superconductor Near Itinerant Magnetism

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*Materials Science and Technology Division, Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831-6114, USA*

(Received 4 March 2008; published 12 June 2008)



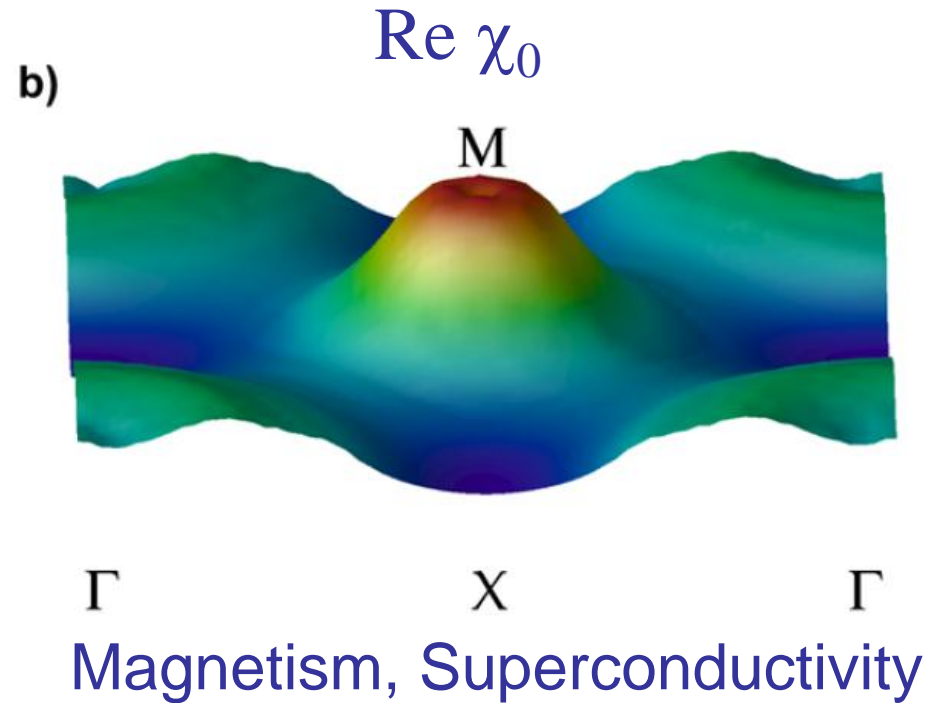
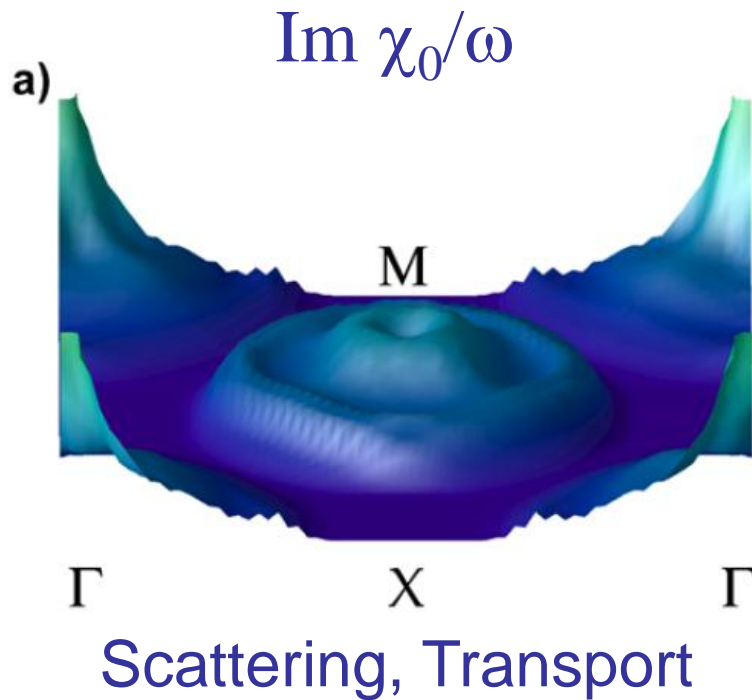
Fermi Surface of  
 $\text{LaFeAsO}$   
(not spin polarized)

Low carrier density:  
 $n_e = n_h = 0.13 / \text{Fe}$

Band anisotropy:  $\langle v_x^2 \rangle / \langle v_z^2 \rangle \sim 15 \rightarrow$   
a modest value that is favorable for applications.

# Lindhard Function (Metal Physics)

- LaFeAs(O,F) neglecting matrix elements:



***Note the pronounced peak at the zone corner.***

# Spin Fluctuations and Superconductivity

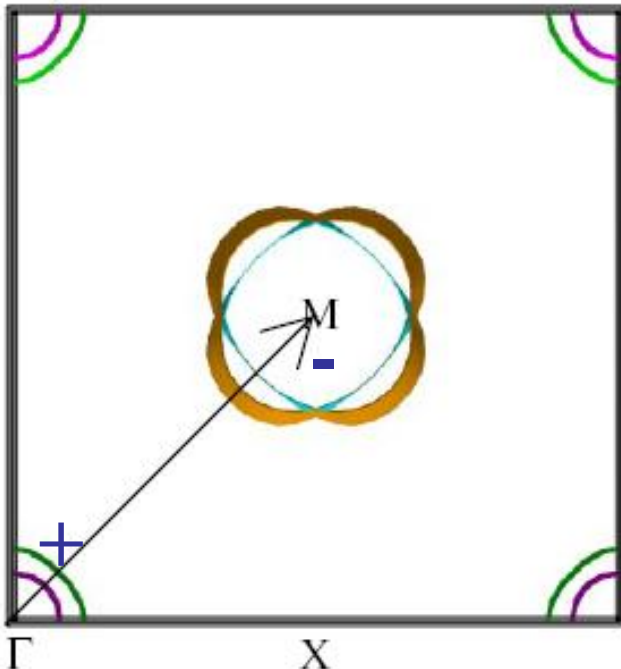
One way to proceed (weak coupling):

- Calculate matrix elements  $V_{\mathbf{k},\mathbf{k}'}$  for a set of  $\mathbf{k},\mathbf{k}'$  on the FS.
- Set-up gap equation -- diagonalize  $V$ .

*Berk-Schrieffer-Fay-Appel weak coupling theory, 1966-1980:*

Singlet:

$$V(\mathbf{q}) = - \frac{I^2(\mathbf{q})\chi_0(\mathbf{q})}{1 - I^2(\mathbf{q})\chi_0^2(\mathbf{q})}$$



In a singlet channel there is a minus sign for spin fluctuations (repulsive), which then favors opposite order parameters on the electron and hole sheets  $\rightarrow$  s +/- state.

Note prior work, Aronov & Sonin (1972); Kuroki and Arita (2001)

Does not have an obvious strongly q-dependent interaction for nodes in a FS.

Electron doped LaFeAsO

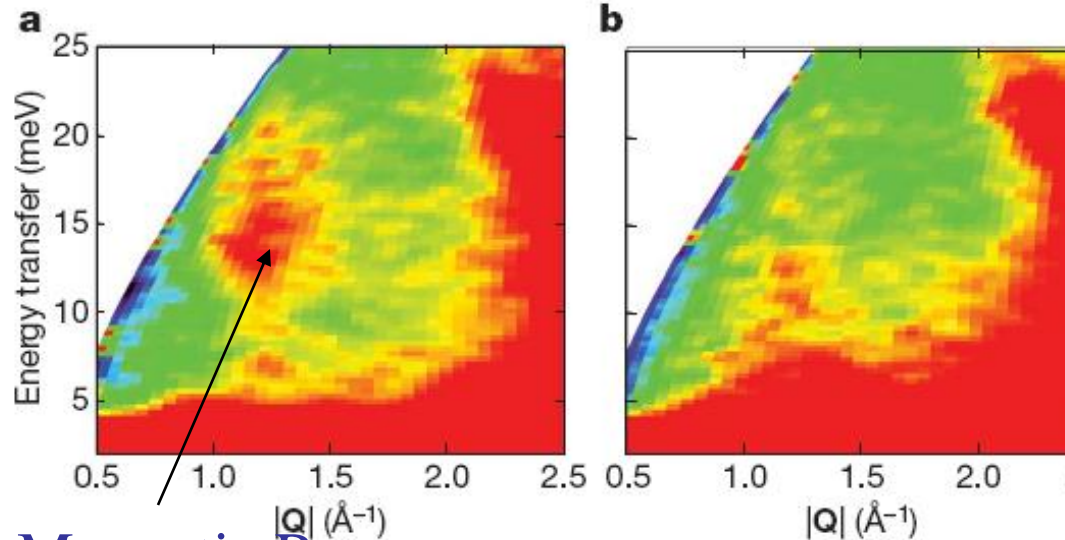
## LETTERS

# Unconventional superconductivity in $\text{Ba}_{0.6}\text{K}_{0.4}\text{Fe}_2\text{As}_2$ from inelastic neutron scattering

