

# Electronic structure of strongly correlated materials Part III

Vladimir I. Anisimov

*Institute of Metal Physics  
Ekaterinburg, Russia*



## **Results of DFT+DMFT calculations:**

**Strongly correlated metal  $\text{Sr}(\text{Ca})\text{VO}_3$**

**Metal-insulator transition in  $\text{V}_2\text{O}_3$**

**Heavy fermions in d-system  $\text{Li}_2\text{VO}_4$**

**Charge transfer insulator  $\text{NiO}$**

**Metal-insulator transition with pressure in  $\text{MnO}$**

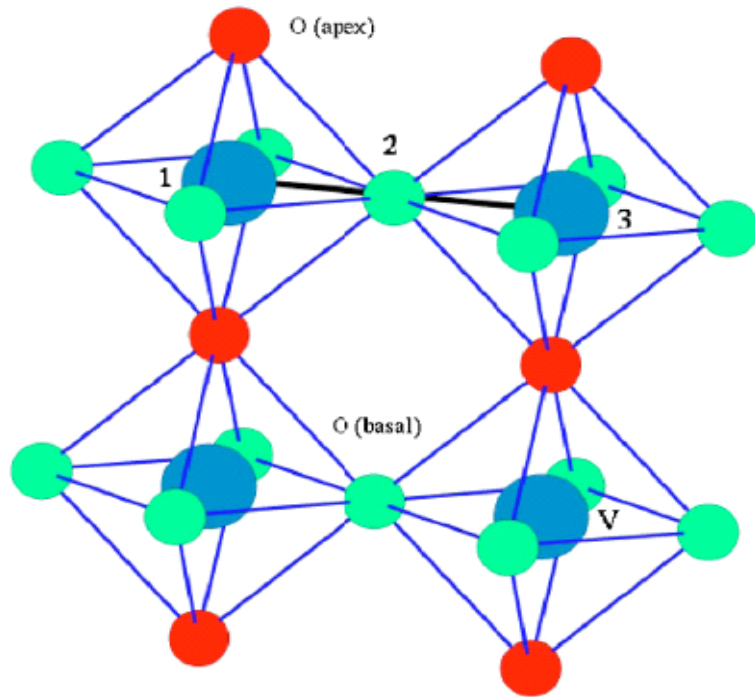
**Correlated covalent insulators  $\text{FeSi}$  and  $\text{FeSb}_2$**

**Novel superconductor  $\text{LaOFeAs}$**

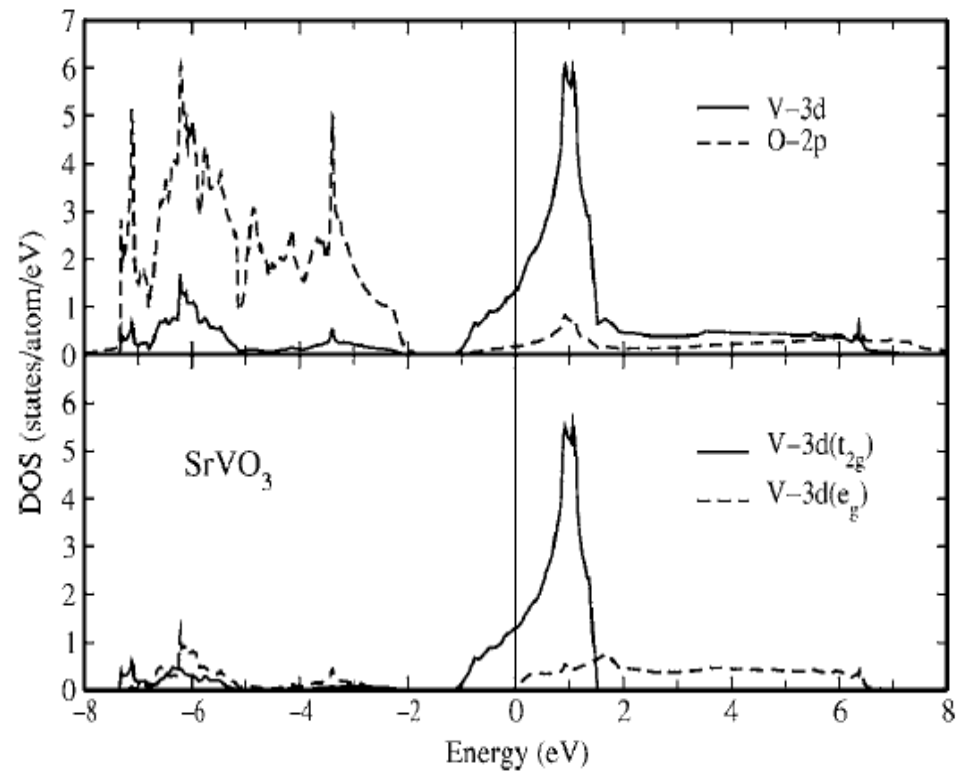
**Jahn-Teller distortions in  $\text{KCuF}_3$**

**f-electrons localization in  $\text{Ce}$**

# Strongly correlated metal $\text{SrVO}_3$

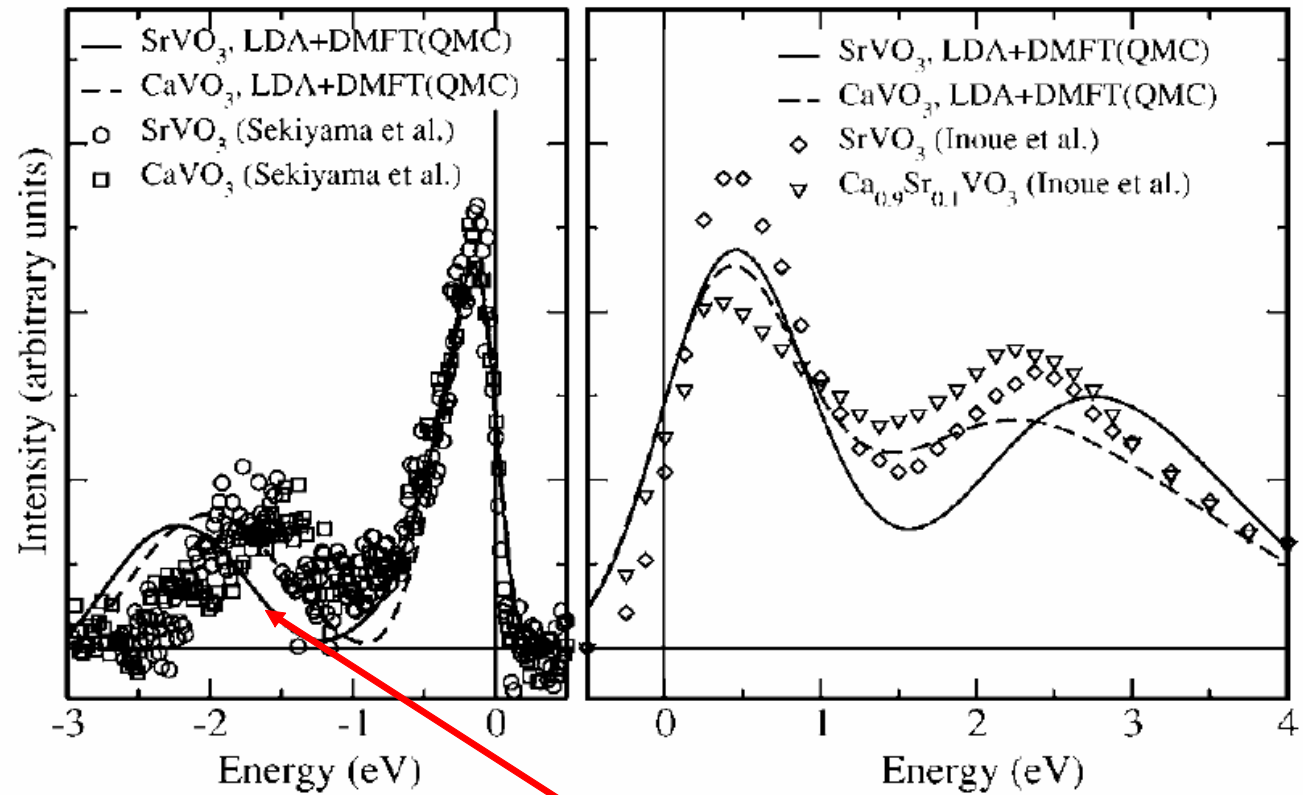
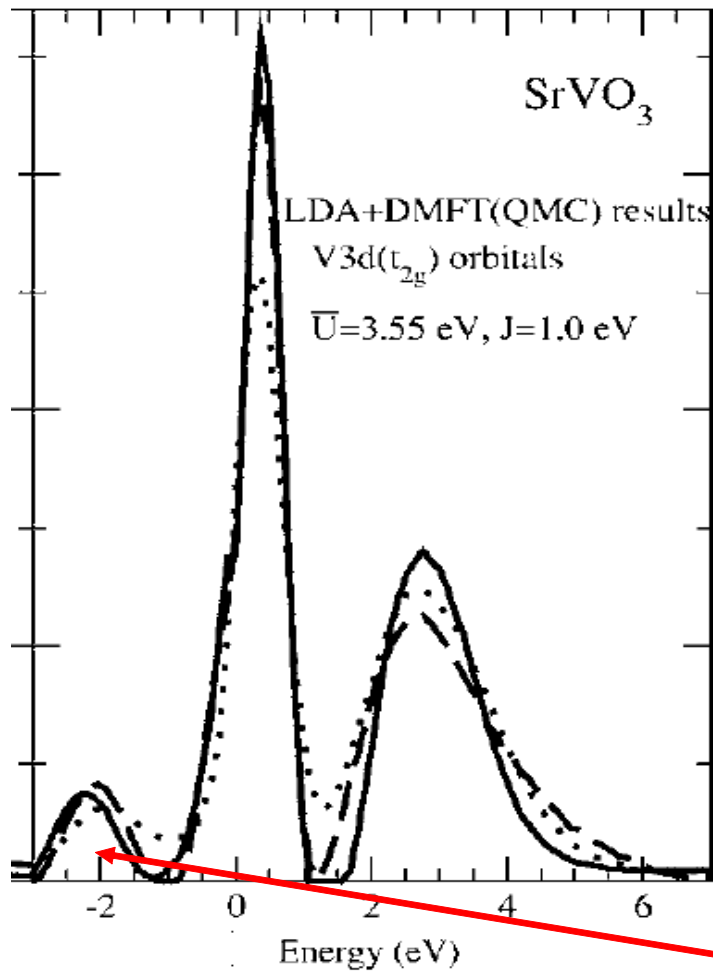


$\text{V}^{+4}$  ( $d^1$ ) ion in cubic perovskite crystal structure



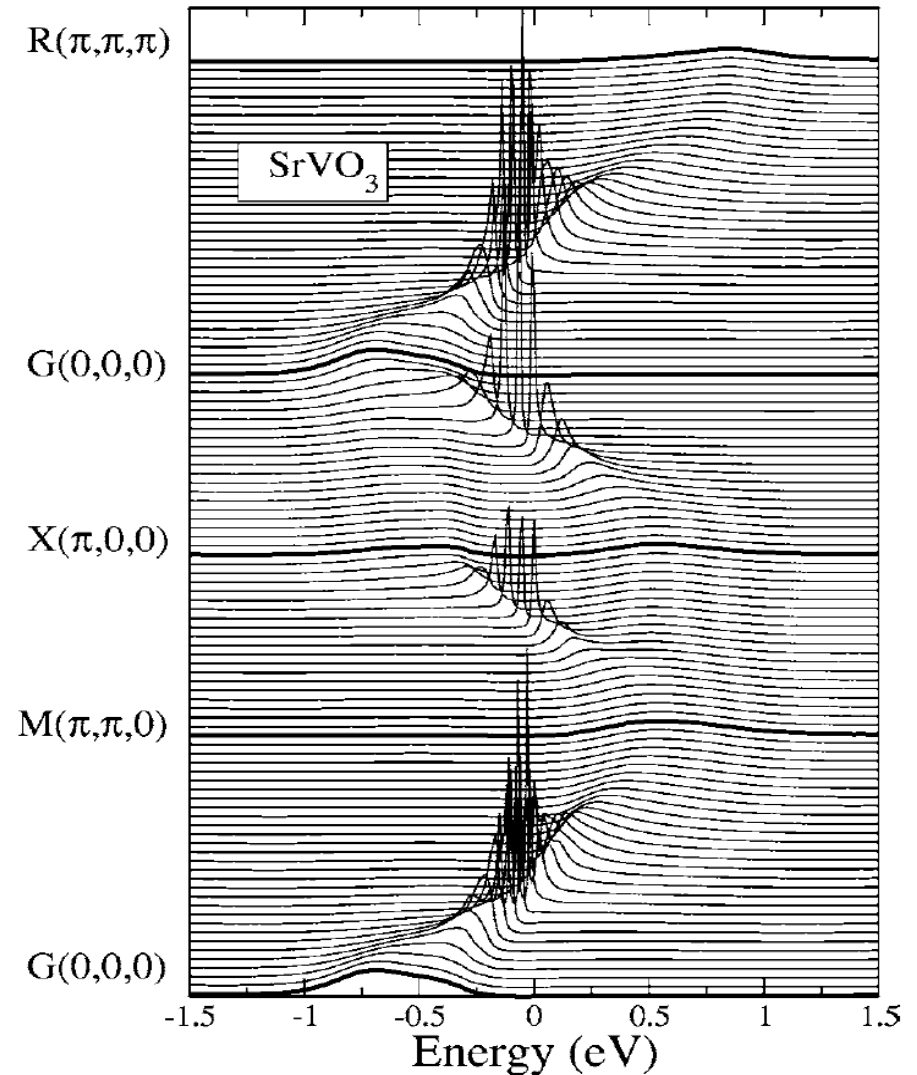
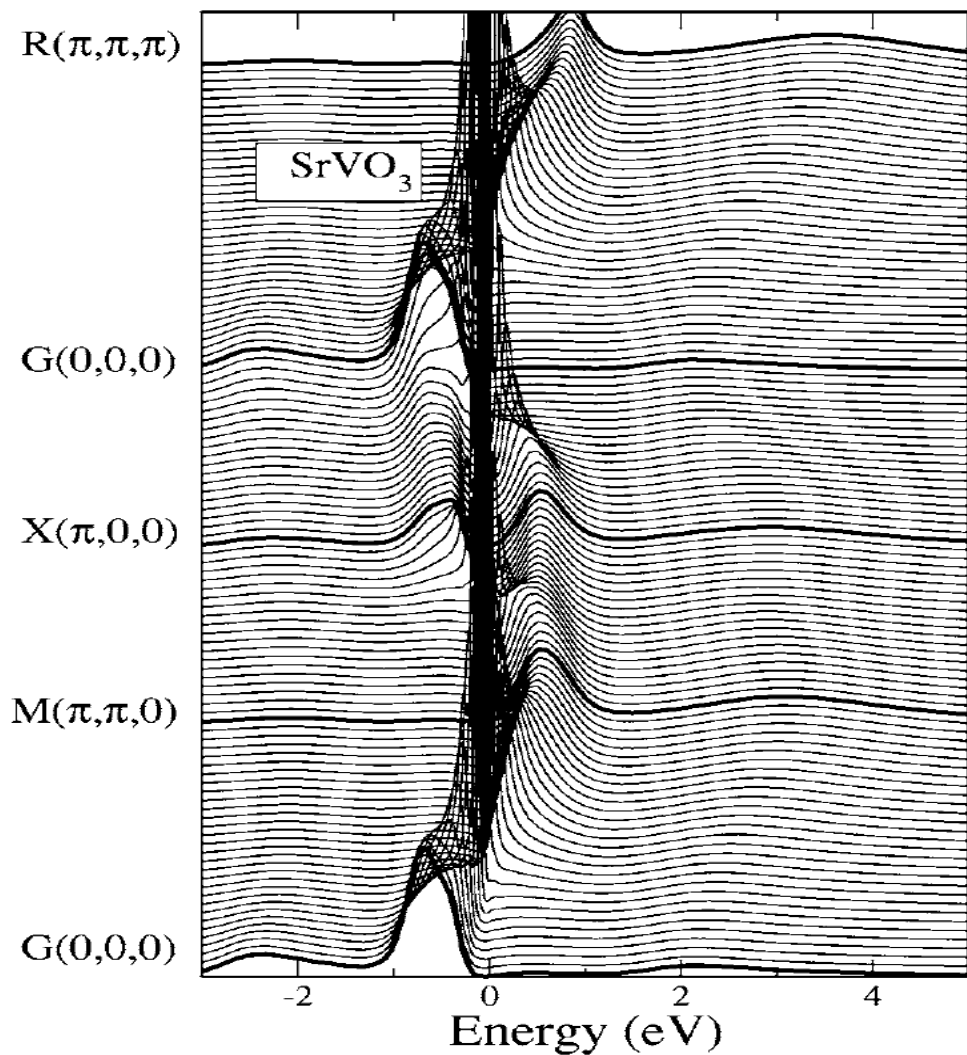
One electron in partially filled  $t_{2g}$  band