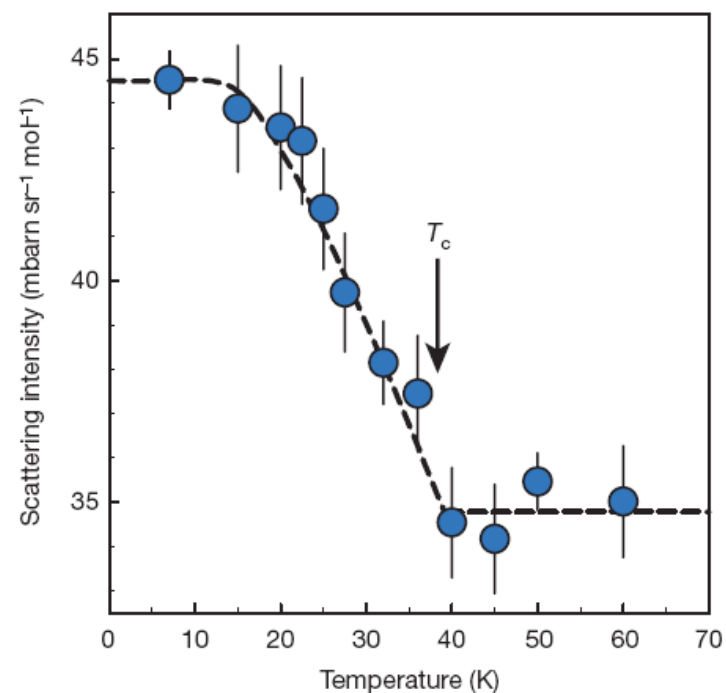
A. D. Christianson<sup>1</sup>, E. A. Goremychkin<sup>2,3</sup>, R. Osborn<sup>2</sup>, S. Rosenkranz<sup>2</sup>, M. D. Lumsden<sup>1</sup>, C. D. Malliakas<sup>2,4</sup>, I. S. Todorov<sup>2</sup>, H. Claus<sup>2</sup>, D. Y. Chung<sup>2</sup>, M. G. Kanatzidis<sup>2,4</sup>, R. I. Bewley<sup>3</sup> & T. Guidi<sup>3</sup>

$T=7\text{K}$

$T=50\text{K}$



Magnetic Resonance

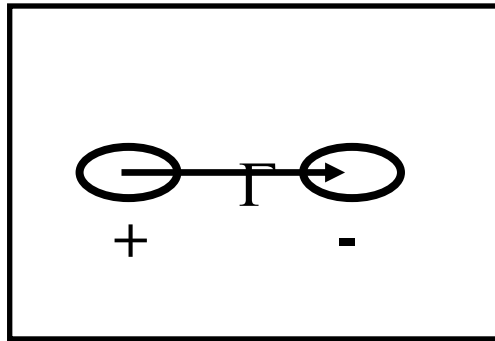


Sign changing gap with  $q$  corresponding to  $(\pi, \pi)$

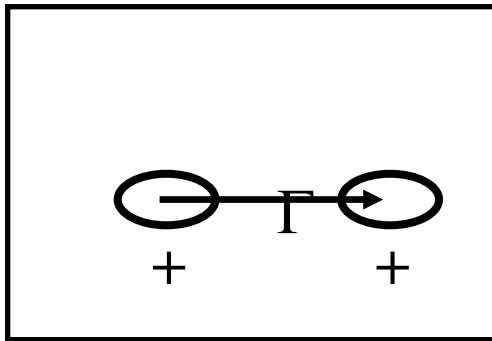


# Small Fermi Surfaces in General

- Does superconductivity arise in general if one has small Fermi surfaces with nesting driven spin fluctuations? – Answer seems to be no.



*p-wave state (triplet):* spin-fluctuation pairing interaction has + sign → Pair breaking for the state shown.



*s-wave state (singlet):* spin-fluctuation pairing interaction has – sign → Pair breaking for the state shown.

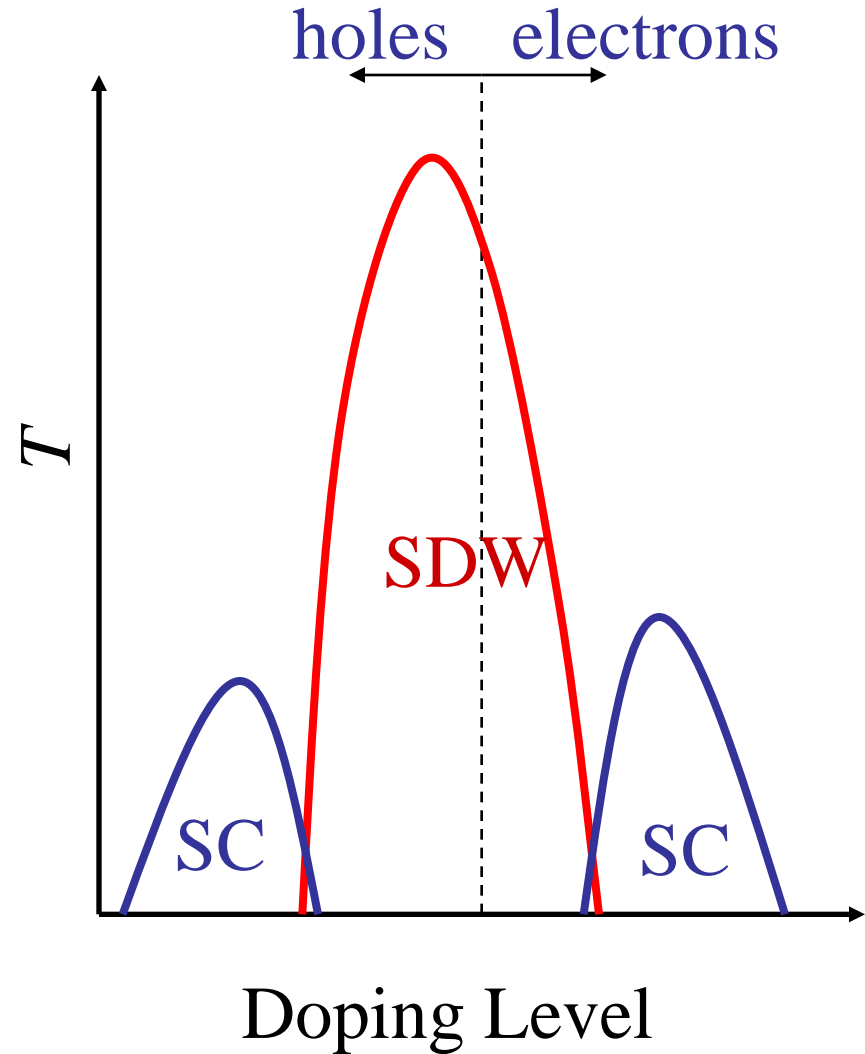
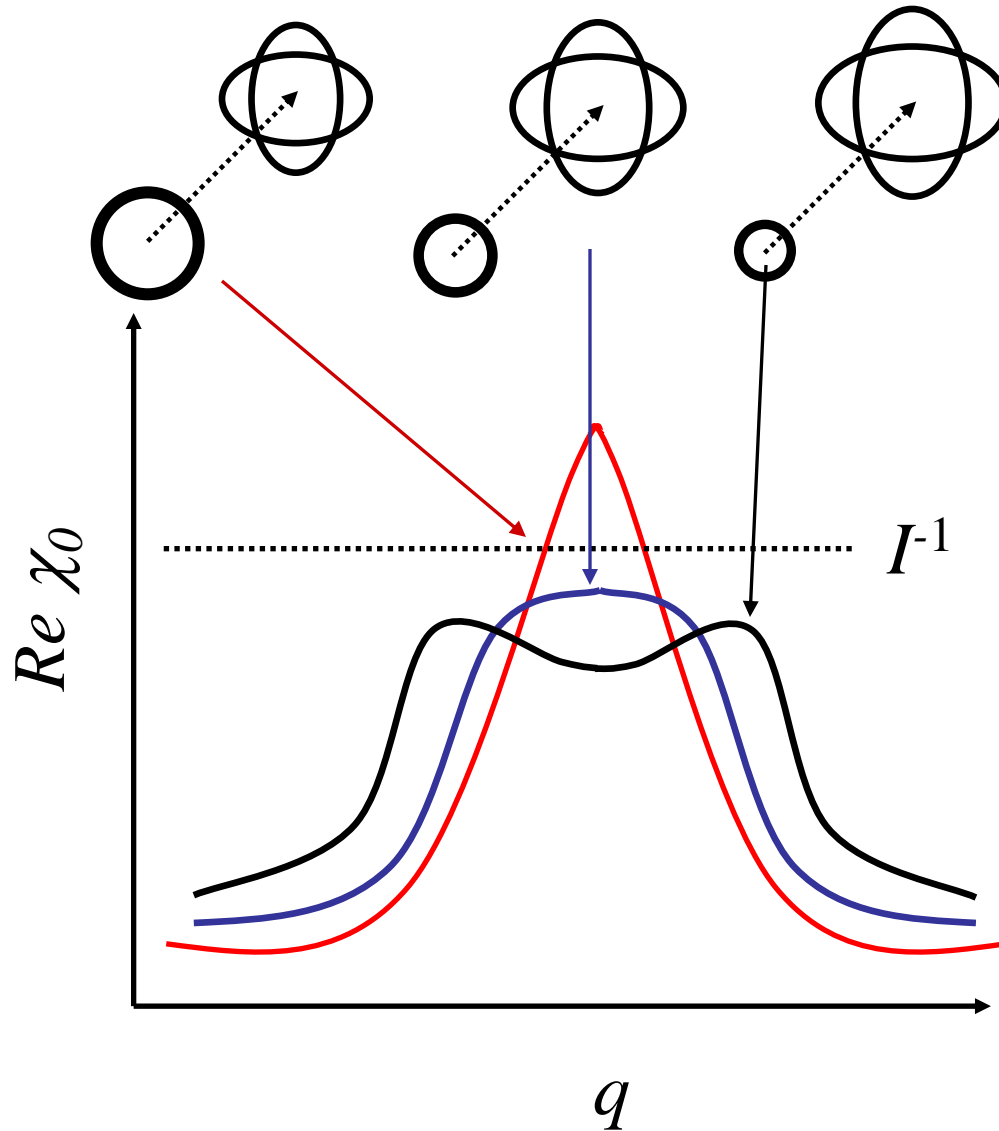
e.g. small pockets on  $\text{Na}_x\text{CoO}_2$  (Johannes et al., 2004).