# Strongly correlated metal SrVO<sub>3</sub>



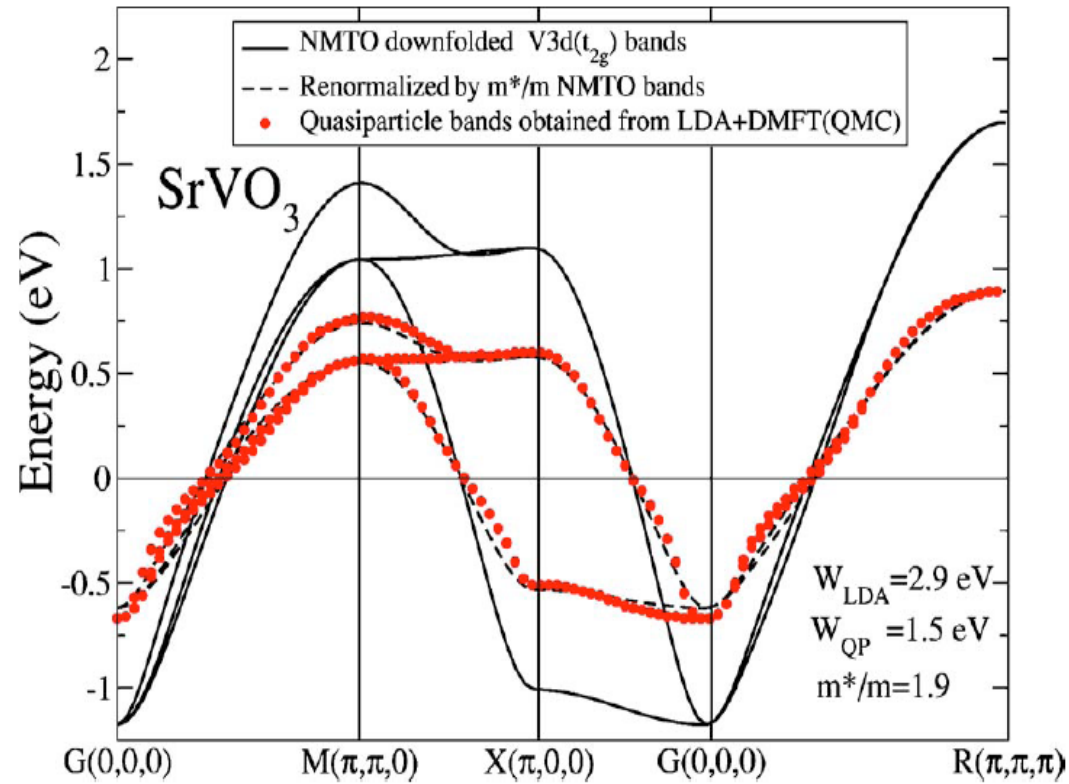
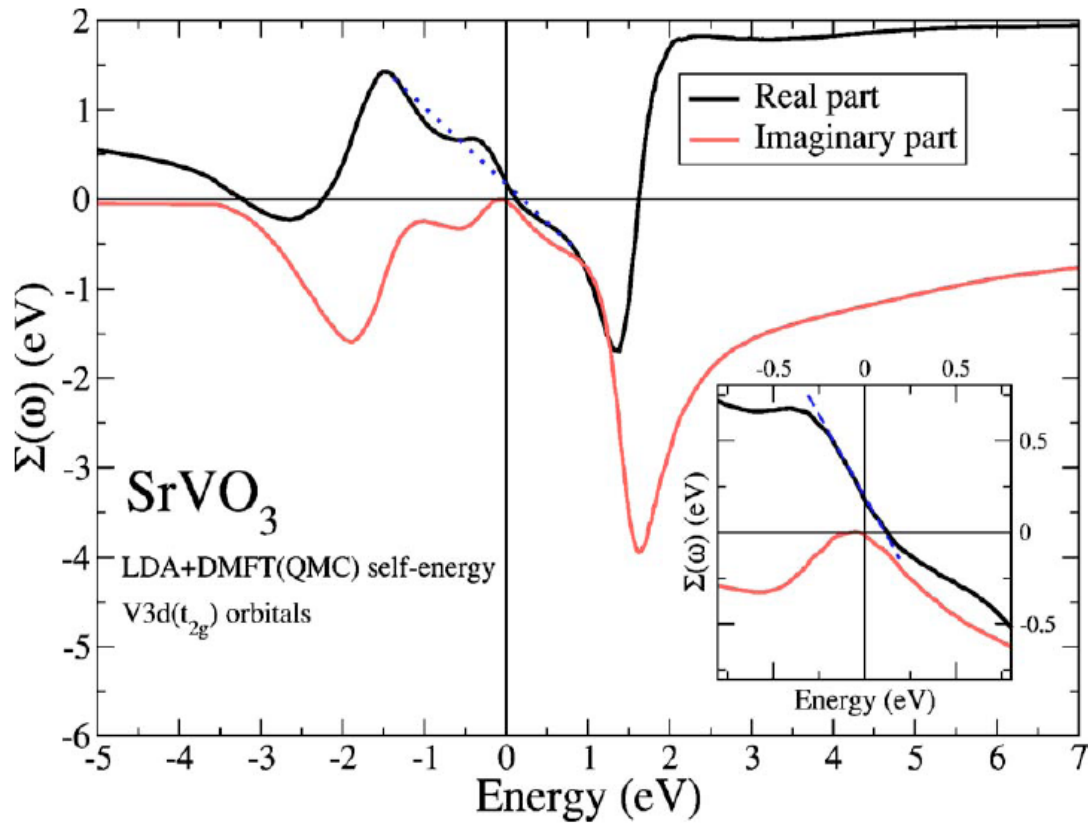
Strongly correlated metal with pronounced Lower Hubbard band (LHB)

# Strongly correlated metal SrVO<sub>3</sub>



$$\text{Spectral function } A(k, \omega) = -\frac{1}{\pi} \text{Im Tr} [\omega - \Sigma(\omega) - H_0(k)]^{-1}$$

# Strongly correlated metal SrVO<sub>3</sub>



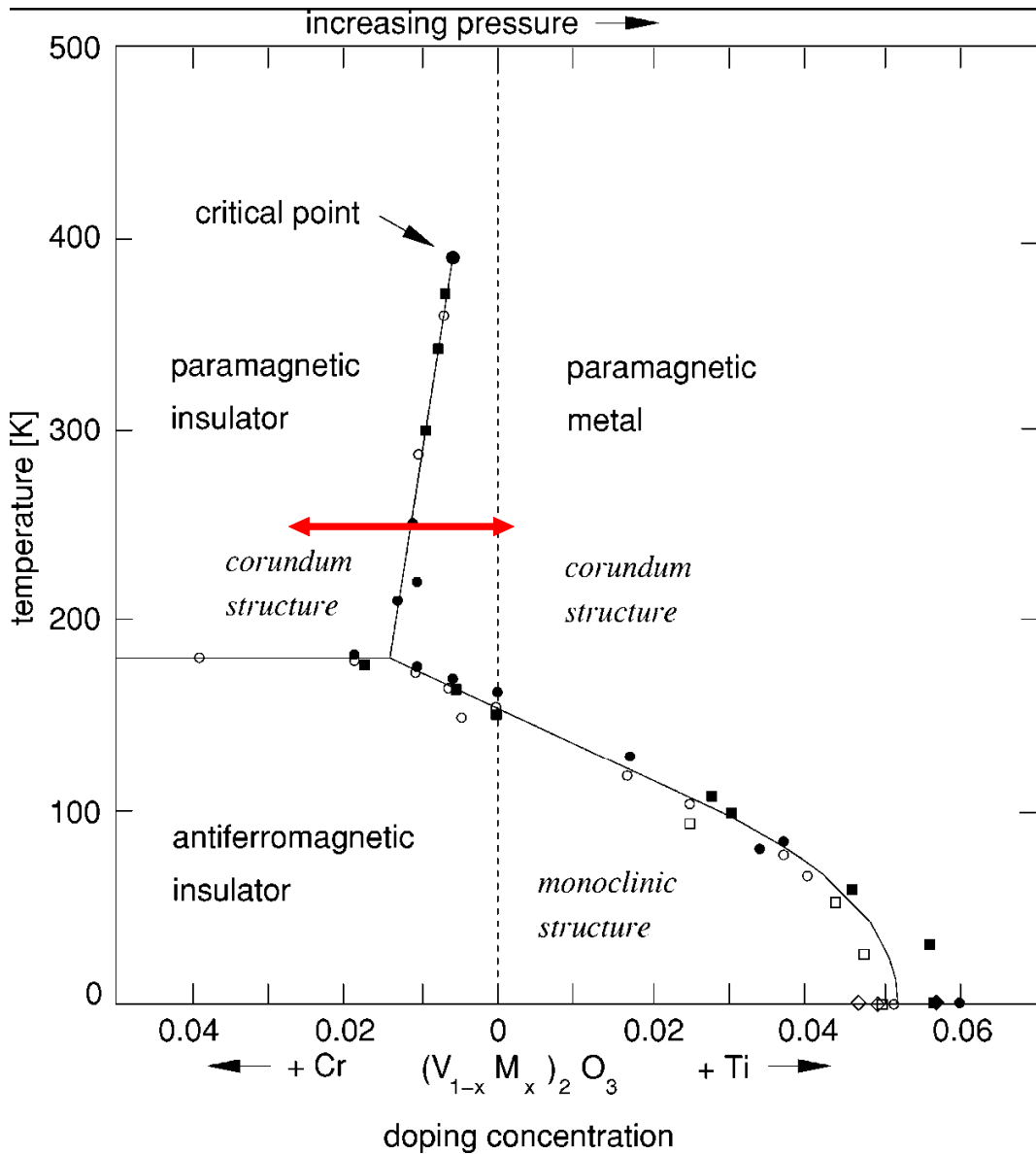
Effective electron mass

$$\frac{m^*}{m} = 1 - \frac{\partial \text{Re} \Sigma(\omega)}{\partial \omega} \Big|_{\omega=0} \approx 2$$

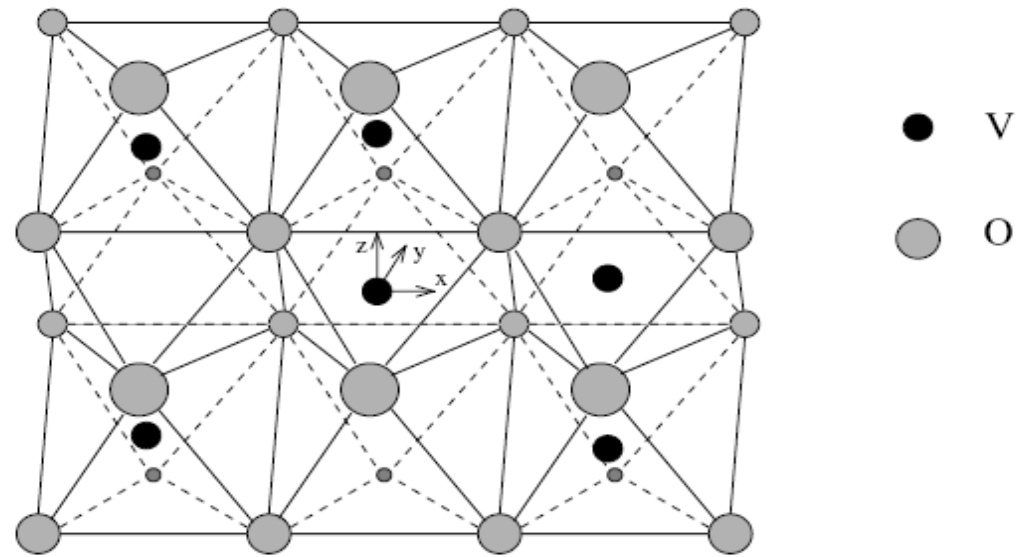
Bands narrowing

$$\tilde{\epsilon}(k) = \left( \frac{m^*}{m} \right)^{-1} \epsilon_0(k)$$

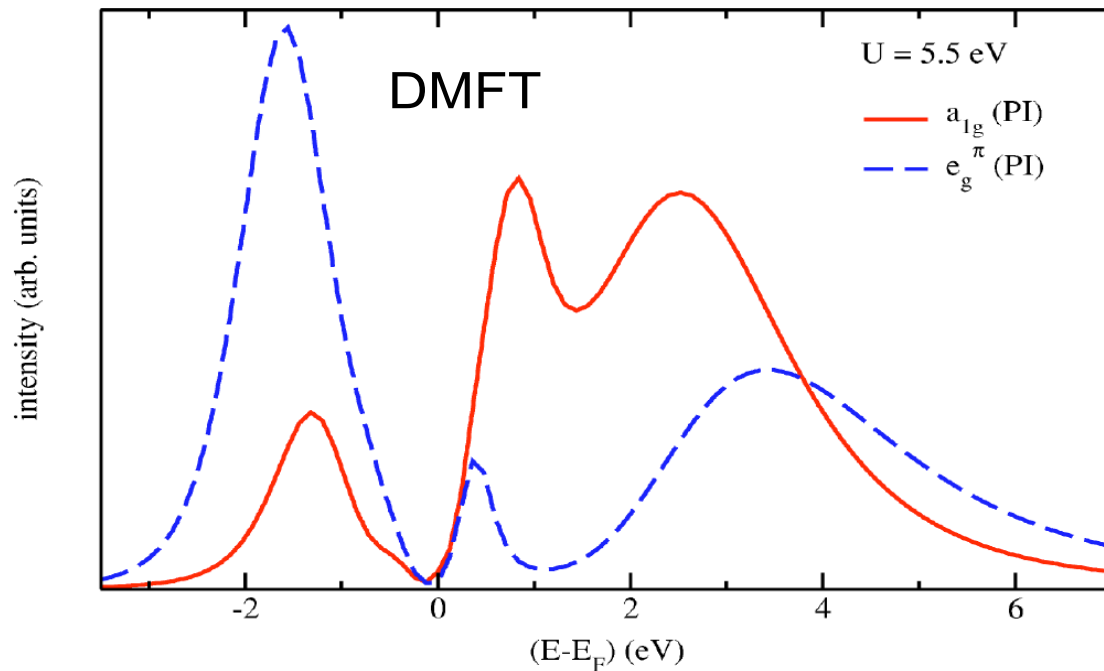
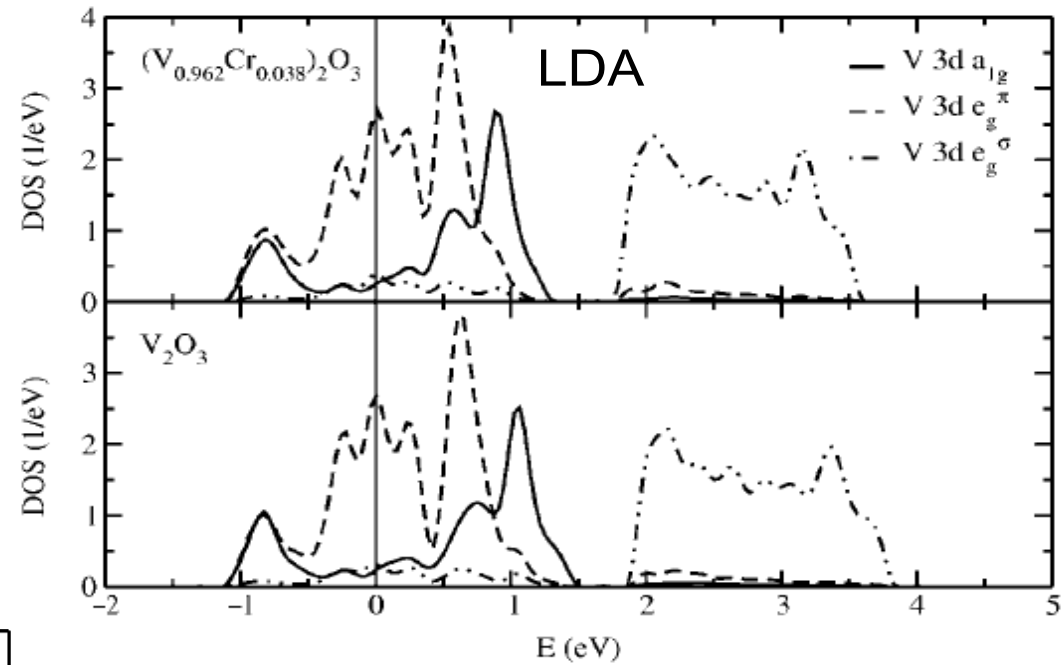
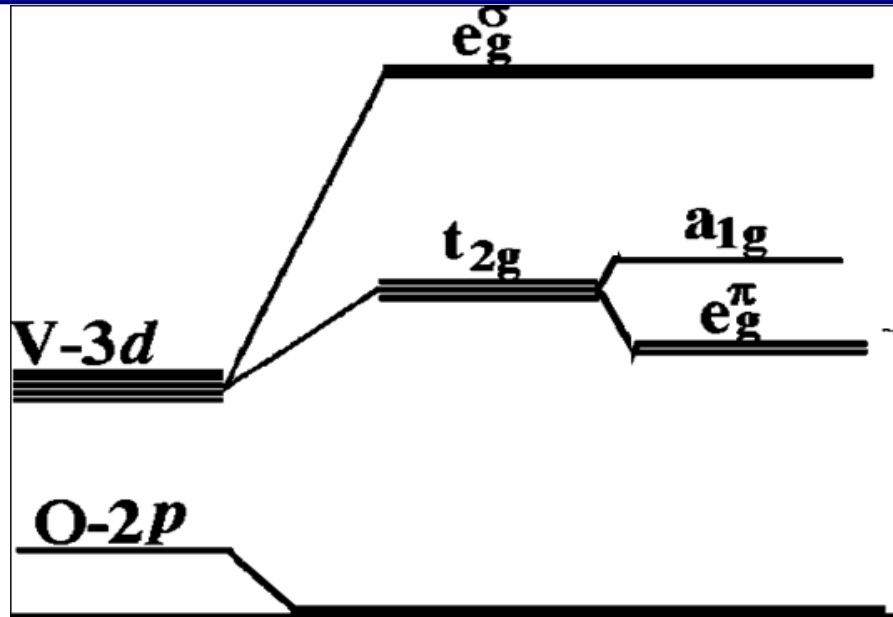
# Mott insulator $V_2O_3$



Prototypical Mott insulator.  
Iso-structural paramagnetic metal to  
paramagnetic insulator transition  
with small volume change due to  
chemical negative pressure.



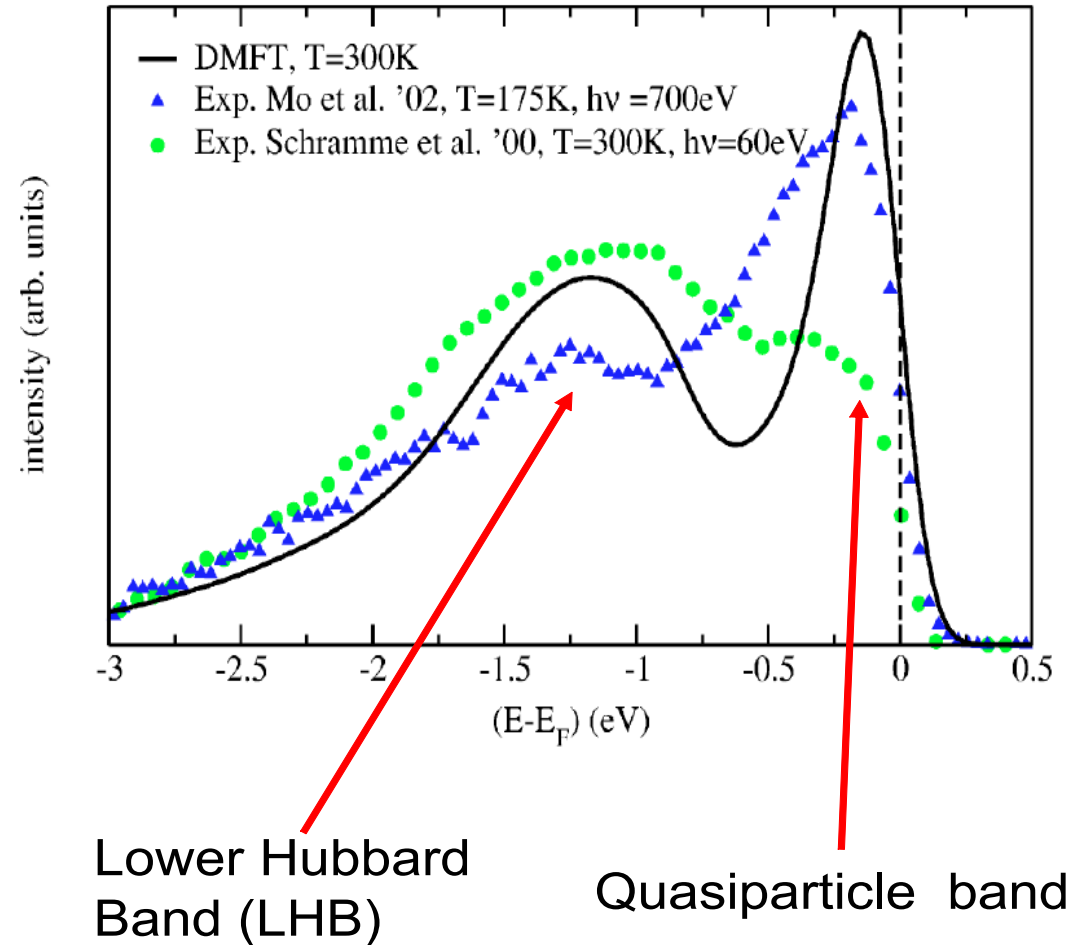
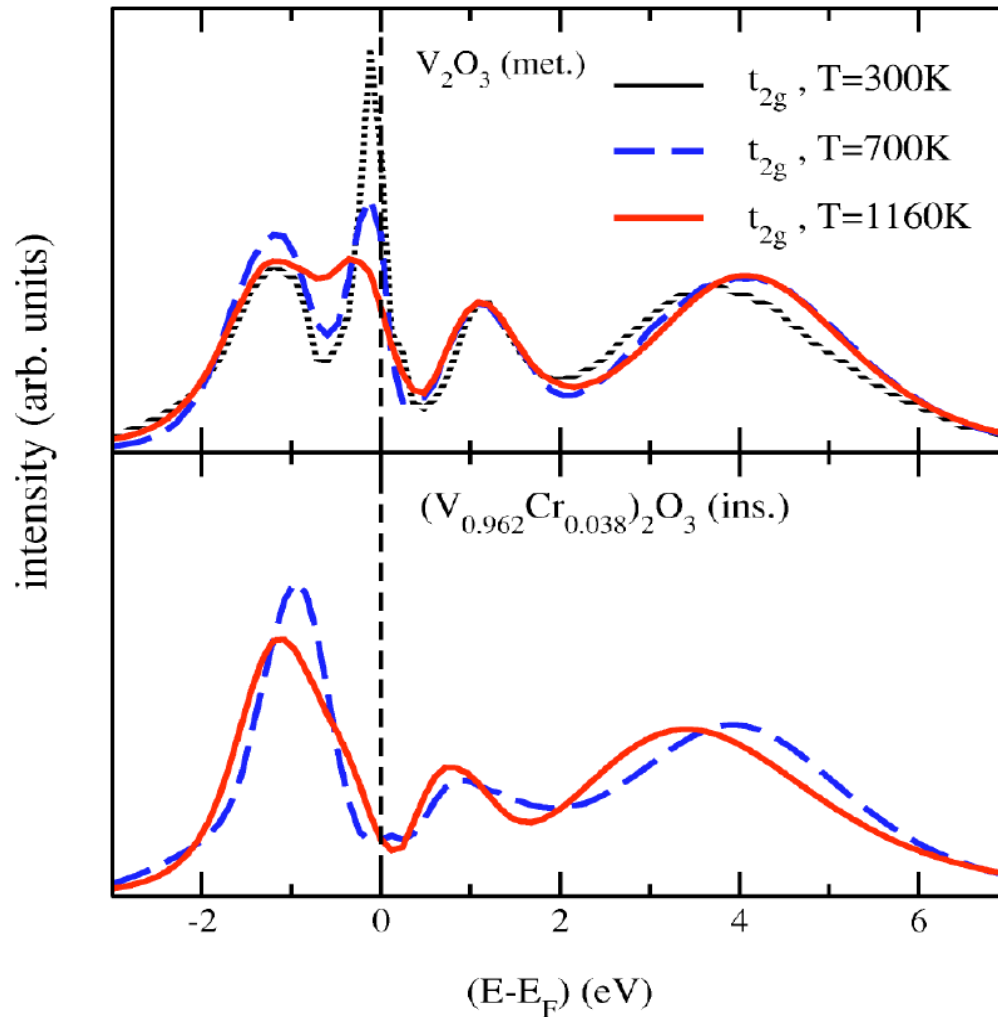
# Mott insulator $V_2O_3$



$V^{+3}$  ( $d^2$ ) ion in trigonal symmetry corundum crystal structure.  
 Two electrons in  $t_{2g}$  band ( $W \sim 2.5$  eV).  
 Trigonal crystal field splitting  $\sim 0.3$  eV leads to orbital polarization in DMFT



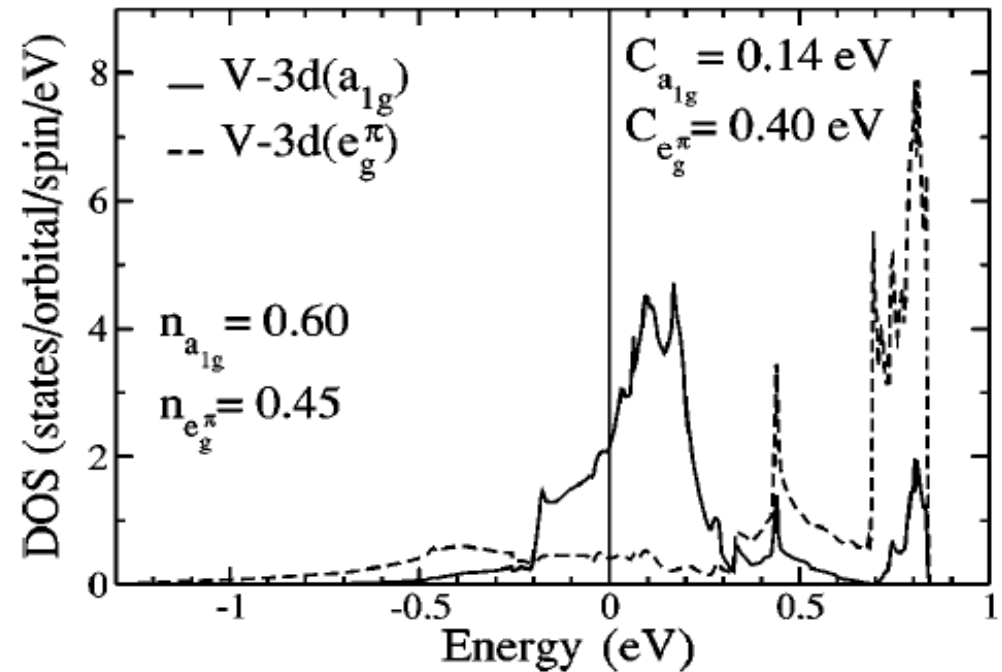
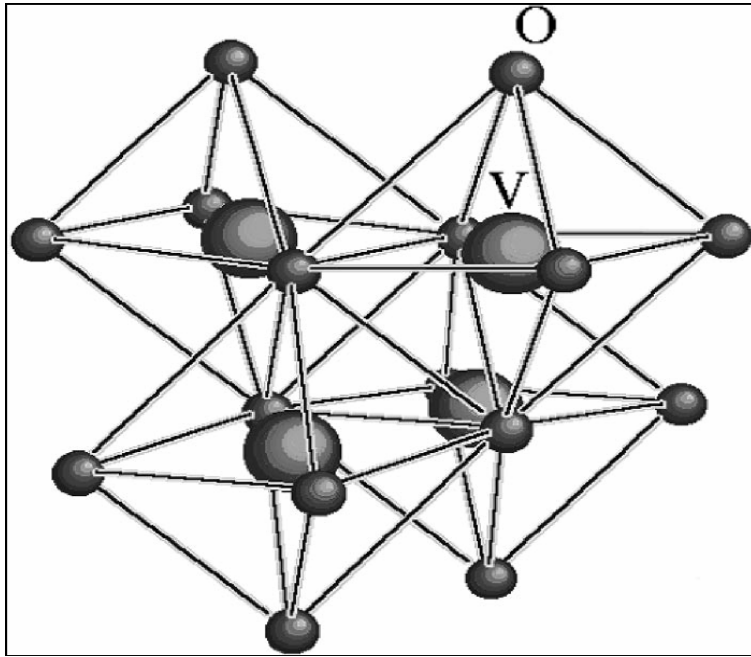
# Mott insulator $V_2O_3$



Paramagnetic metal to paramagnetic insulator transition with small change in corundum crystal structure parameters

K.Held et al, Phys. Rev. Lett. 86, 5345 (2001), G.Keller et al, Phys. Rev. B 70, 205116 (2004)

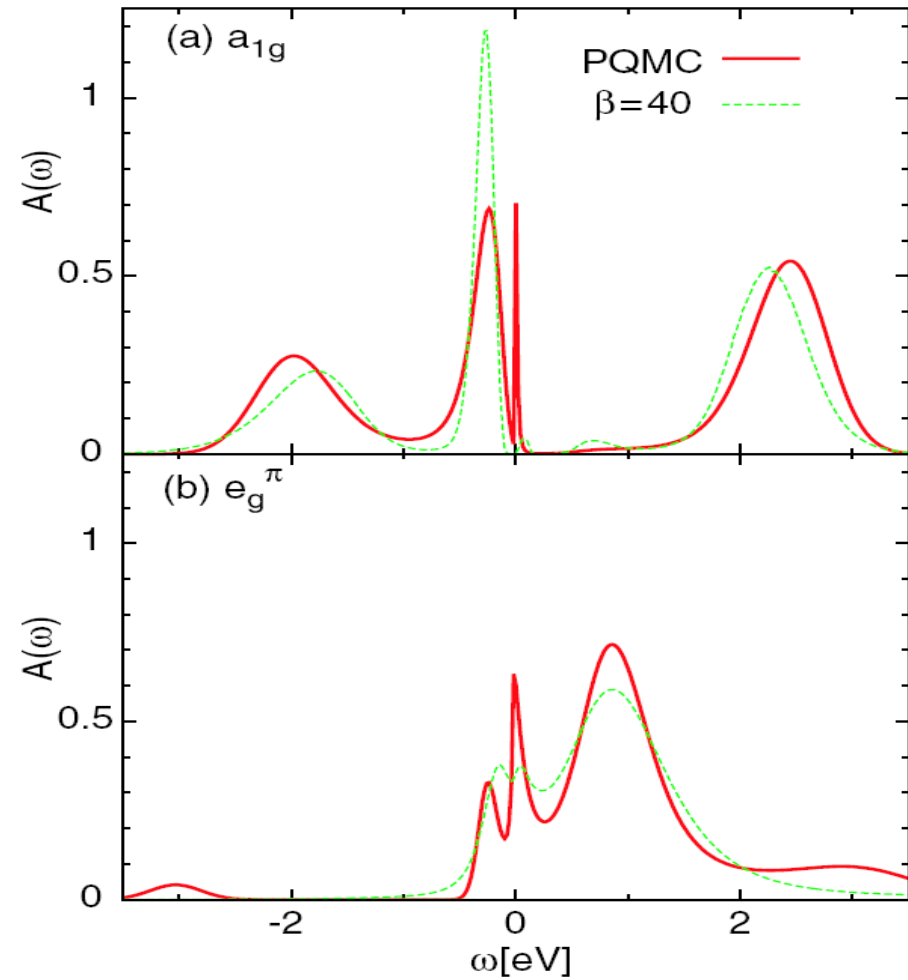
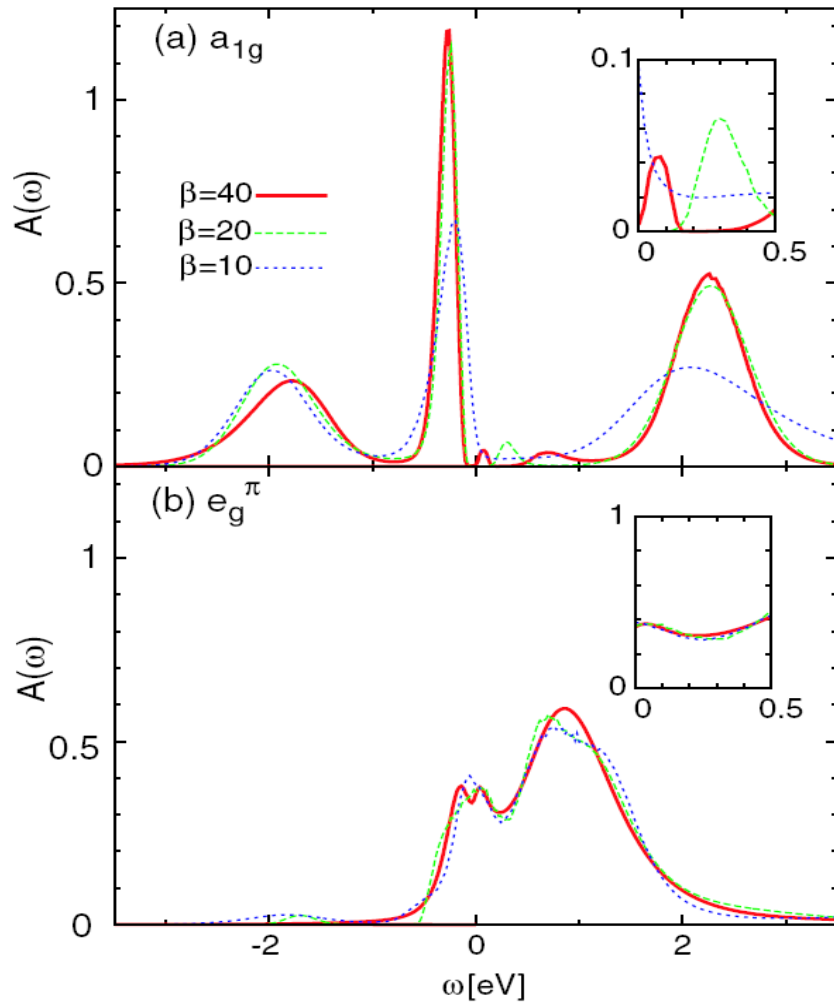
# Heavy fermions material $\text{LiV}_2\text{O}_4$