In such cases, look for chemistry with strong electron phonon and low Stoner parameter, to obtain Kohn anomaly and e-p superconductivity or maybe strange states, e.g. odd frequency.

# Normal Metallic State

- Low carrier density semi-metal (dis-connected small Fermi surfaces).
- Less anisotropic than cuprates, even  $\text{YBa}_2\text{Cu}_3\text{O}_7$ .
- High  $N(E_F)$ .
  - Near itinerant magnetism in general.
  - Expect short coherence length relative to  $T_c$ .
  - Expect high superfluid density.
- Electron-Phonon interaction is weak ( $\lambda \sim 0.2$ ,  $T_c = 0$ )

# Nesting, Doping and the Lindhard Function



*Disorder affects both magnetism and superconductivity*

# Neutron Scattering – Structure Details

## LaFeAsO (Tetragonal → Orth/Mono):

**Table 2 | Properties of LaOFeAs at 4 K**

a, Refined structure parameters					
Atom	Site	x	y	z	B (Å <sup>2</sup> )
La	2e	1/4	1/4	0.1426(3)	0.54(6)
Fe	2f	3/4	1/4	0.5006(12)	0.16(4)
As	2e	1/4	1/4	0.6499(4)	0.23(7)
O	2f	3/4	1/4	-0.0057(17)	0.69(7)

$$z_{\text{As}}(4\text{K}) = 1.308 \text{ \AA}$$

$$z_{\text{As}}(175\text{K}) = 1.317 \text{ \AA}$$

## LaFeAsO<sub>0.92</sub>F<sub>0.08</sub> (Tetragonal):

**Table 3 | Properties of LaO<sub>0.92</sub>F<sub>0.08</sub>FeAs at 10 K (first line), 35 K (second line) and 175 K (third line)**

a, Refined structure parameters					
Atom	Site	x	y	z	B (Å <sup>2</sup> )
La	2c	1/4	1/4	0.1448(3)	0.40(5)
		1/4	1/4	0.1458(3)	0.50(5)
		1/4	1/4	0.1446(3)	0.73(5)
Fe	2b	3/4	1/4	1/2	0.32(4)
		3/4	1/4	1/2	0.41(4)
		3/4	1/4	1/2	0.65(4)
As	2c	1/4	1/4	0.6521(4)	0.41(7)
		1/4	1/4	0.6515(4)	0.40(6)
		1/4	1/4	0.6527(4)	0.69(7)
O/F	2a	3/4	1/4	0	0.53(6)
		3/4	1/4	0	0.62(6)
		3/4	1/4	0	0.71(6)

$$z_{\text{As}}(10\text{K}) = 1.323 \text{ \AA}$$

$$z_{\text{As}}(175\text{K}) = 1.331 \text{ \AA}$$

Non-magnetic LDA calc.  
(LaFeAsO – Tetragonal)

$$z_{\text{As}}(\text{LDA}) = 1.159 \text{ \AA}$$

**A huge difference!**



# Structure and Magnetism

- As height is too low by  $>0.1 \text{ \AA}$  in non-magnetic LSDA calculations.
- SDW is too robust in DFT.
- Using GGA and including magnetism one can obtain much better As height. In that case magnetism is extremely robust ( $m \sim 2\mu_B$ ) contrary to experiment.
- Discrepancy in As height persists in the paramagnetic (superconducting) doped phases.

# Metals Where the LSDA Overestimates Ferromagnetism

**Class 1:** Ferromagnets where the LDA overestimates the magnetization.

	m (LDA, $\mu_B$ /f.u.)	m (expt., $\mu_B$ /f.u.)
ZrZn <sub>2</sub>	0.72	0.17
Ni <sub>3</sub> Al	0.71	0.23
Sc <sub>3</sub> In	1.05	0.20

**Class 2:** Paramagnets where the LDA predicts ferromagnetism

	m (LDA, $\mu_B$ /f.u.)	m (expt., $\mu_B$ /f.u.)
FeAl	0.80	0.0
Ni <sub>3</sub> Ga	0.79	0.0
Sr <sub>3</sub> Ru <sub>2</sub> O <sub>7</sub>	1.1	0.0
Na <sub>0.7</sub> CoO <sub>2</sub>	0.30	0.0

**c.f. “Normal” Materials**

	m (DFT, $\mu_B$ /f.u.)	m (expt., $\mu_B$ /f.u.)
bcc Fe	2.17	2.12
SrRuO <sub>3</sub>	1.59	1.6

# Renormalization and The Fluctuation Dissipation Theorem

Relates fluctuation amplitude to dissipation term, i.e. spin fluctuation spectrum:

$$\xi^2 = \frac{4\hbar}{\Omega} \int d^3q \int \frac{d\omega}{2\pi} \frac{1}{2} \text{Im} \chi(\mathbf{q}, \omega)$$

Landau functional approach (after Moriya, Shimizu, others) is based on the magnetic moment dependence of the total energy *without* fluctuations

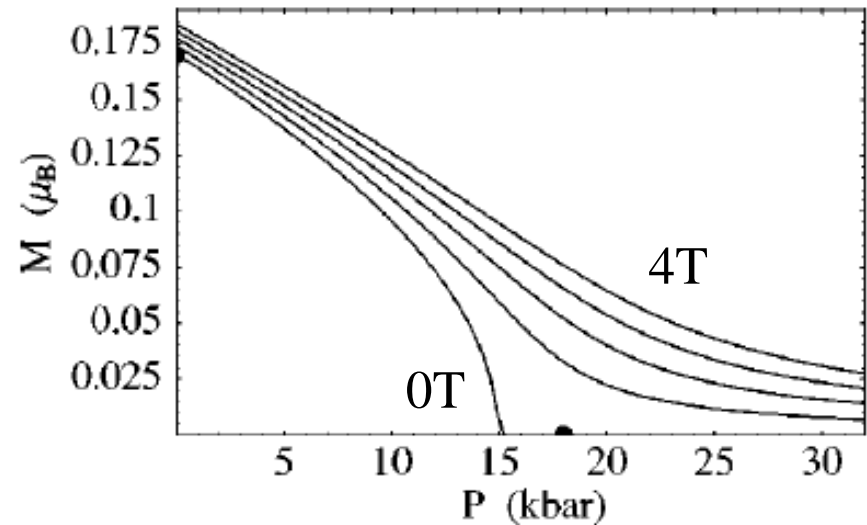
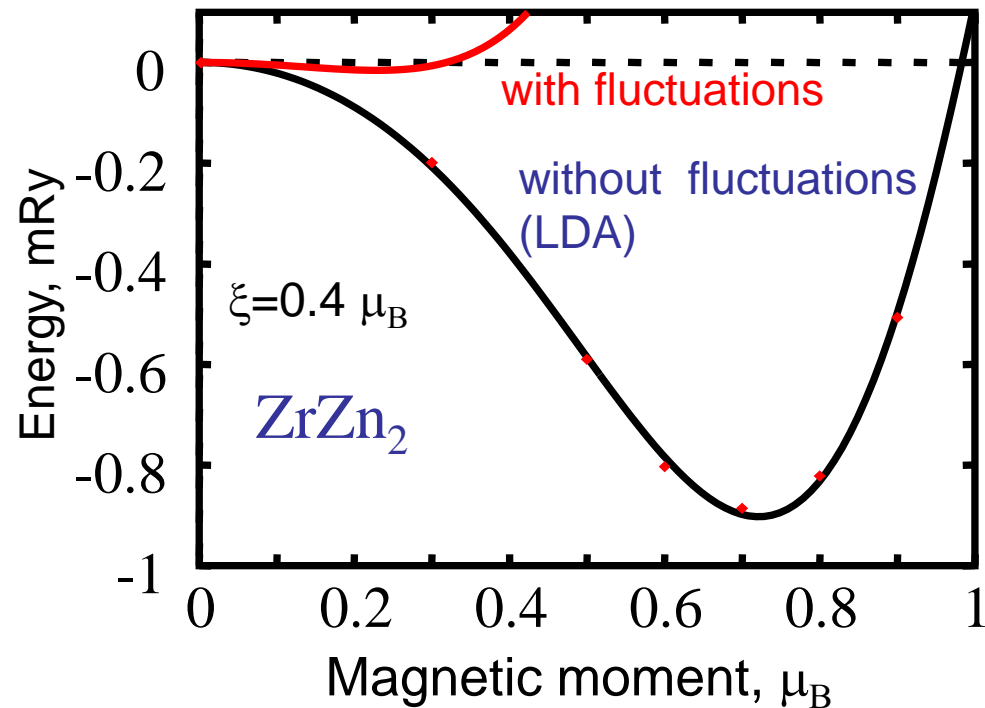
$$\Delta E(M) = aM^2 + bM^4 + cM^6 \quad a^{-1} / 2 = \chi, \text{ susceptibility}$$

Spin fluctuations renormalize this dependence, i.e.  $a \rightarrow \alpha$ , etc. via integration of the Landau functional with Gaussian of rms width  $\xi$ .

- 1. Large renormalization  $\rightarrow$  large fluctuation amplitude.**
- 2. Large amplitude requires large integral  $\rightarrow$  Im  $\chi$  large over wide range of  $\mathbf{q}$  and  $\omega$ .**

# Example: $\text{ZrZn}_2$ (Weak Itinerant Ferromagnet)

Bare LDA moment of  $\sim 0.7 \mu_B$  to  $\sim 0.2 \mu_B$  by fluctuations  $\xi \sim 0.4 \mu_B$



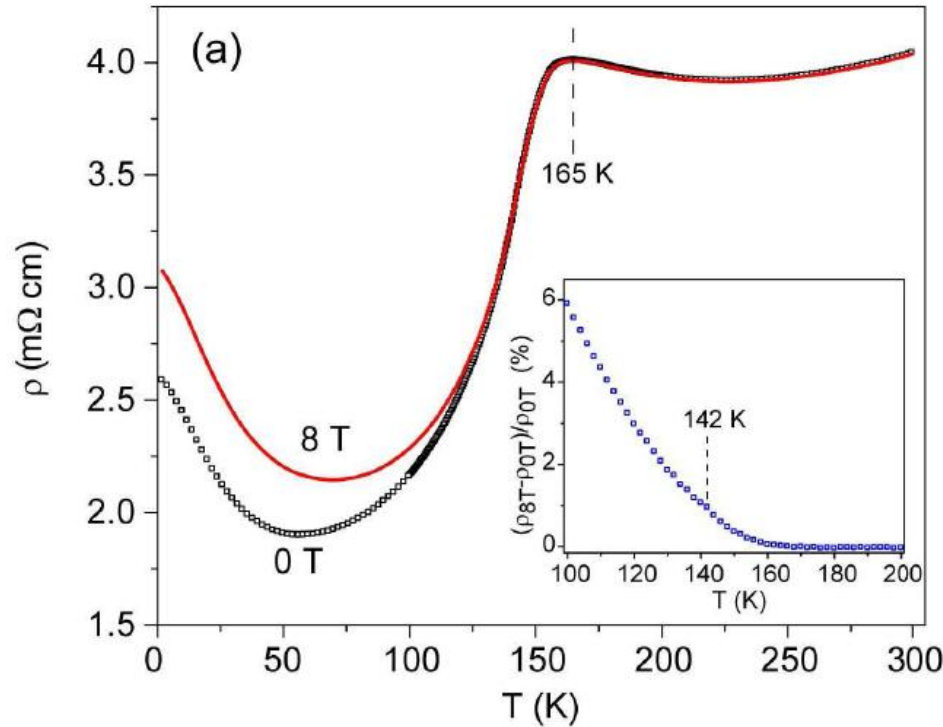
I.I. Mazin and D.J. Singh, Phys. Rev. B **69**, 020402 (2004).



# Resistivity in LaFeAsO

McGuire *et al.* (cond-mat):

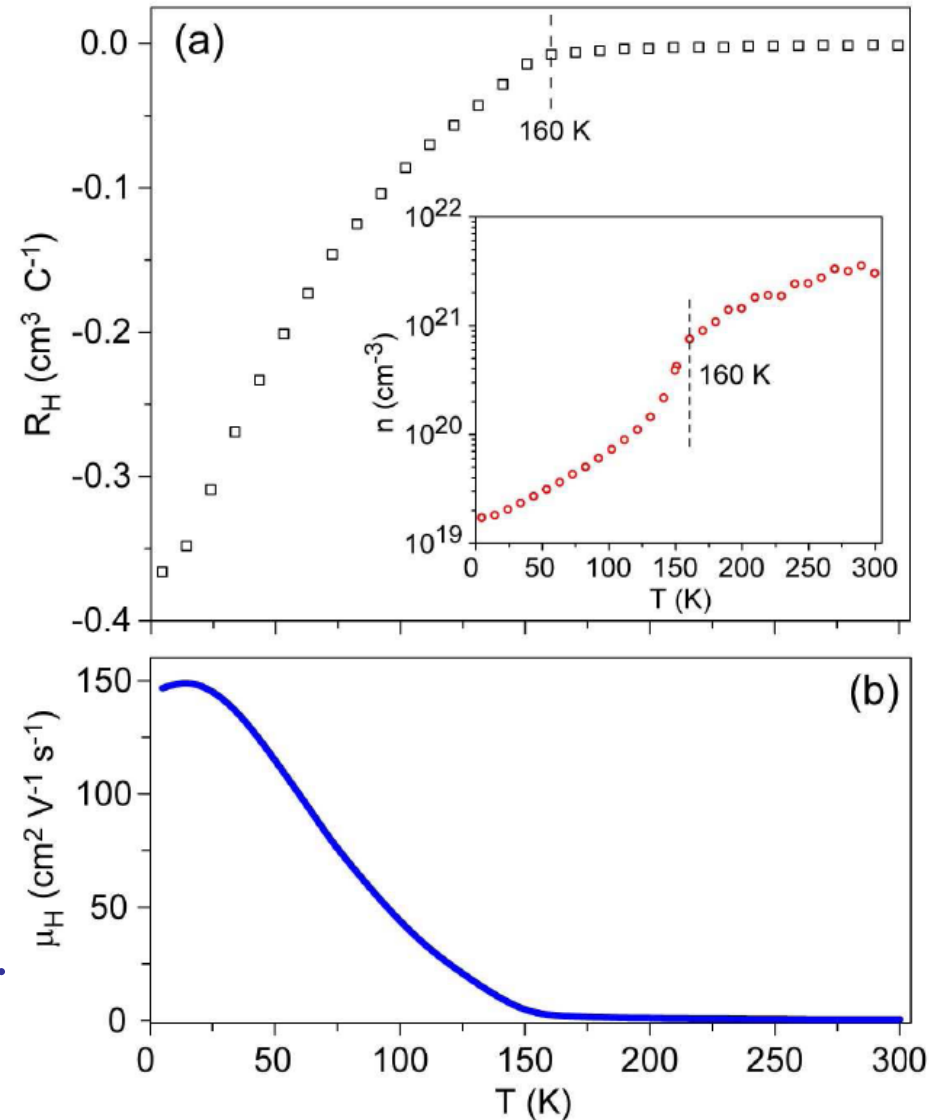
Resistivity:



Evidence of strong interplay of magnetic ordering and Fermi surface.