Heavy-fermions without f-electrons:  
linear specific heat coefficient  
 $\gamma = 420 \text{ mJ/molK}^2$ ,  
effective electron mass  $m^*/m = 25$   
below  $T_K \sim 28 \text{ K}$

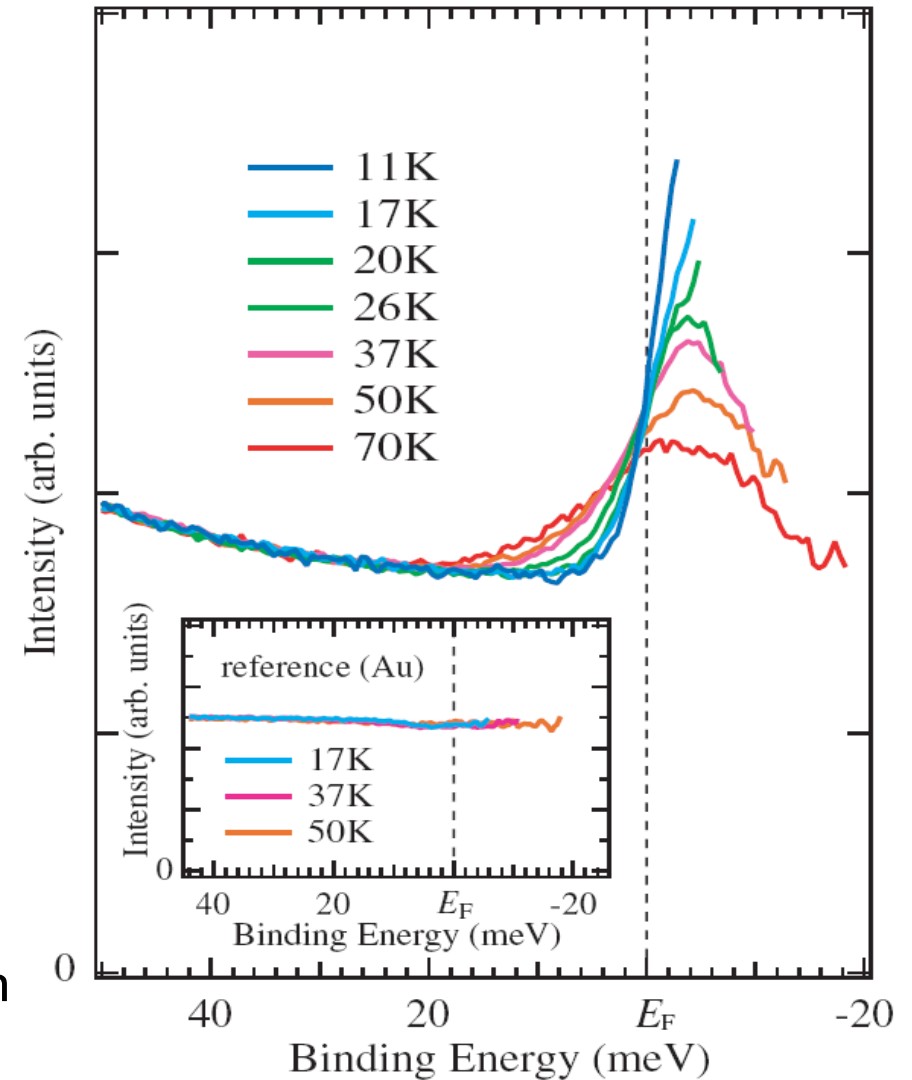
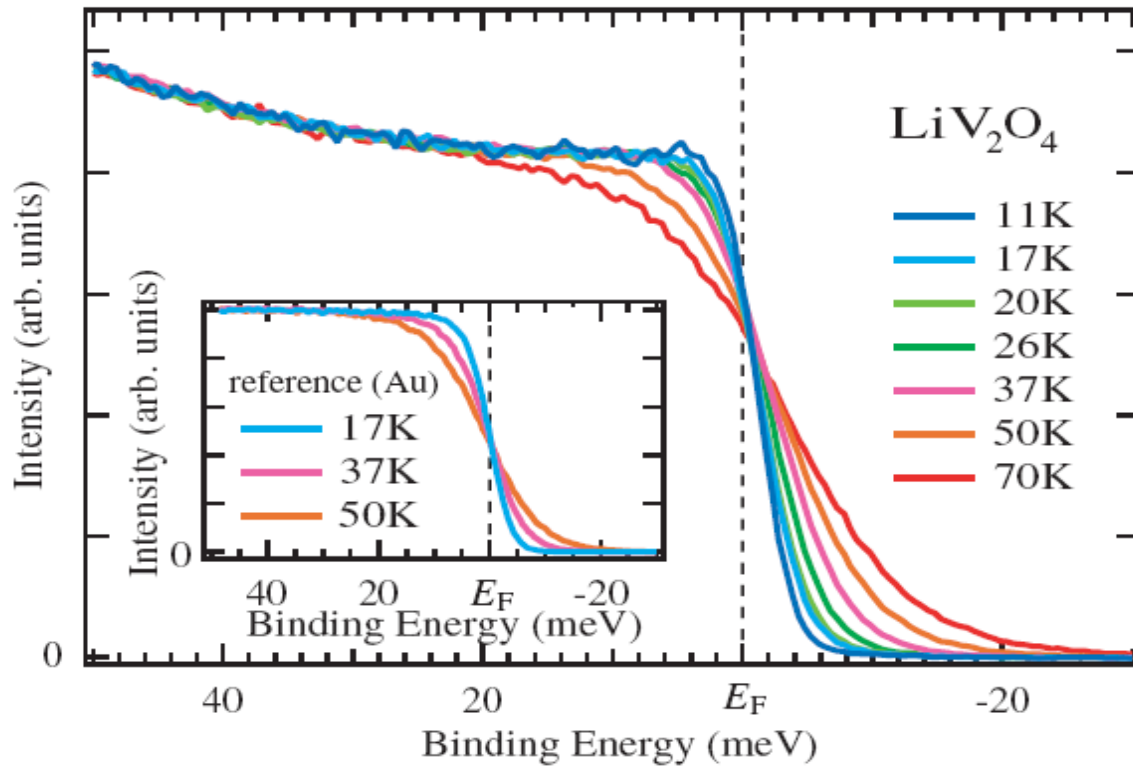
Cubic spinel crystal structure  
with local trigonal symmetry

# Heavy fermions material $\text{LiV}_2\text{O}_4$



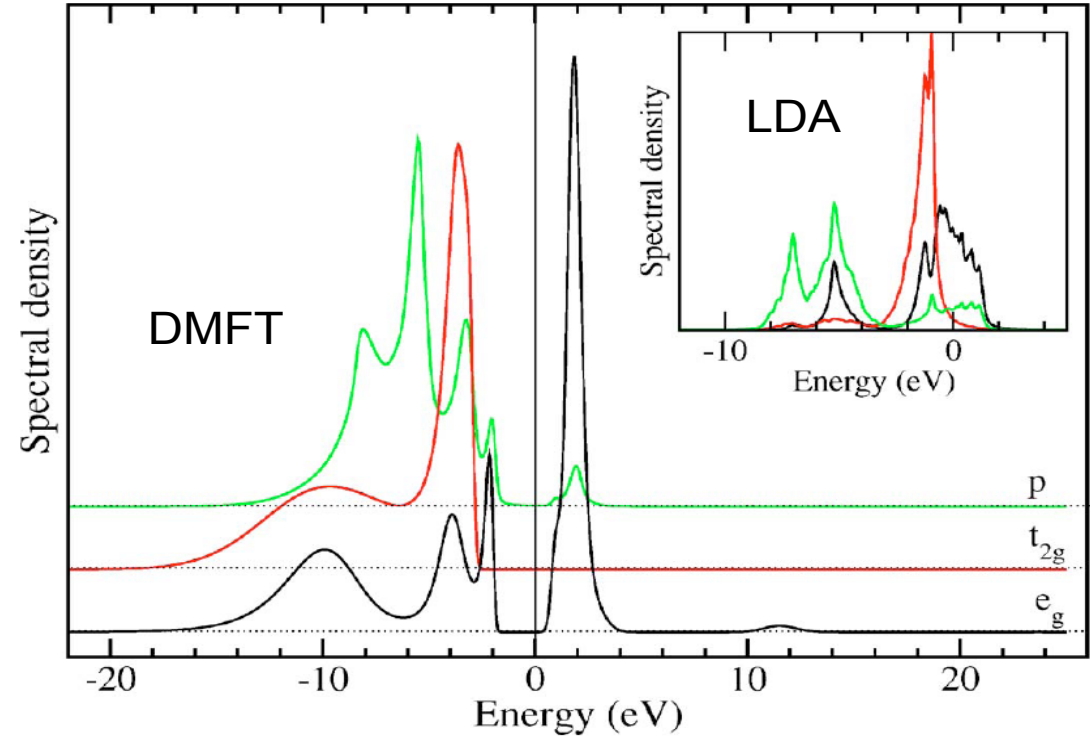
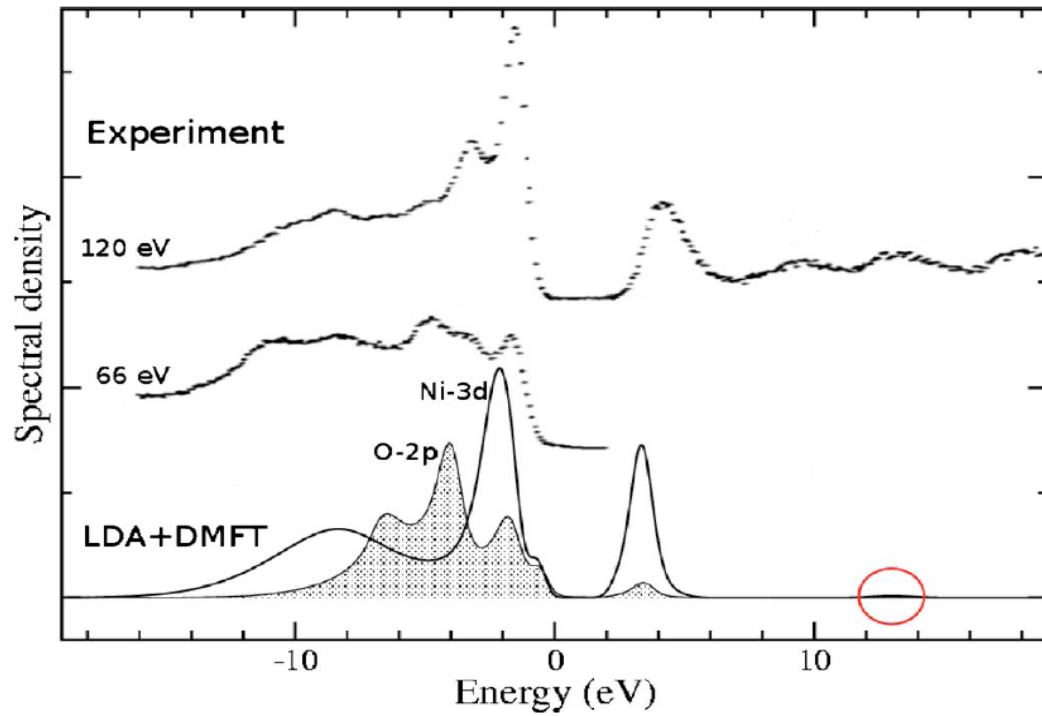
Sharp quasiparticle peak above the Fermi for  $T=0$  limit (PQMC)

# Heavy fermions material $\text{LiV}_2\text{O}_4$



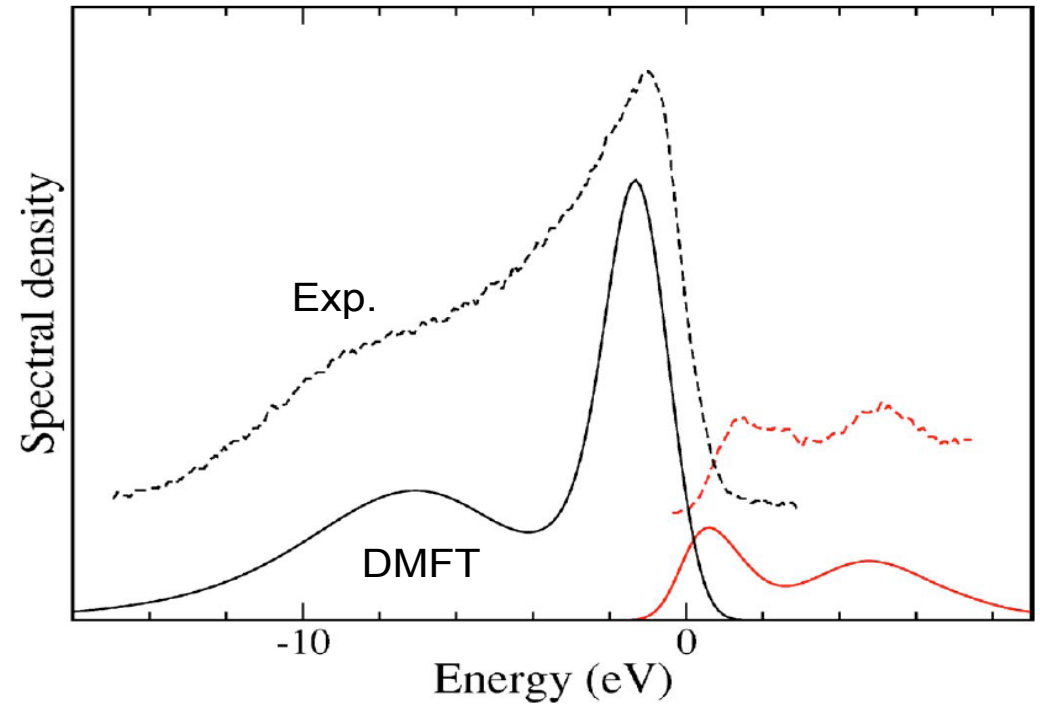
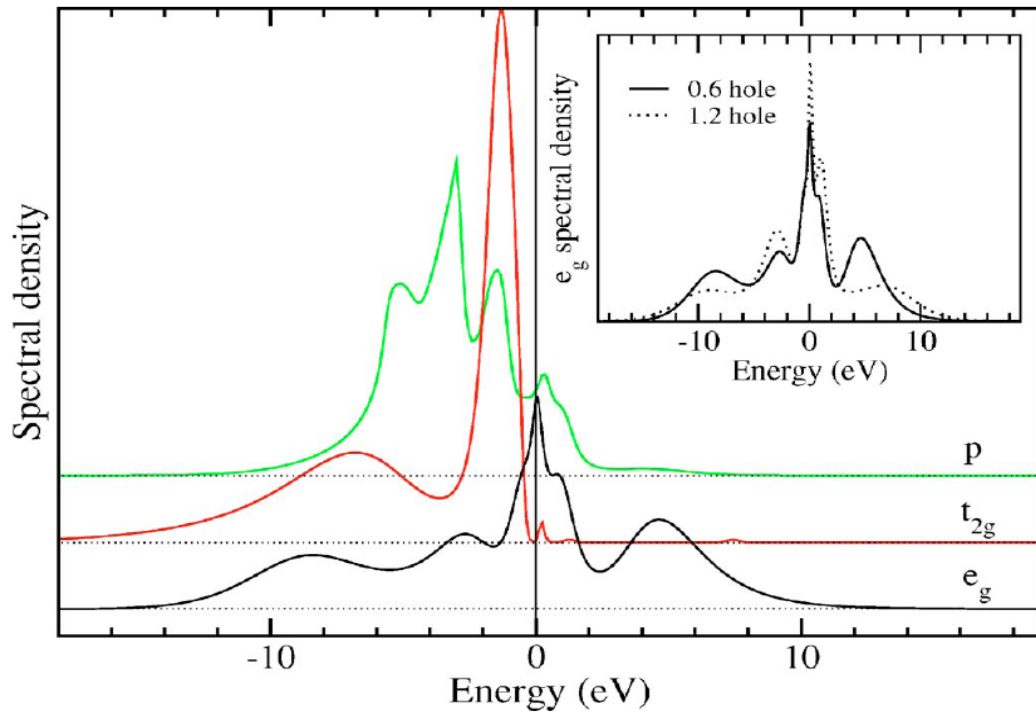
XPS => Quasiparticle peak 10 meV width  
4 meV above the Fermi

# Charge transfer insulator NiO



Charge transfer insulator in paramagnetic phase.  
 $\text{Ni}^{+2}$  ( $d^8$ ) ion in cubic rock salt crystal structure

# Charge transfer insulator NiO

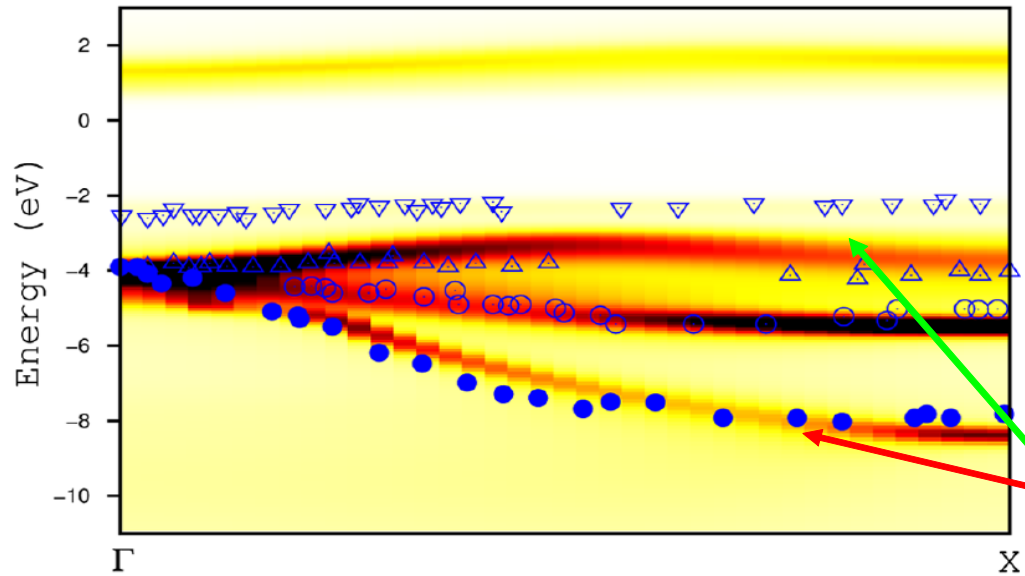


$\text{Li}_x\text{Ni}_{1-x}\text{O}$  spectra

$n_h$	$n_{e_g}$	$n_{t_{2g}}$	$n_p$	$m_d$
0	0.547	1.000	0.969	1.85
0.6	0.531	0.994	0.885	1.61
1.2	0.530	0.980	0.800	1.45

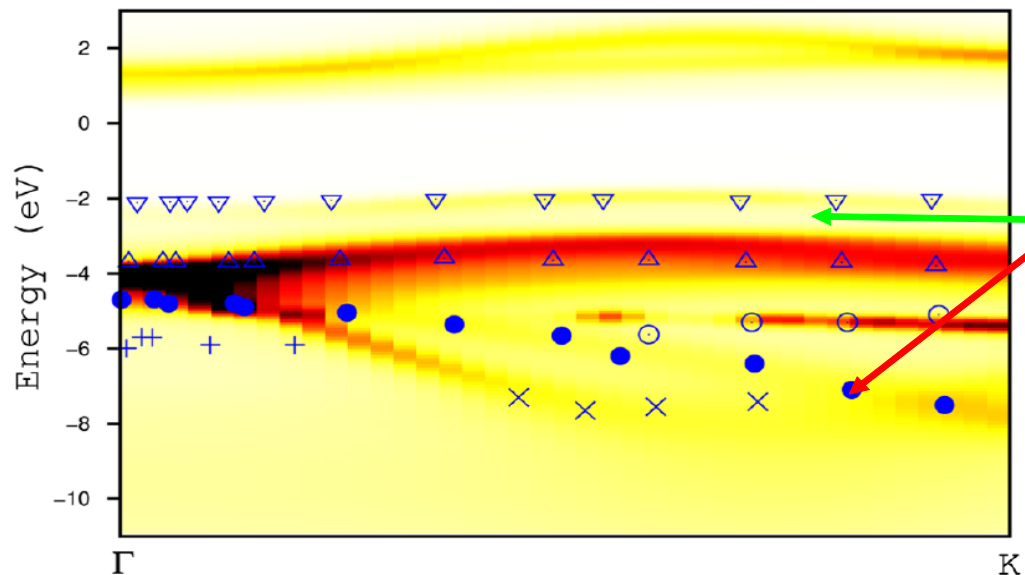
Holes in charge transfer insulator have predominantly oxygen 2p character.

# Charge transfer insulator NiO



Band structure of charge transfer insulator combines dispersive (itinerant states) and flat bands (localized states).

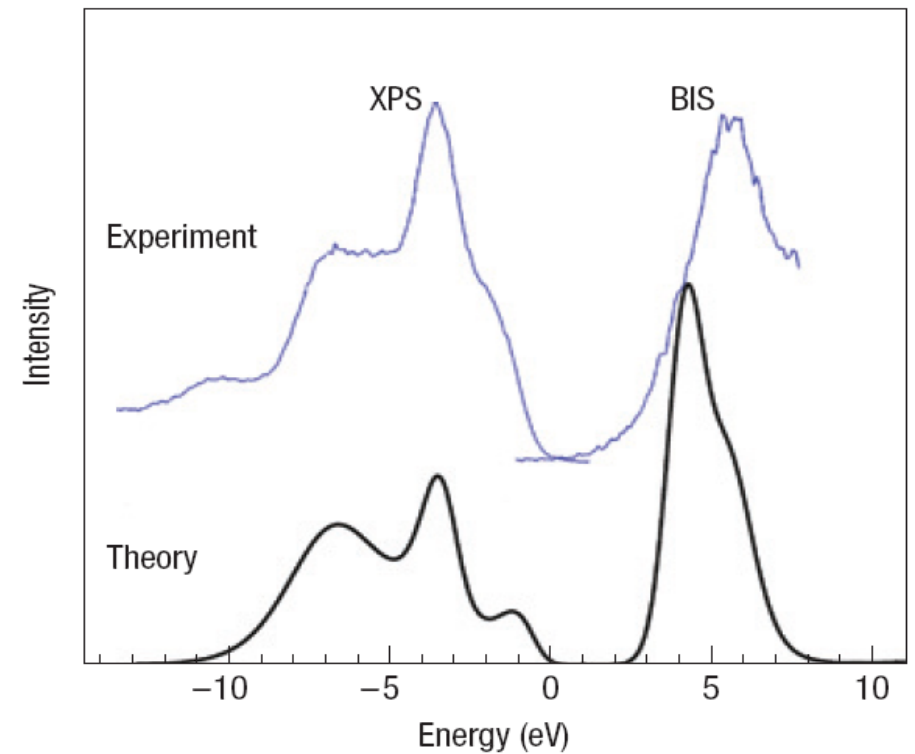
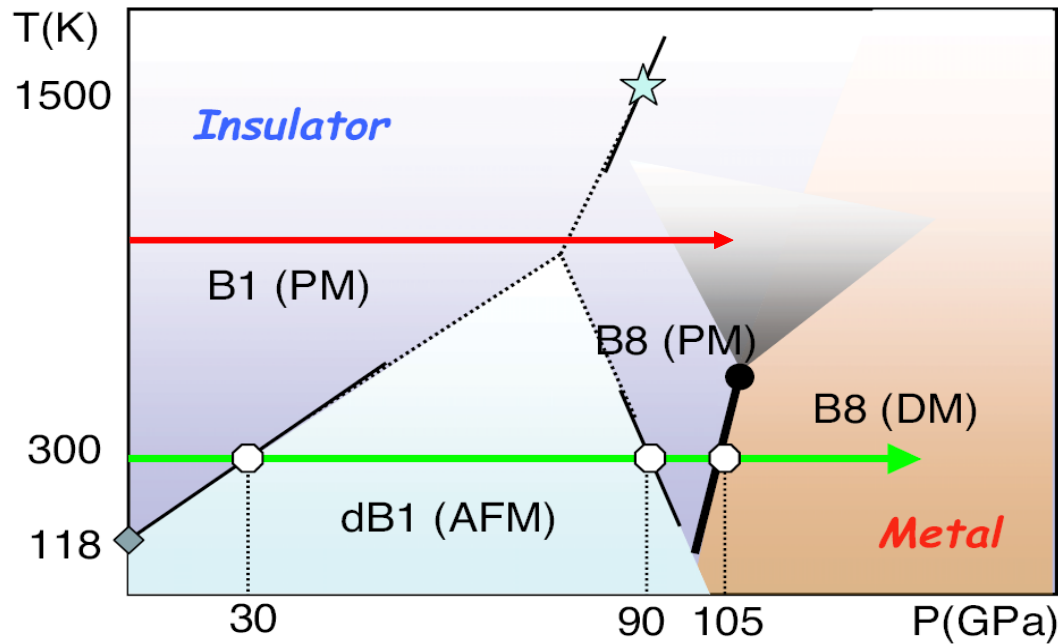
O2p bands



Ni3d bands

J. Kunes et al, Phys. Rev. Lett. 99, 156404 (2007)

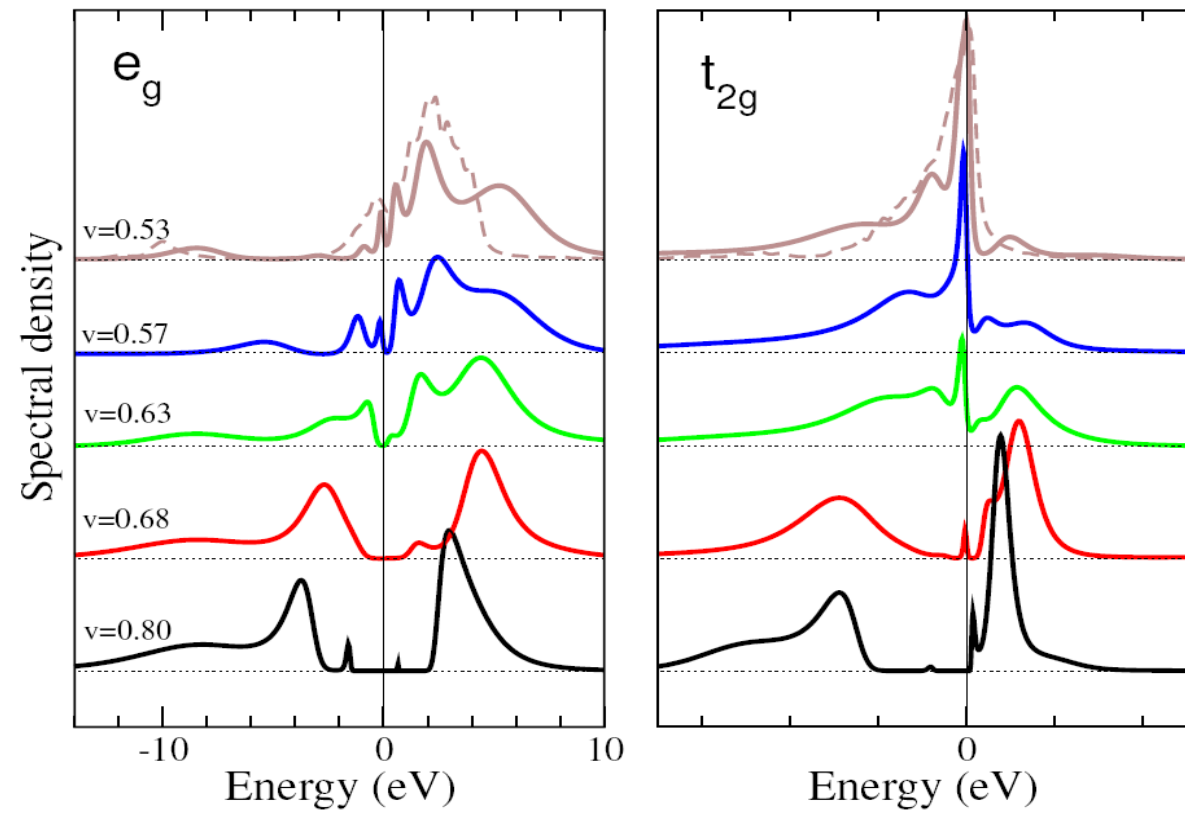
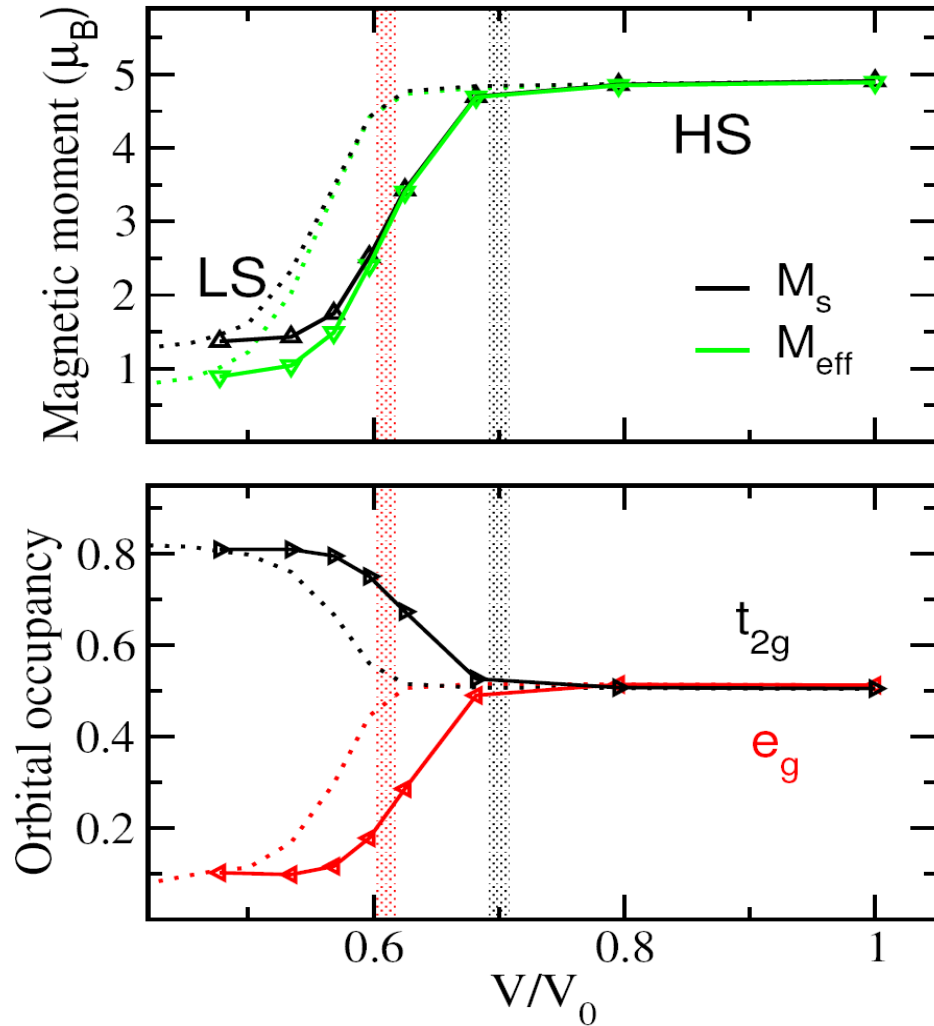
# Metal-insulator transition in MnO



Metal-insulator transition (paramagnetic insulator to paramagnetic metal) with pressure in MnO accompanied with high-spin to low-spin state transition.



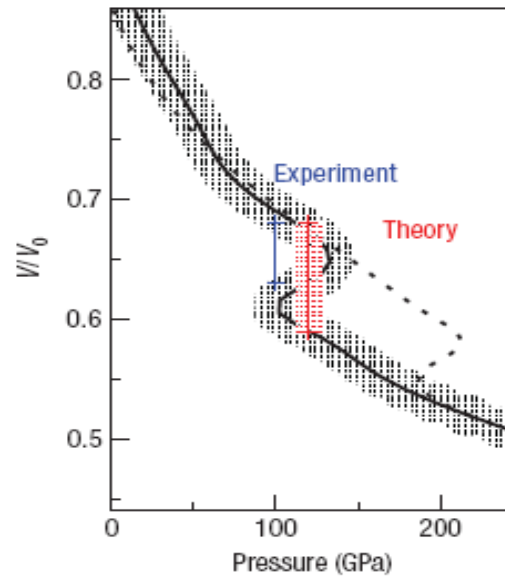
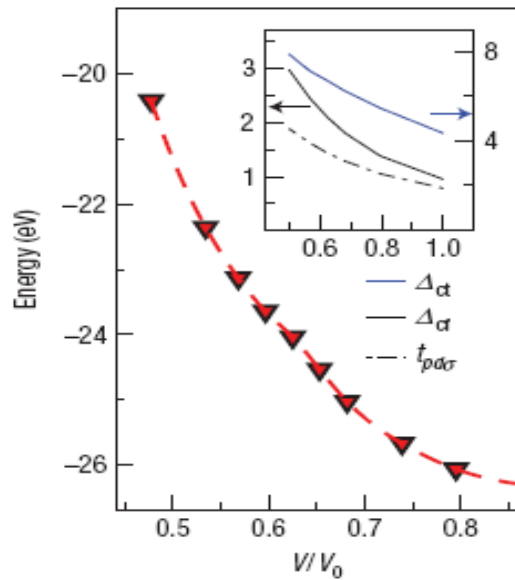
# Metal-insulator transition in MnO



High-spin state (HS) -  $t^3_{2g} e^2_g$  configuration

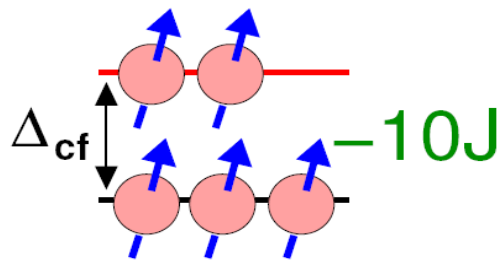
Low-spin state (LS) -  $t^5_{2g} e^0_g$  configuration

# Metal-insulator transition in MnO

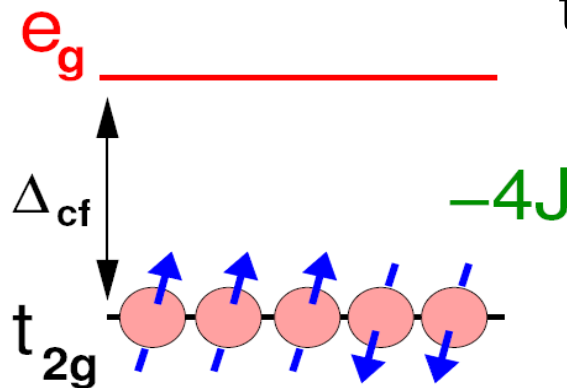


Decreasing volume with pressure increases crystal field splitting  $\Delta_{cf}$  competing with exchange energy  $J$  that results in HS  $\rightarrow$  LS transition with volume collapse.