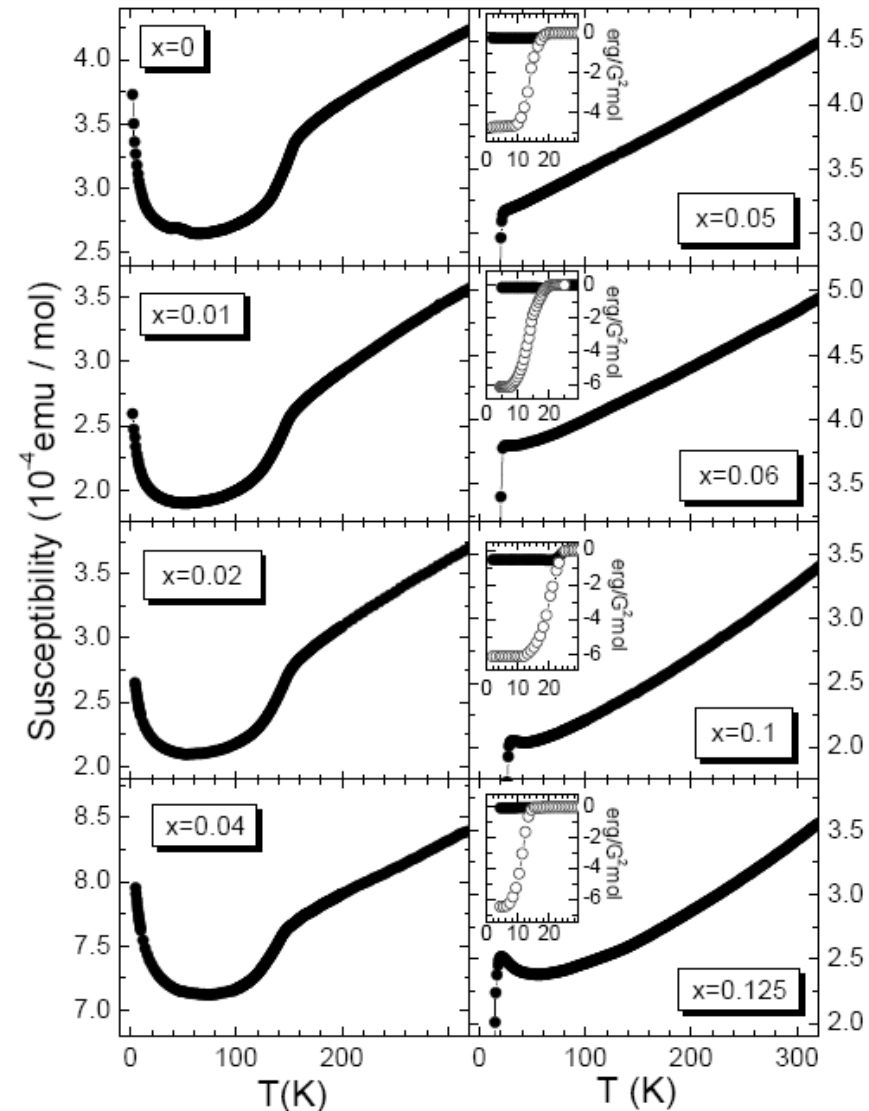
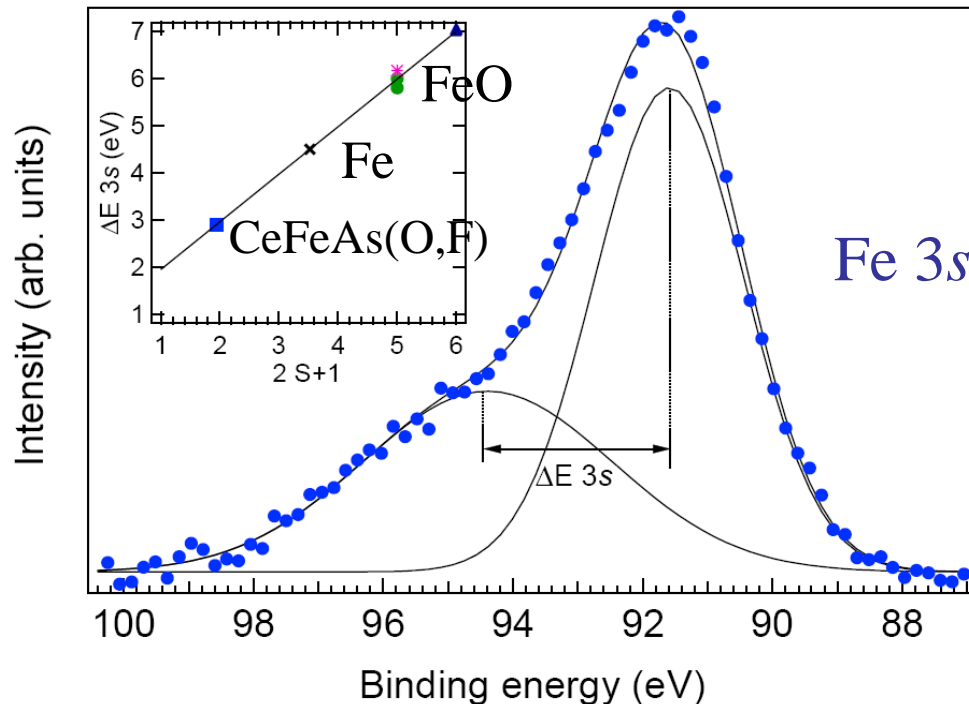
Evidence of spin fluctuations.

Hall:



# Strong Spin Fluctuations in Normal State

- Transport data.
- Susceptibility -  $\chi(T)$ .
- Spectroscopy.
- Scattering.
- Overly magnetic in LDA.
- Precursor structural transition.

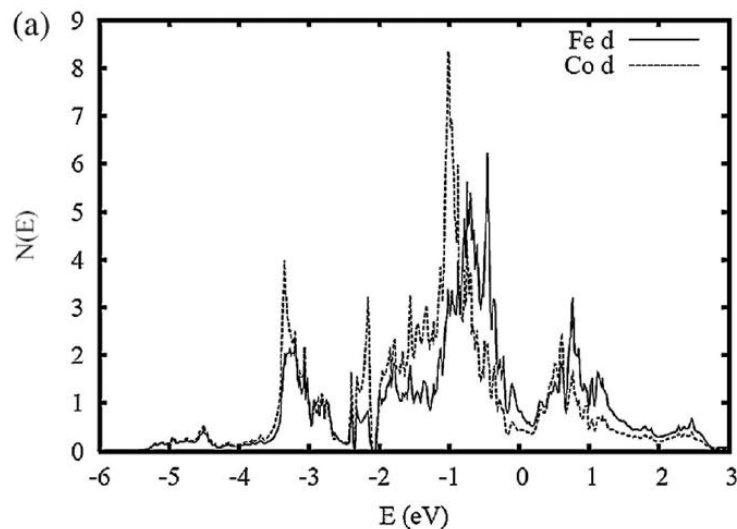
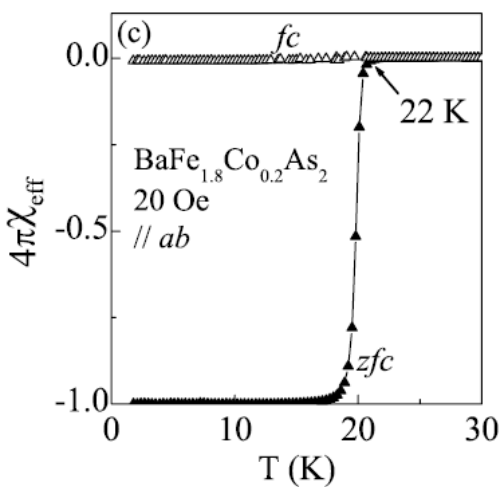


R. Klingeler et al., cond-mat  
LaFeAsO<sub>1-x</sub>F<sub>x</sub>

Bondino et al. (2008); c.f. NbFe<sub>2</sub>

# Superconductivity in Metal Doped Materials

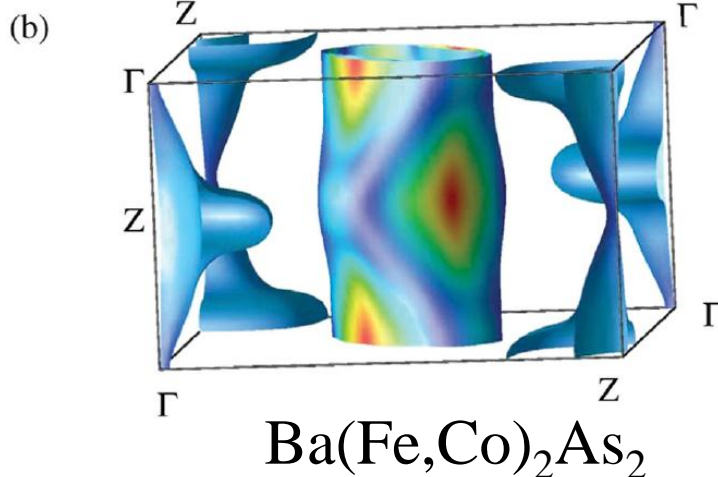
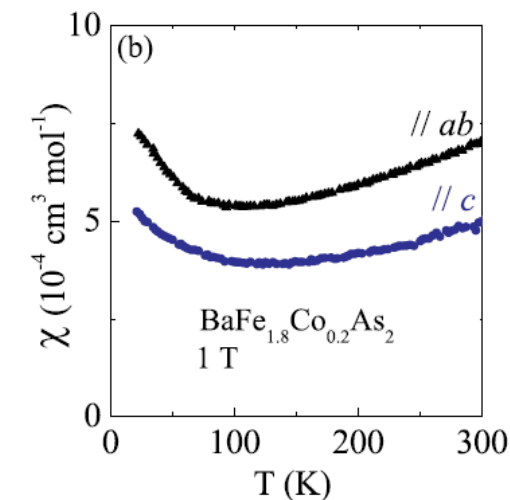
- Superconductivity requires destruction of SDW by doping.
- Remarkably, doping with Co or Ni works (*c.f.* cuprates).