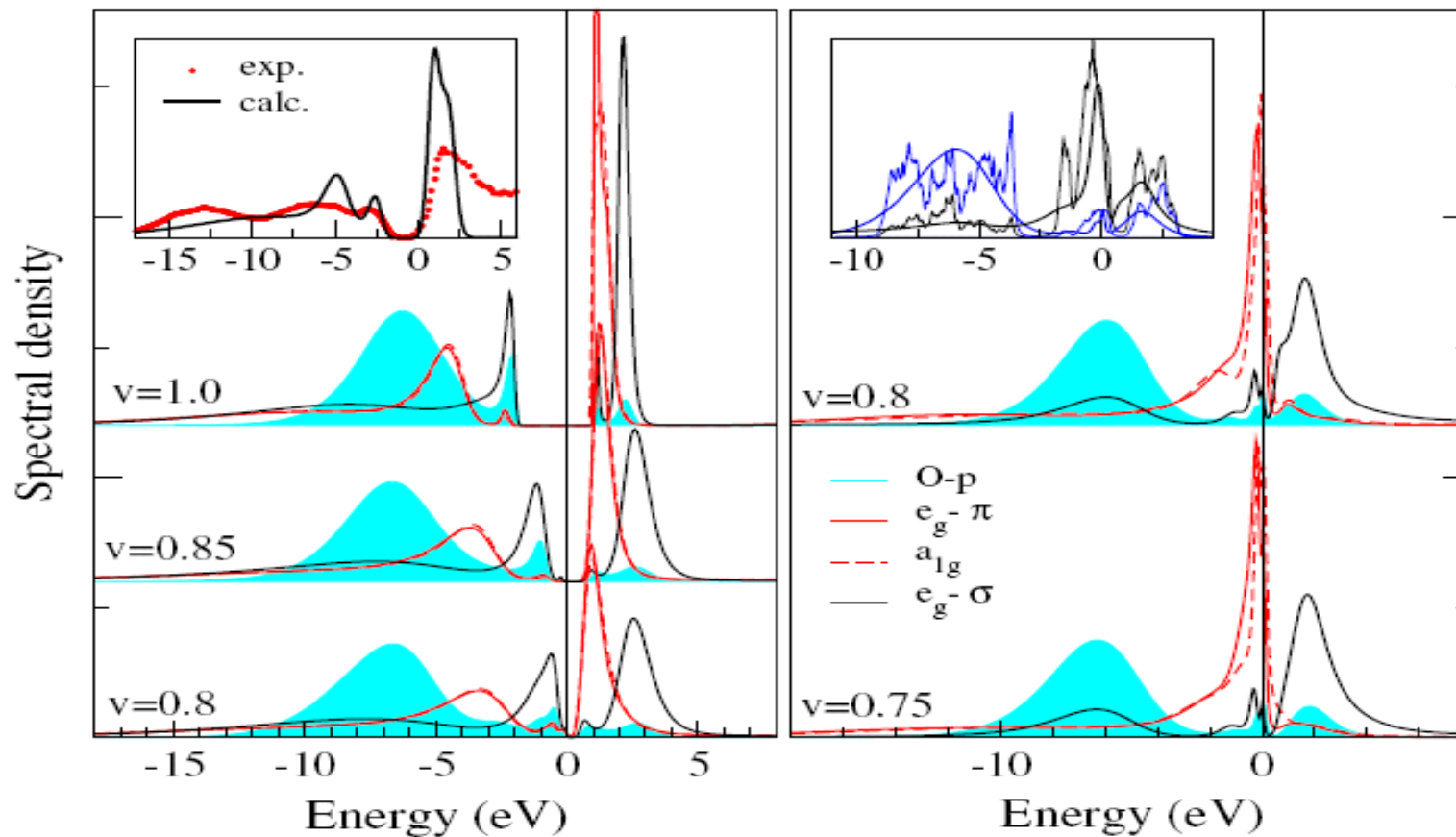
HS



LS

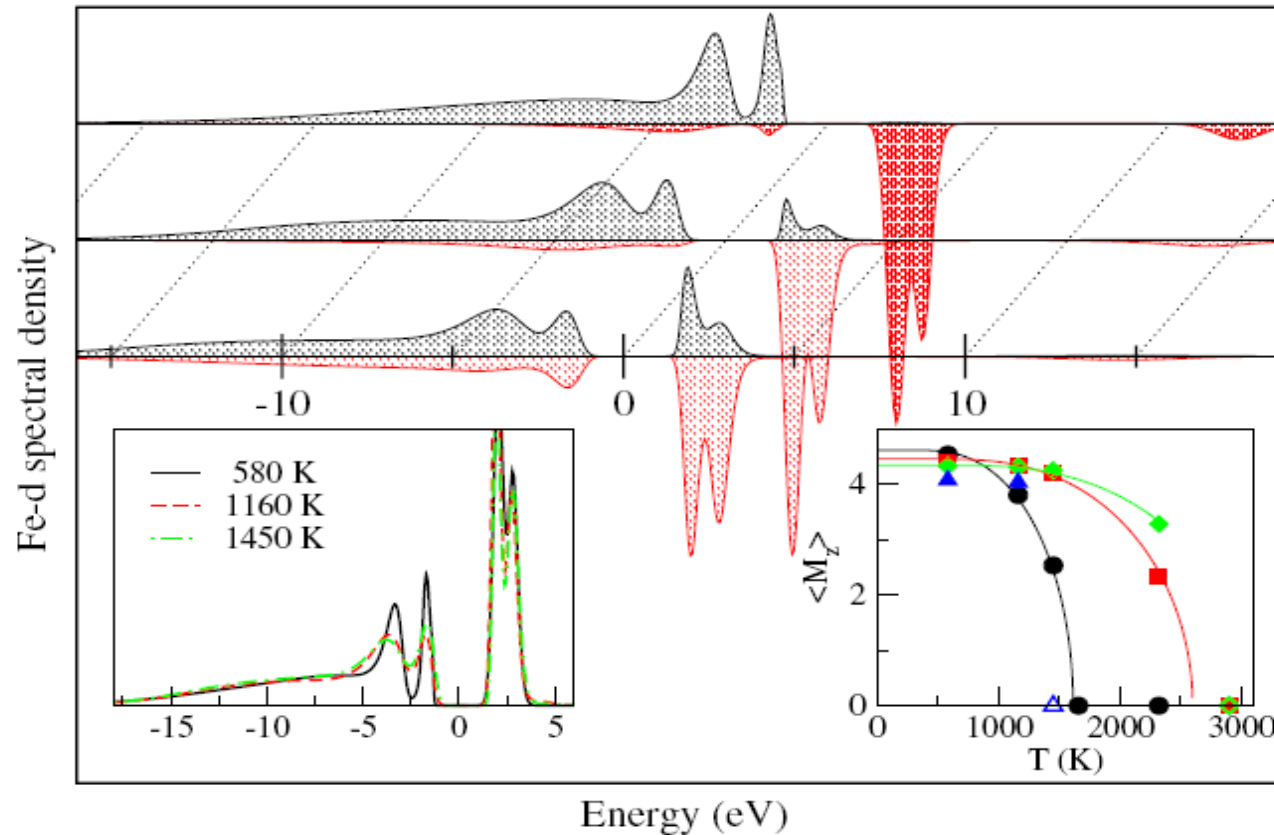


# Metal-insulator transition in $\text{Fe}_2\text{O}_3$



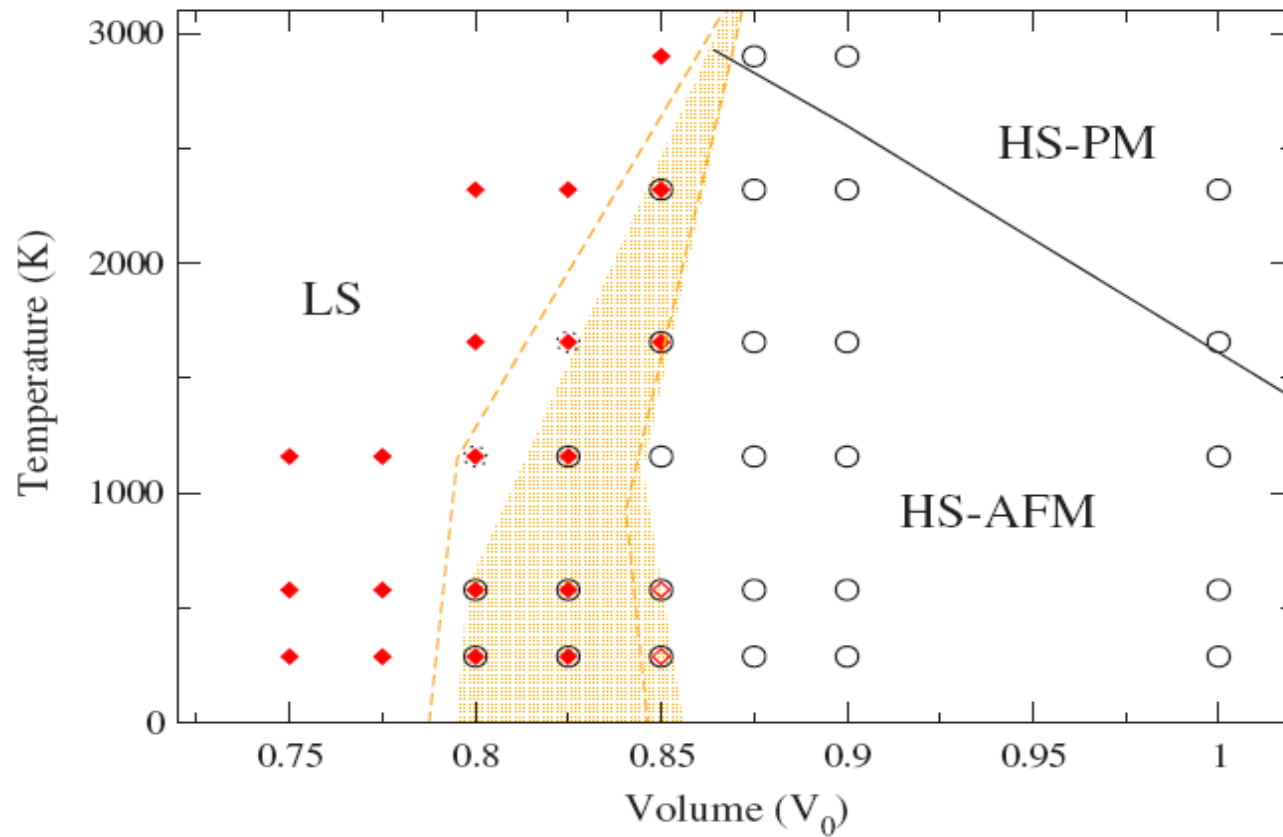
Evolution of the paramagnetic state single-particle spectra with pressure (T = 580 K).

# Metal-insulator transition in $\text{Fe}_2\text{O}_3$



Spin-polarized Fe-d spectra at the ambient pressure for 580, 1160, and 1450 K (top to bottom). Left-hand inset: The same spectra averaged over spin. Right-hand inset: The staggered magnetization versus temperature curves for various volumes.

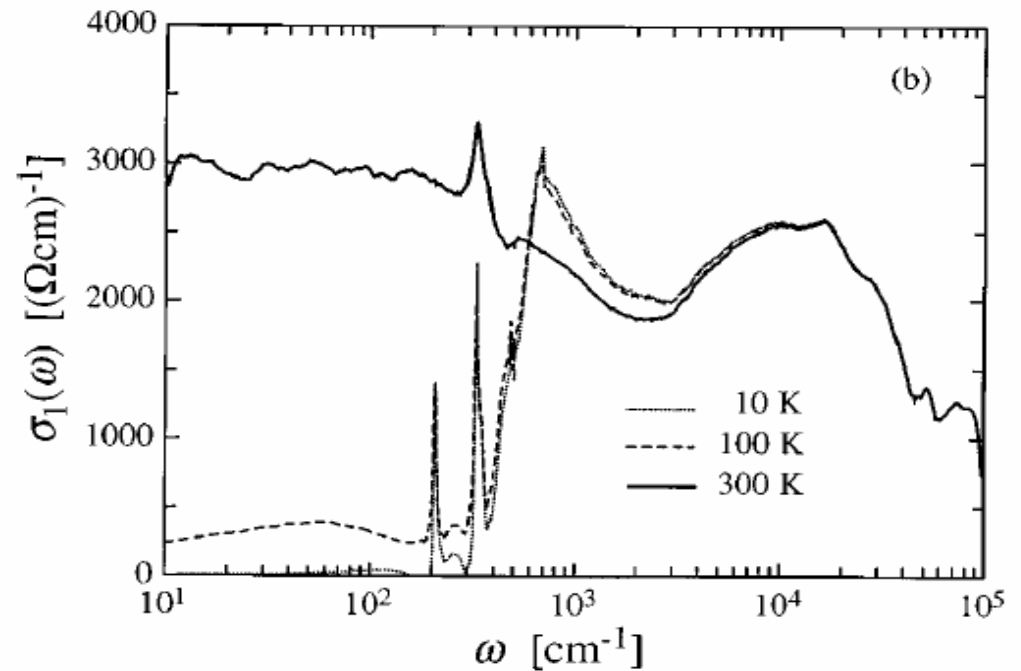
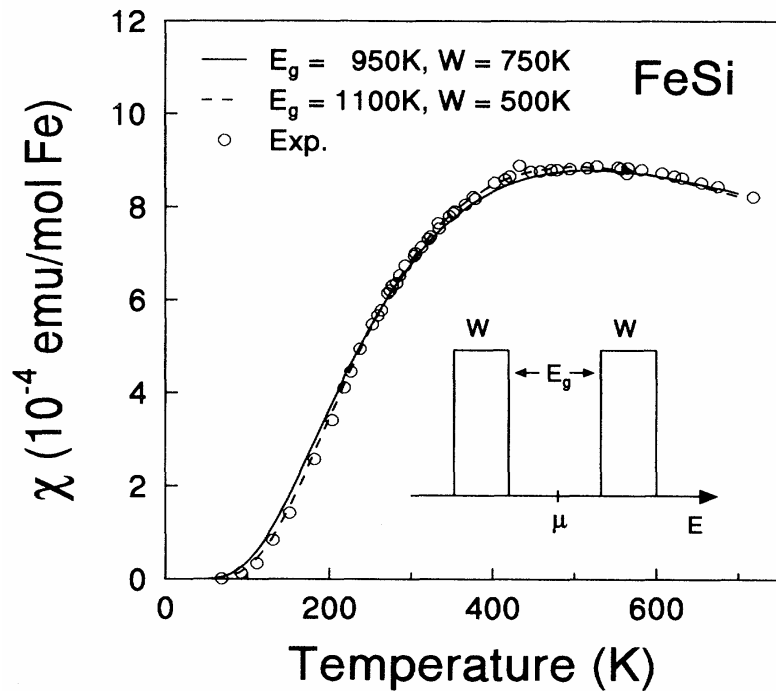
# Metal-insulator transition in $\text{Fe}_2\text{O}_3$



Calculated  $V$ - $T$  phase diagram of hematite.

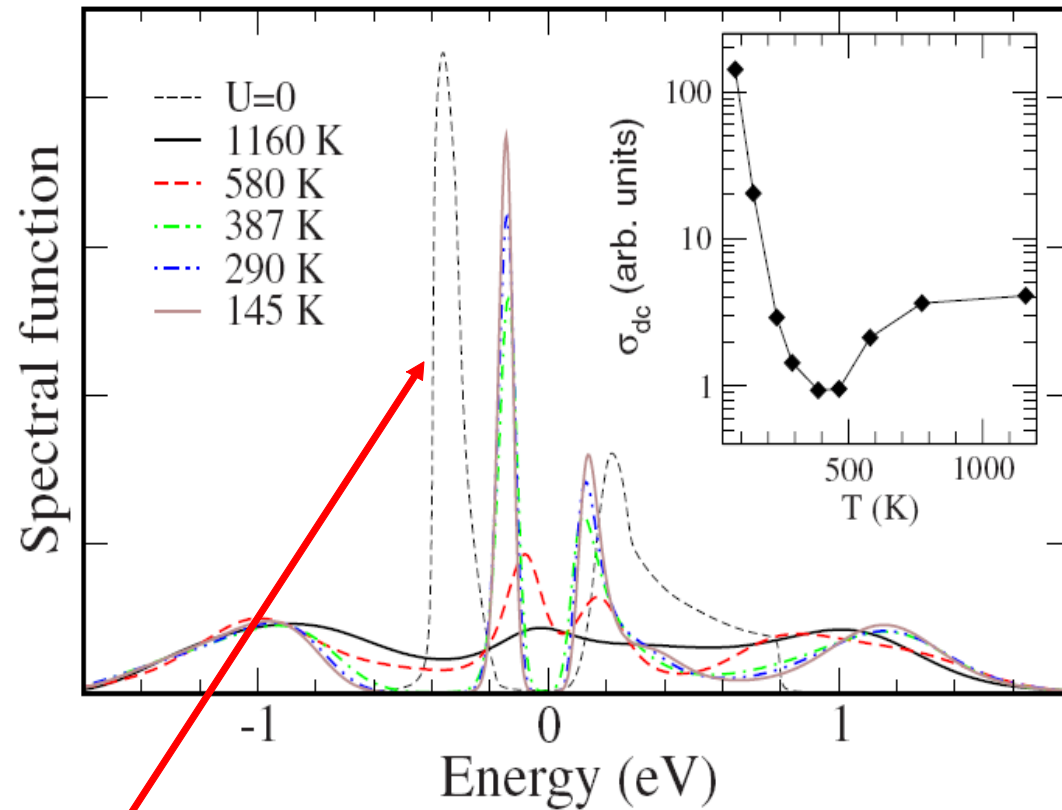
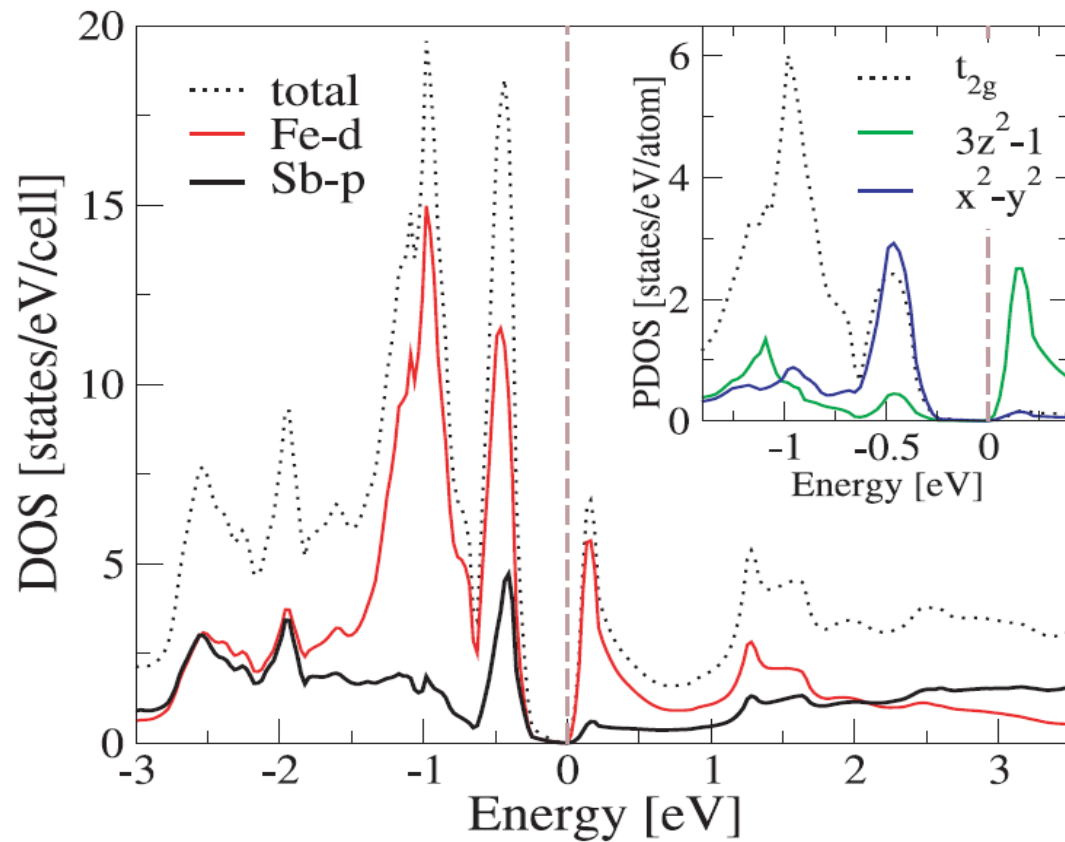
J. Kunes et al, PRL 102, 146402 (2009)

# Correlated covalent insulators FeSi and FeSb<sub>2</sub>



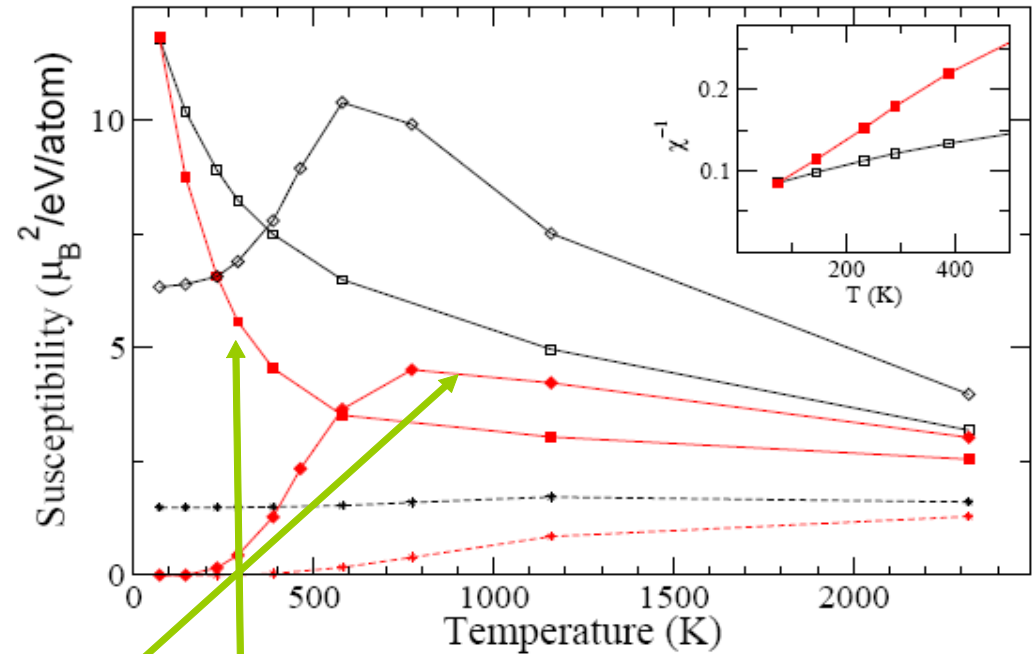
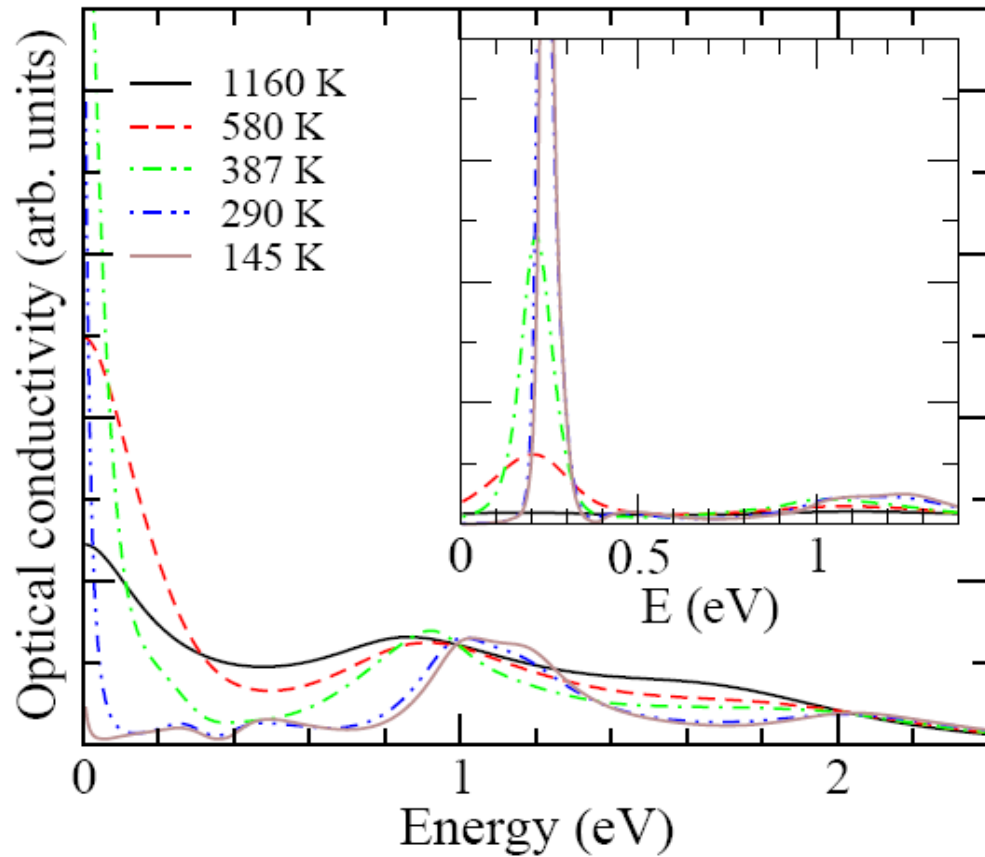
Transition from non-magnetic semiconductor to paramagnetic metal with temperature increase in FeSi and FeSb<sub>2</sub>. Electron doping in Fe<sub>1-x</sub>Co<sub>x</sub>Si results in ferromagnetic metallic state.

# Correlated covalent insulators FeSi and FeSb<sub>2</sub>



Effective one-orbital per Fe ion model corresponding to covalent insulator

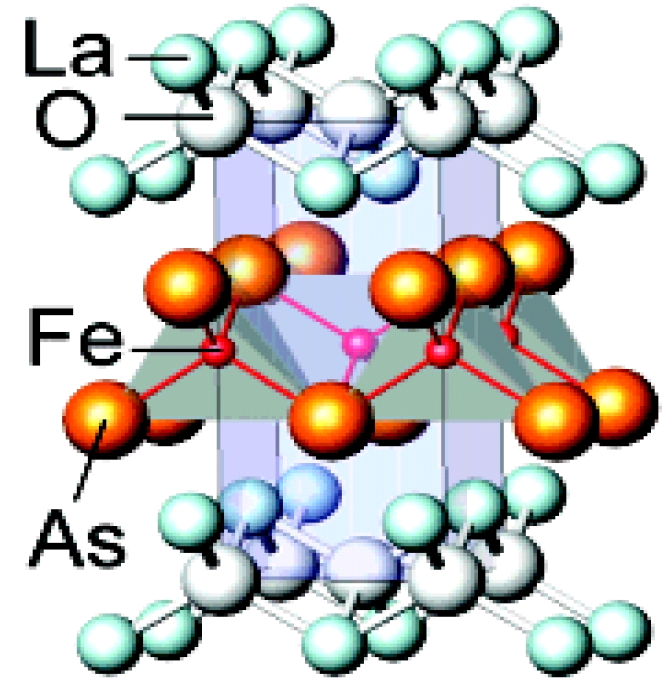
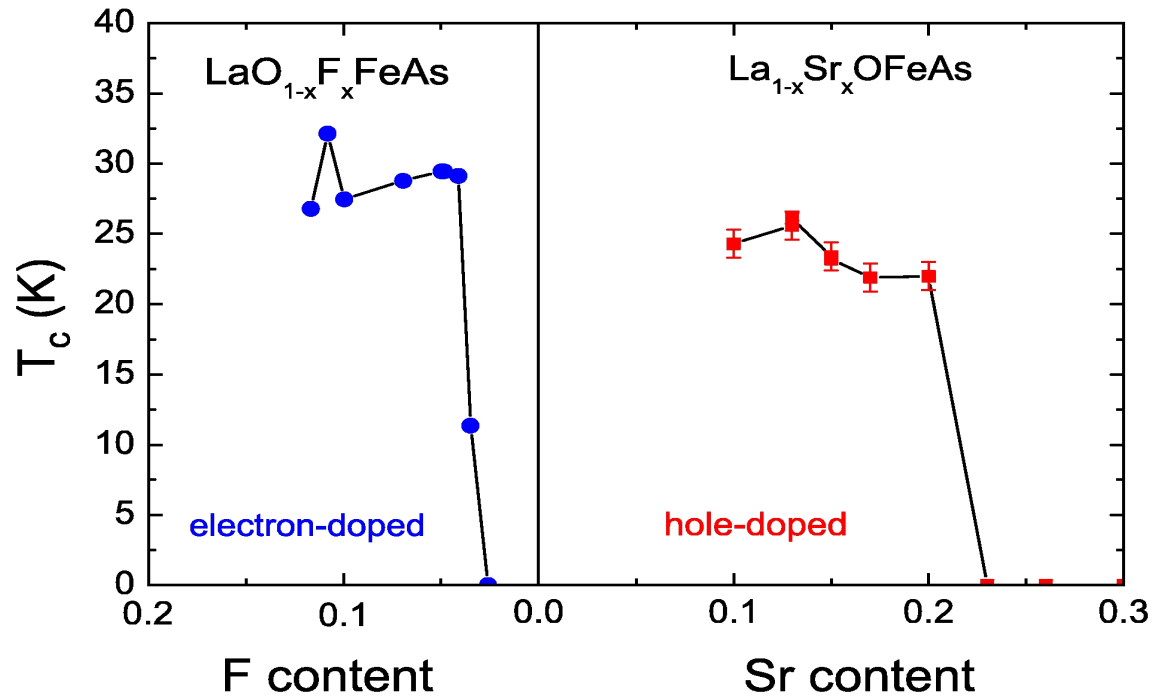
# Correlated covalent insulators FeSi and FeSb<sub>2</sub>



Temperature increase results in transition from nonmagnetic covalent insulator to bad metal with local moments. Electron doping leads to divergence of susceptibility for low T indicating ferromagnetic instability



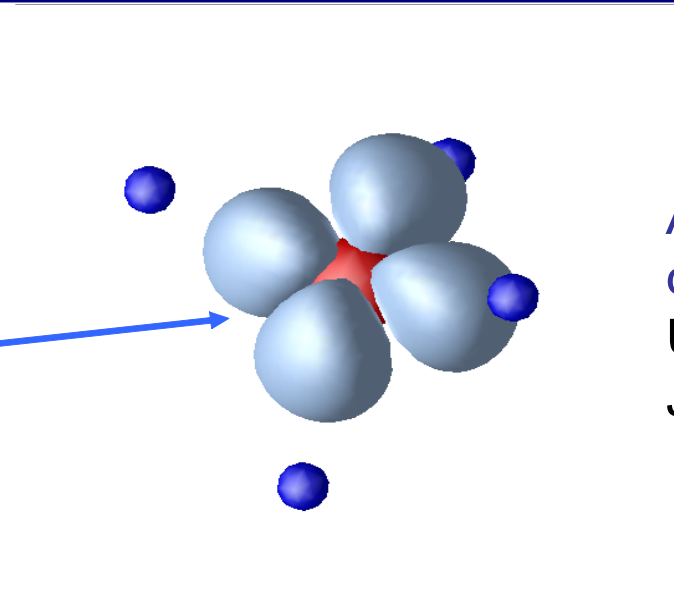
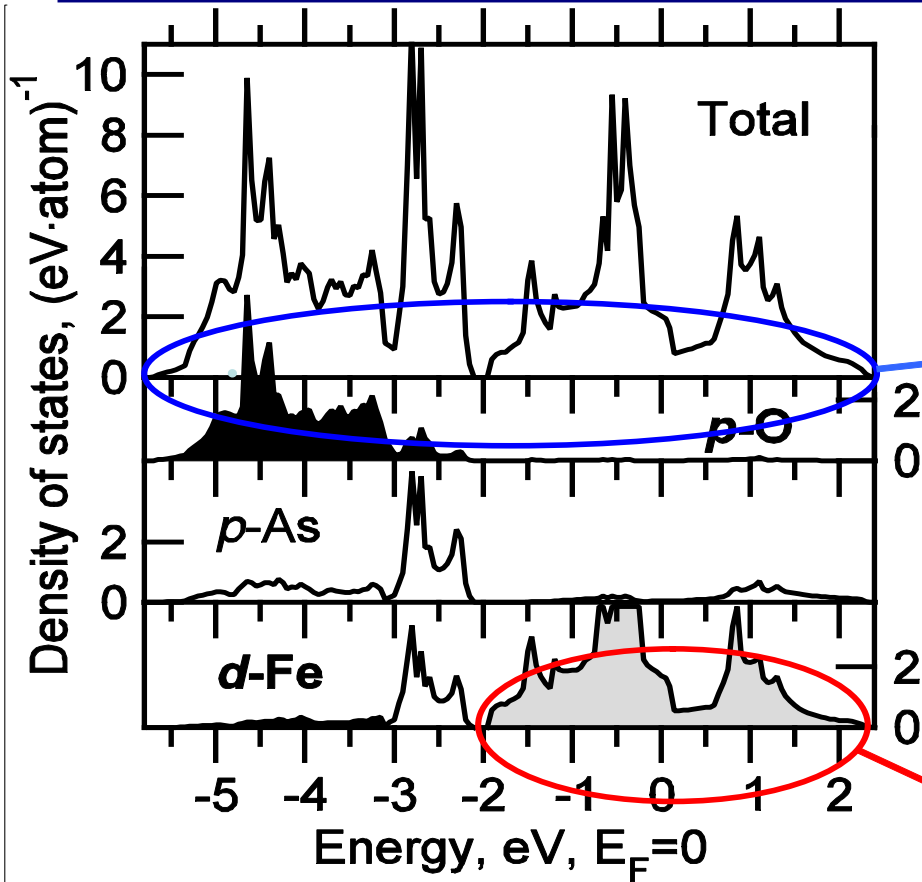
# Novel superconductor LaOFeAs