Calculations show that alloy behaves very much in a rigid band sense.

Fe-Co-Ni behave very similarly apart from electron count.

Mn and Cr show strong spin dependent hybridization (different).



*Is iron essential?*

# ThCr<sub>2</sub>Si<sub>2</sub> Structure

JOURNAL OF SOLID STATE CHEMISTRY **56**, 278–287 (1985)

## The Most Populous of All Crystal Structure Types—the Tetragonal BaAl<sub>4</sub> Structure

W. B. PEARSON

*Departments of Physics and of Chemistry, University of Waterloo,  
Waterloo, Ontario, Canada, N2L 3G1*

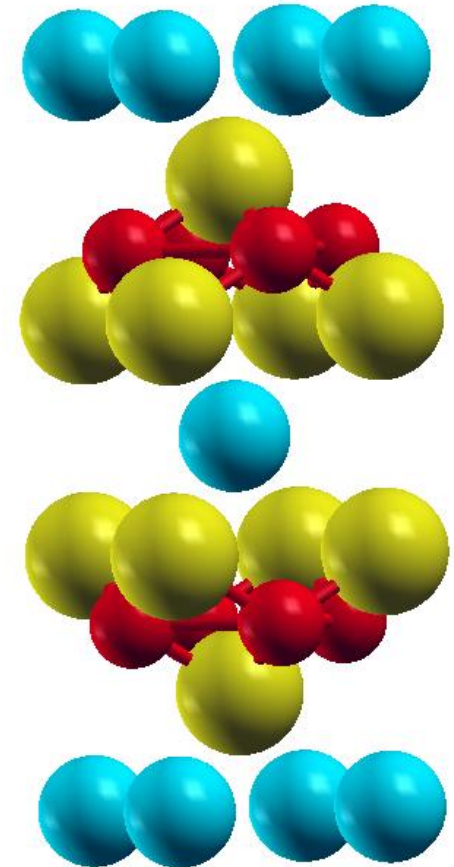
Received April 9, 1984; in revised form August 3, 1984

The BaAl<sub>4</sub> (ThCr<sub>2</sub>Si<sub>2</sub>) *tI10* structure, *MN<sub>2</sub>X<sub>2</sub>*, is not only the most populous of all known structure types, being adopted by some 400 phases, but is representative of a new group of metallurgically

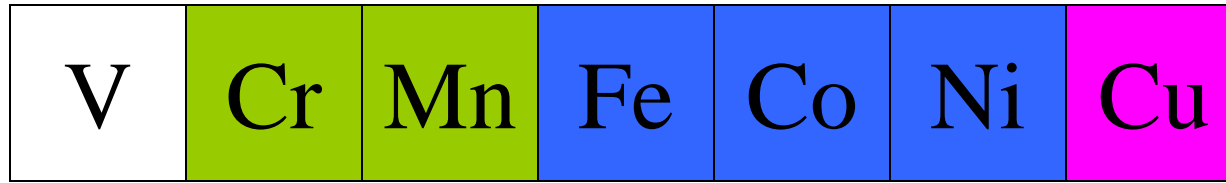
Pearson data-base now has 2,000+ ThCr<sub>2</sub>Si<sub>2</sub> entries

*Can be stabilized with different bonding patterns  
→ extremely wide variety of properties.*

**Examples:** BaZn<sub>2</sub>P<sub>2</sub>, BaFe<sub>2</sub>As<sub>2</sub>, BiN<sub>2</sub>Th<sub>2</sub>, CaAl<sub>2</sub>Ga<sub>2</sub>,  
SrCd<sub>2</sub>Ga<sub>2</sub> ...



# ThCr<sub>2</sub>Si<sub>2</sub> Structure *DT*<sub>2</sub>As<sub>2</sub>



Strong spin dependent *T*-As hybridization, G-type AF with high  $T_N$ .  
BaCr<sub>2</sub>As<sub>2</sub> is itinerant metal. BaMn<sub>2</sub>As<sub>2</sub> is a semiconductor.

Metallic  $M^{2+}$  sheets. As is anionic. *M* can be alloyed.  
Fe: SDW and superconductivity.  
Co: Near FM  
Ni: electron-phonon superconductor.

BaCu<sub>2</sub>As<sub>2</sub> has Cu  $d^{10}$  with As-As and Cu-As sp bonding.

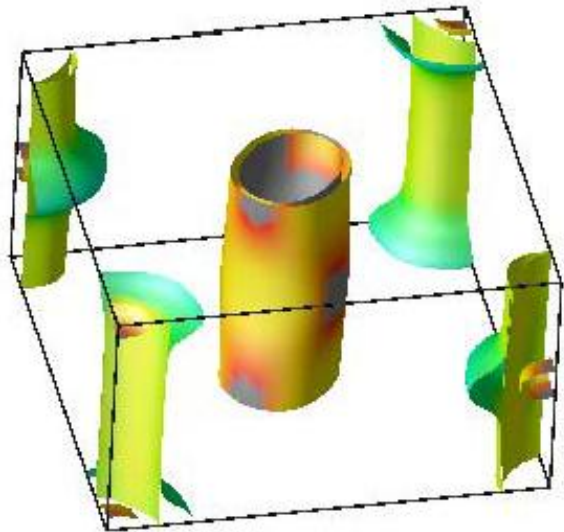
*Chemistry of chalcogenides may be expected to differ.*

# Is Iron Essential for Iron-Based Superconductivity?

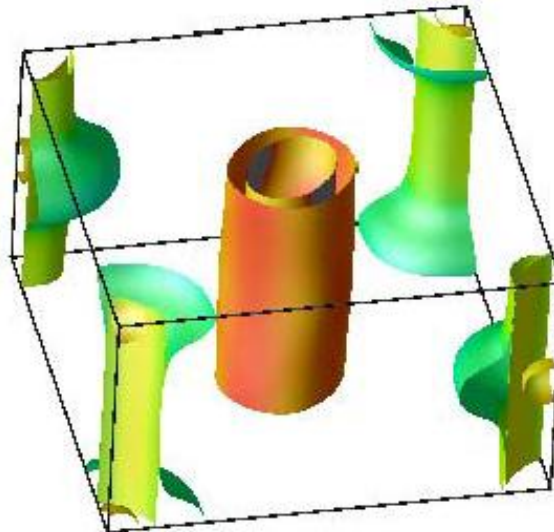
$\text{KRu}_2\text{As}_2$ ;  $\text{KFe}_2\text{As}_2$ ;  $\text{KCo}_2\text{As}_2$ : Can we do something with the alloys?

$\text{KFeCoAs}_2 \approx \text{BaFe}_2\text{As}_2$

$\text{KFeCoAs}_2$

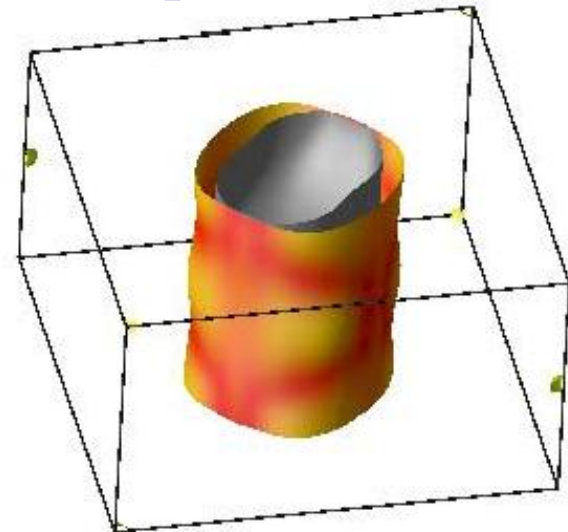


Virtual Crystal



Ordered Cell

$\text{KFe}_{0.5}\text{Co}_{1.5}\text{As}_2$   
(overdoped)

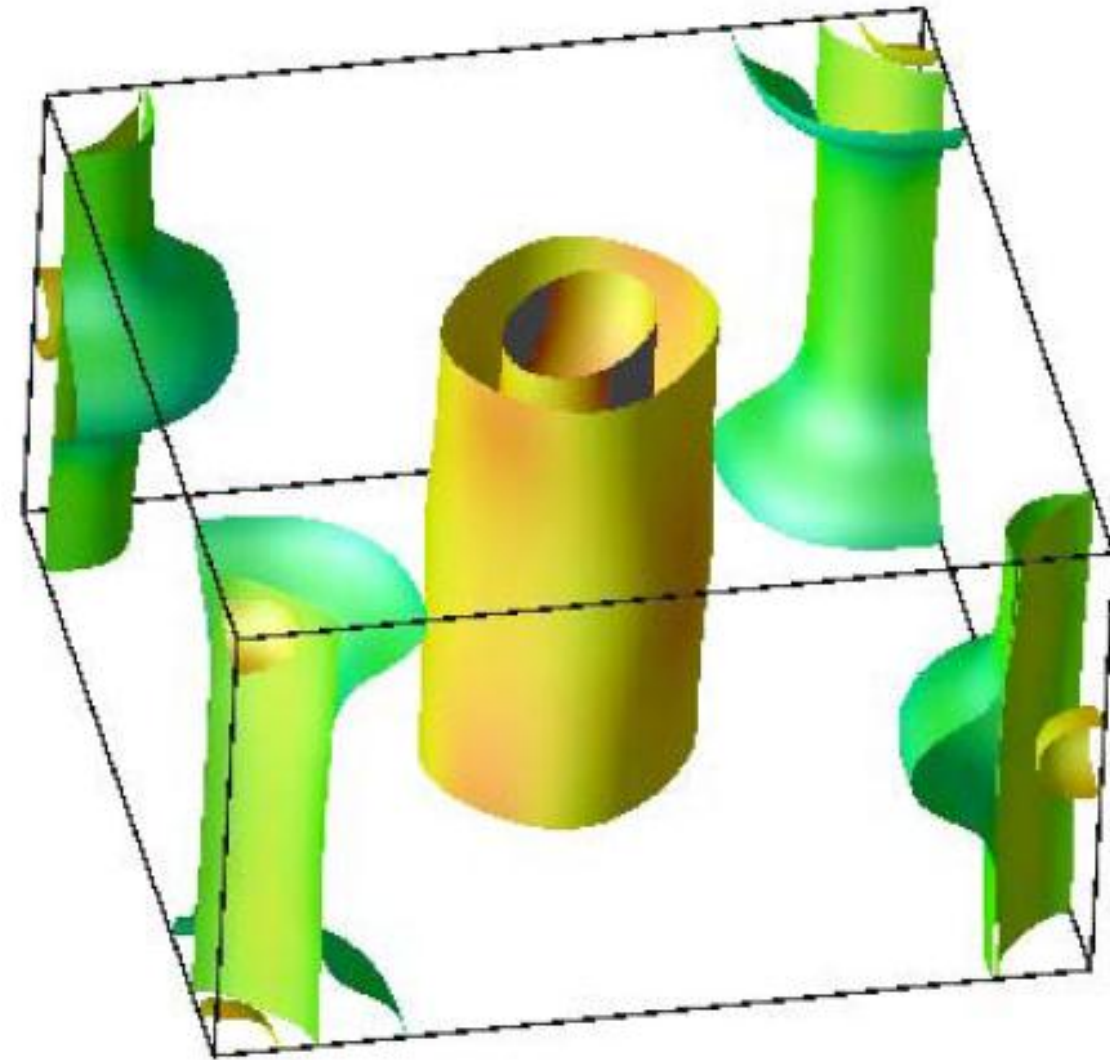


Virtual Crystal

Coherent alloy: Look for superconductivity in  $\text{KFe}_{1-x}\text{Co}_{1+x}\text{As}_2$  (Fe-poor)

Also, similar results, but less magnetic for  $\text{KRu}_{1-x}\text{Co}_{1+x}\text{As}_2$ , but significantly less magnetic (Fe-free).

# Fermi Surface of Ordered $\text{KRuCoAs}_2$



Do not find SDW magnetic order at this composition.

Will it appear as Ru concentration is reduced.

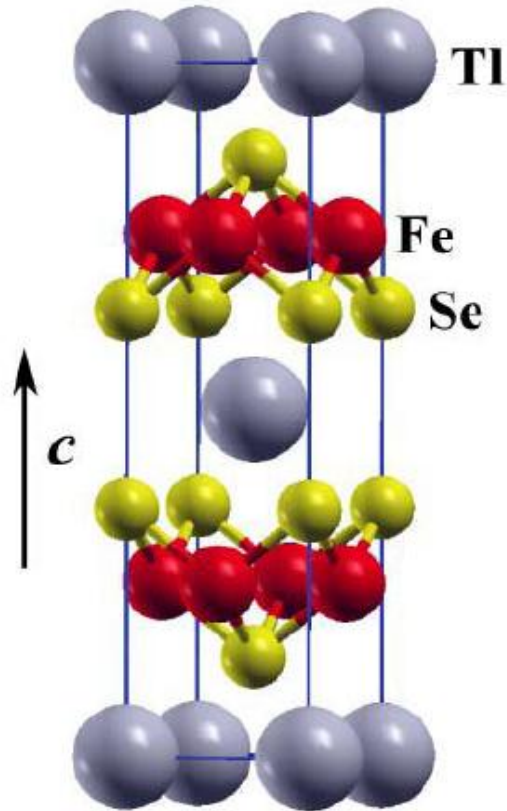
Will superconductivity appear?

$$\chi(\mathbf{q}) = \frac{\chi_0(\mathbf{q})}{1 - \chi_0(\mathbf{q})I(\mathbf{q})}$$

Ru lowers average Stoner parameter  $I(\mathbf{q})$  both because it is  $4d$  and because of Ru  $d - \text{As } p$  hybridization.

# Properties of the Over-Doped Side: $\text{TlFe}_2\text{Se}_2$

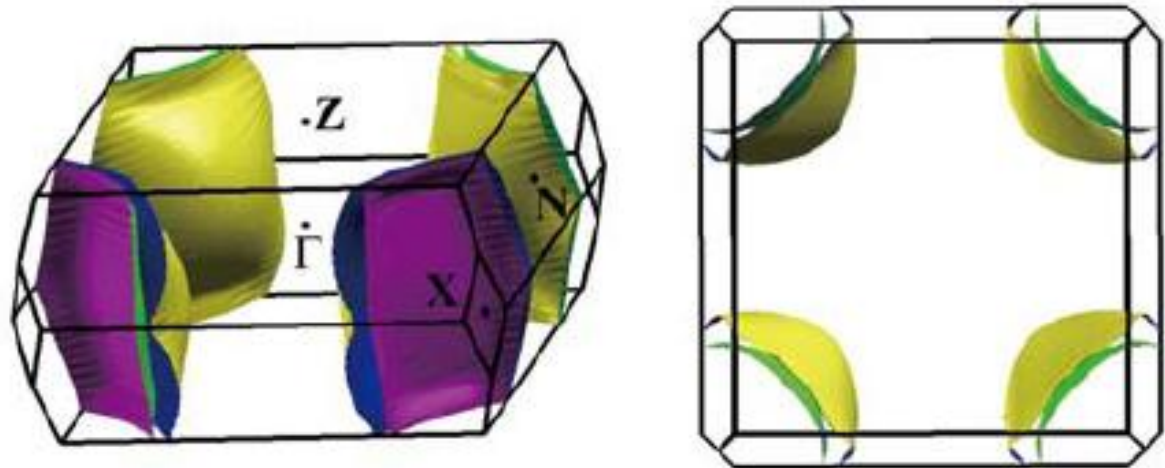
Haggstrom, 1986



Antiferromagnetic  
with  $T_N \sim 450$  K.  
Unknown order.

First Principles Results (GGA):

- Electronic structure is very similar to FeSC, but with higher electron count (0.5 e/Fe).
- Strong instability against nearest neighbor AFM (78 meV/Fe) and weaker instability against FM (44 meV/Fe). No instability for SDW type chain order  $\rightarrow$  itinerant n.n. AFM



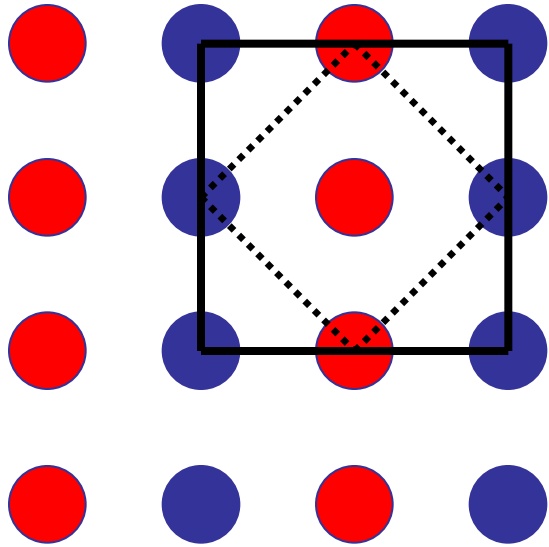
Non spin polarized Fermi surface



# Competing Magnetic States

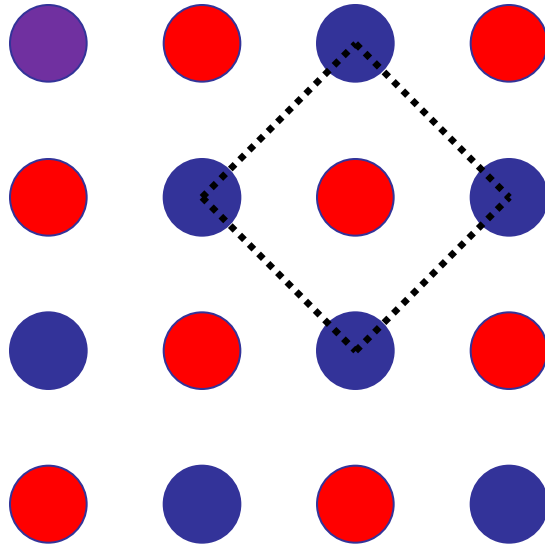
Competition between different magnetic states provides phase space for fluctuations and works against ordering.

SDW -  $c(2 \times 2)$



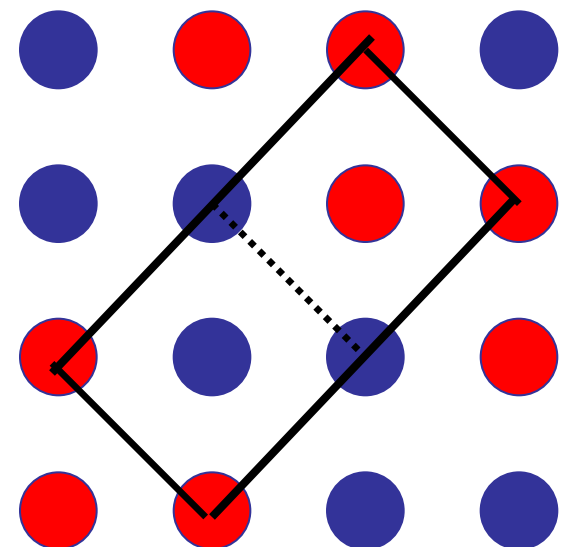
LaFeAsO

N.N (1x1)



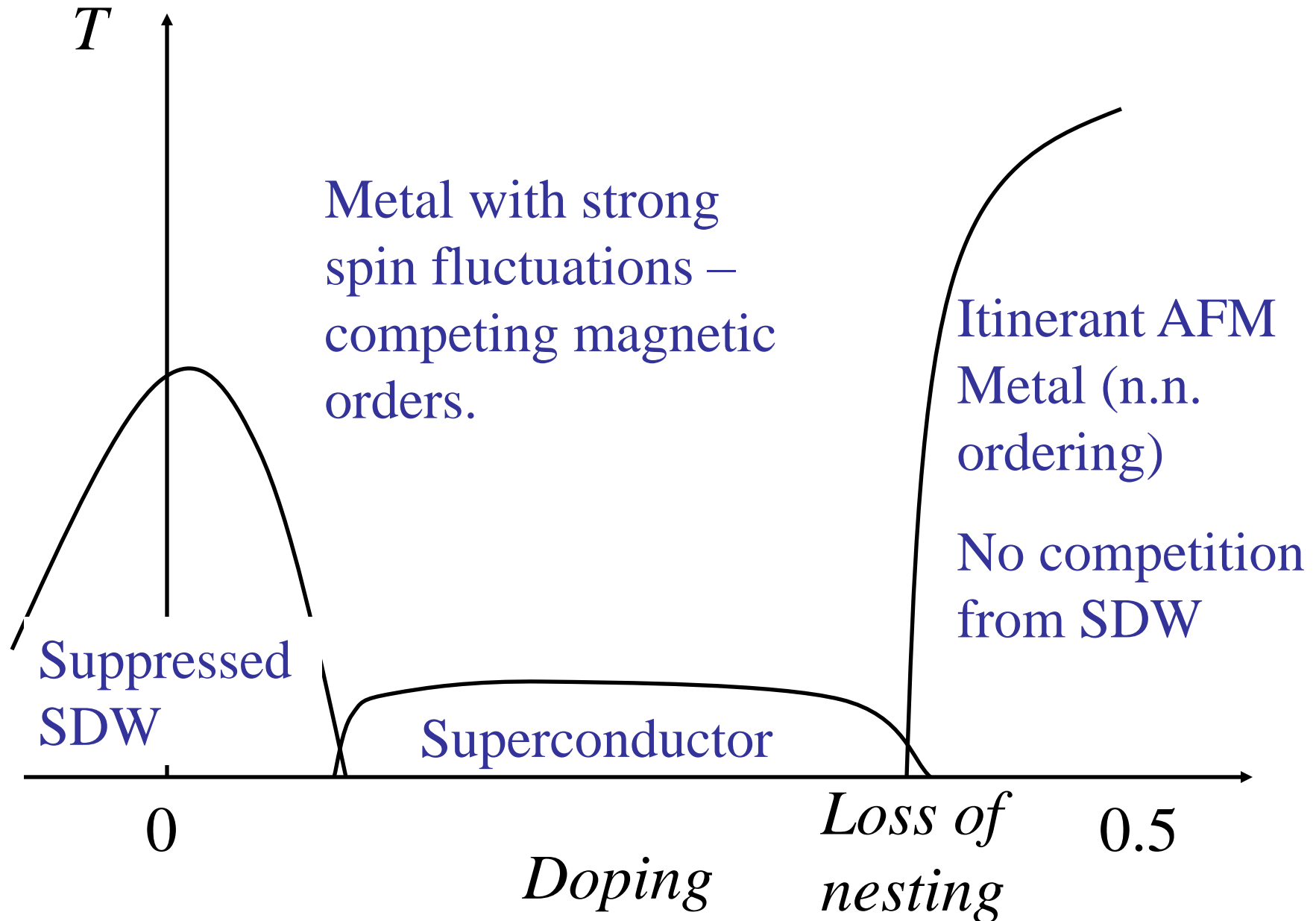
TlFe<sub>2</sub>Se<sub>2</sub>

(2x1)



Fe<sub>1+x</sub>Te

# Possible Electron Doped Phase Diagram



# Comparison with Cuprates

	Cuprates	Fe-As
Magnetic & superconducting phases	Yes, magnetic phase insulating above & below $T_N$ . (Mott insulator)	Yes. Magnetic phase is metallic. Intimate connection of magnetic and superconducting phases
Electronic structure	Moderate $N(E_F)$ , large FS at least for optimal doped	High $N(E_F)$ , small disconnected FS
Doping	Essential.	Destruction of SDW is enough.
Magnetic character	Local moment	Apparently itinerant with strong renormalization from DFT.
Correlations	Strong. Mott-Hubbard type (e.g. p.e. satellites)	Possibly substantial but different e.g. spin fluctuations. Not Mott-Hubbard type.
Superconductivity	<i>d</i> -wave. Nodes. One band. Highly anisotropic	Nodeless ( <i>s</i> +/- ?). Two band. Less anisotropic (material dependent).
Structure	Oxides, corner shared octahedra -- complex	Simpler – tetragonal / orthorhombic, small unit cells.

# Conclusions

- Iron superconductors behave very differently from cuprates – perhaps a rather different mechanism or perhaps we need to look deeper for the connections.
- Strong renormalization of magnetic properties due to strong spin fluctuations – almost certainly necessary for understanding of the normal state and the superconductivity.
- Extended s-wave (+/-) state is a likely scenario.
- Interesting interplay between magnetism and structure.

# Questions

- Can we identify materials with “strong” spin fluctuations and quantify “strong”?
- Can we identify competing magnetic states, even those with relatively weak  $q$ -dependence?
- Could we connect inelastic scattering with magnetic renormalization (fluctuation-dissipation)?
- Can we connect with transport experiments?
- Can we identify trends in magnetic behavior that would allow us to predict new superconductors, or ways to vary composition to improve superconductivity?
- ...