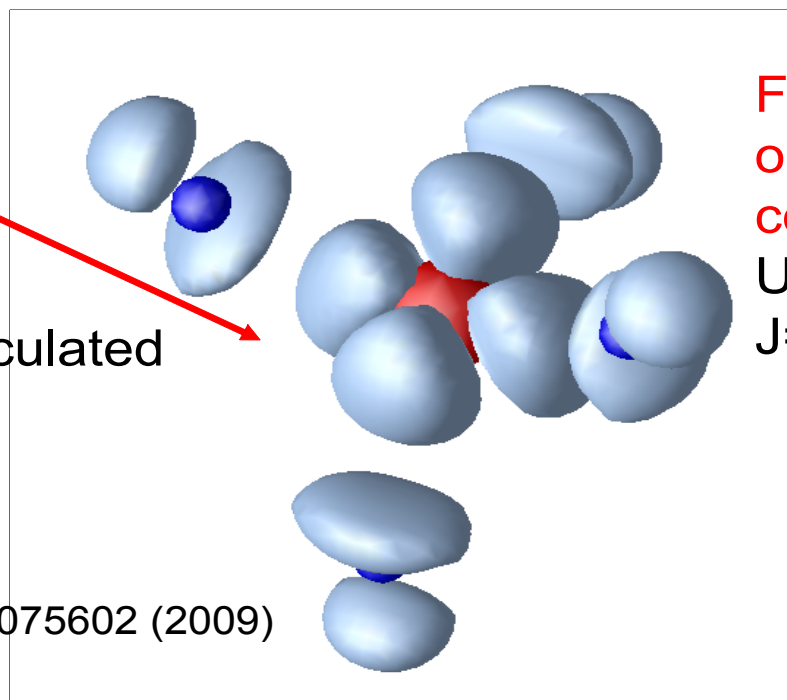
$T_c=26\text{K}$  for F content  $\sim 11\%$

Y. Kanamura *et al.* J. Am. Chem. Soc. 130, 3296 (2008)

# Novel superconductor LaOFeAs



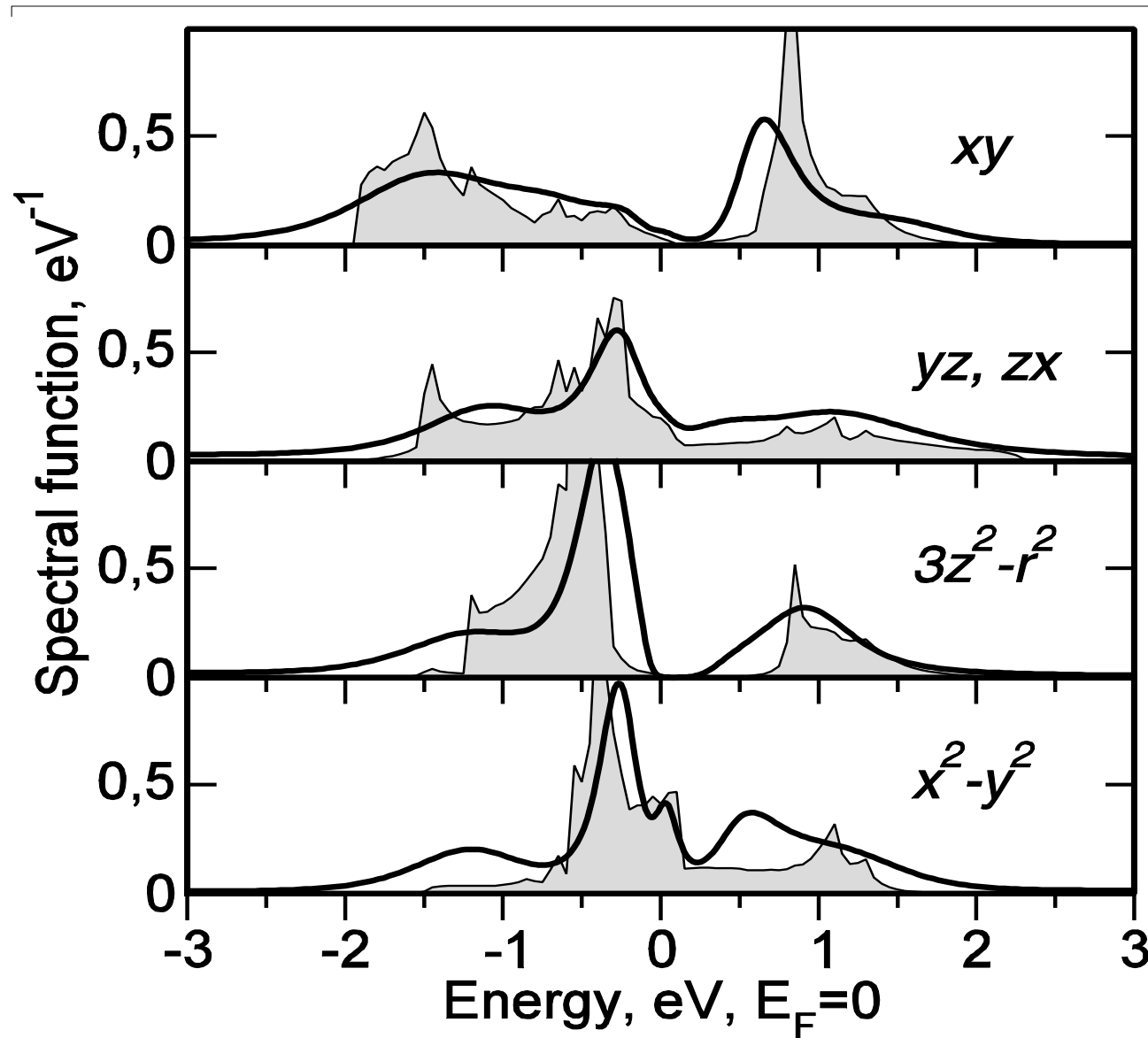
All bands WF  
constrain DFT  
 $U=3.5$  eV  
 $J=0.8$  eV



Fe3d band  
only WF  
constrain DFT  
 $U=0.8$  eV  
 $J=0.5$  eV

$d(x^2-y^2)$  Wannier functions (WF) calculated  
for all bands (O2p,As4p,Fe3d) and  
for Fe3d bands only

# Novel superconductor LaOFeAs



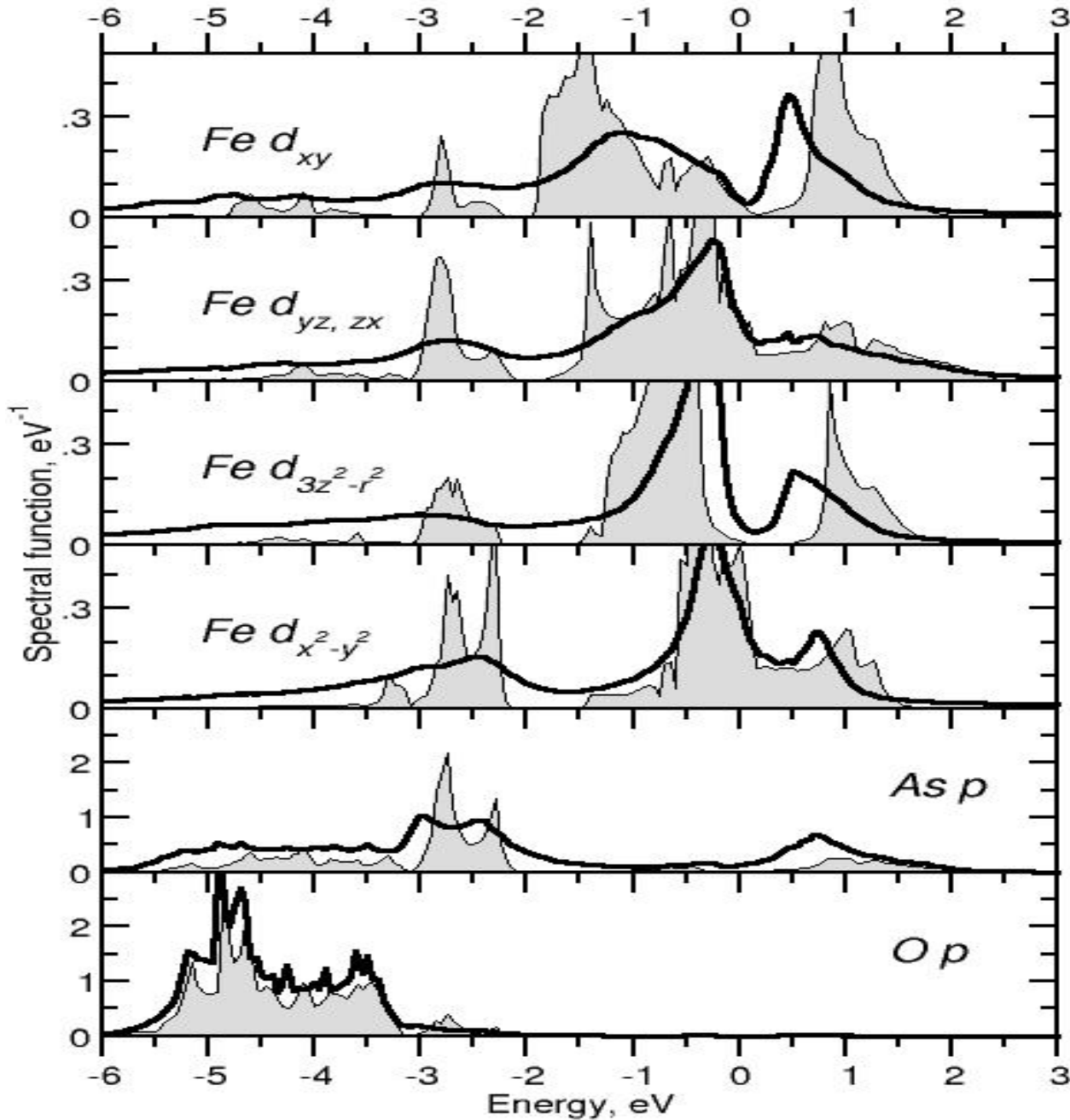
DMFT results for Hamiltonian  
and Coulomb interaction  
parameters calculated  
with Wannier functions  
for Fe3d bands only

$U=0.8$  eV

$J=0.5$  eV

*Weakly correlated  
regime!*

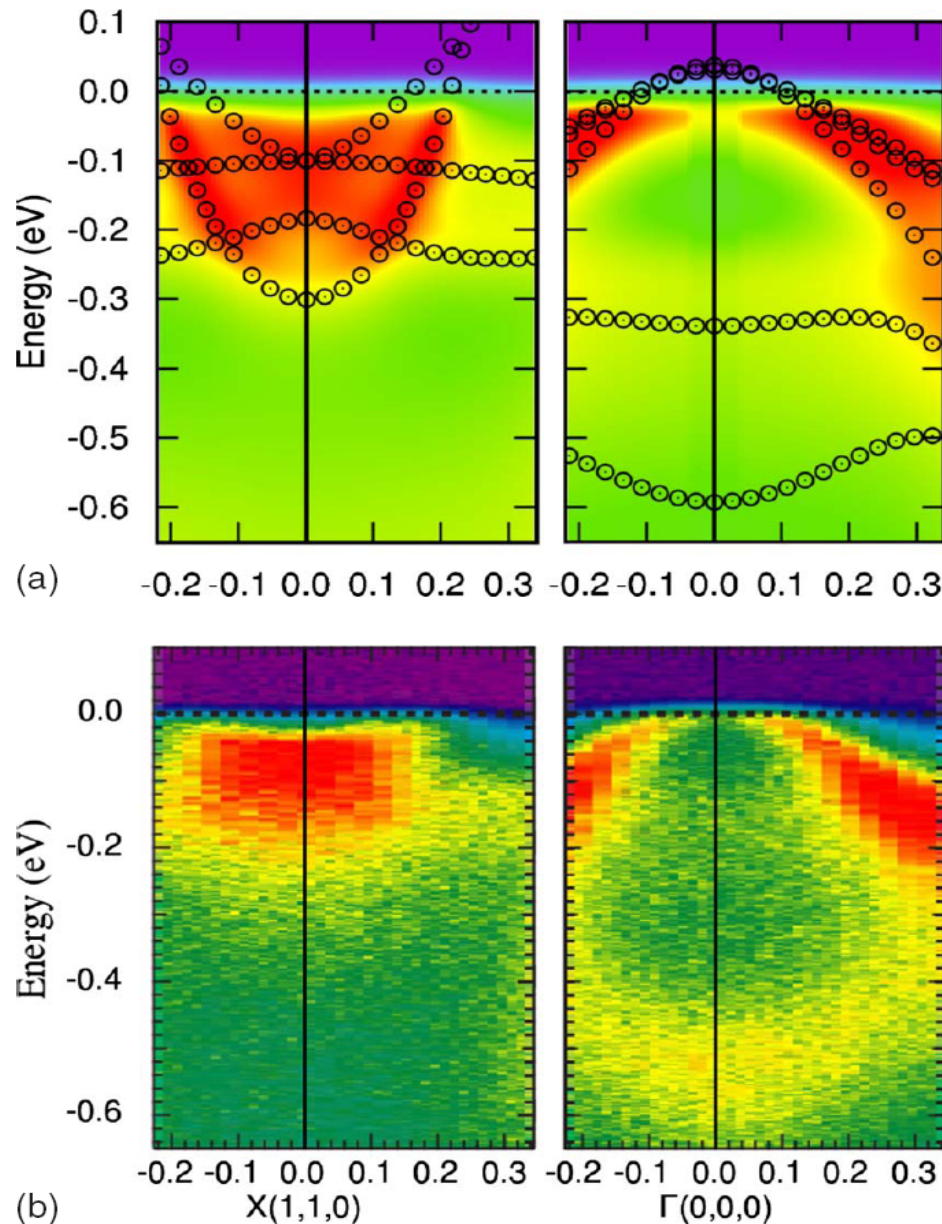
# Novel superconductor LaOFeAs



DMFT results for Hamiltonian and Coulomb interaction parameters calculated with Wannier functions for all bands (O2p, As4p, Fe3d)  
 $U=3.5$  eV  
 $J=0.8$  eV

*Weakly correlated regime!*

# ARPES for novel superconductor $\text{BaFe}_2\text{As}_2$



The  $\mathbf{k}$ -resolved total spectral function  $A(\mathbf{k}, \omega)$  of  $\text{BaFe}_2\text{As}_2$  near the  $\Gamma$  and  $X$  points in the Brillouin zone.

Upper panel: LDA+DMFT spectral function including the renormalized band structure circles obtained by plotting the peak positions of the spectral function  $A(\mathbf{k}, \omega)$ .

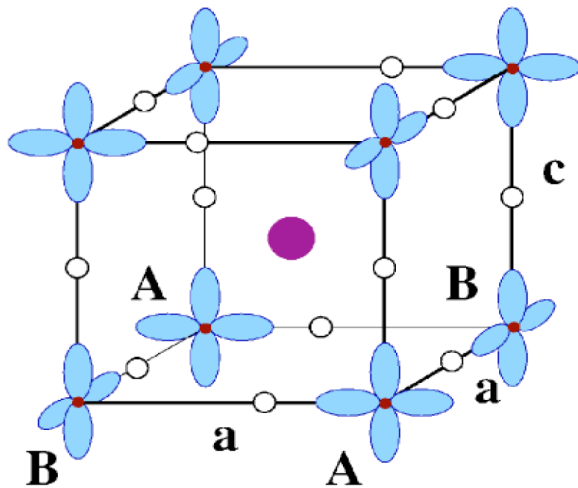
Lower panel: The corresponding experimental ARPES intensity map.

S. L. Skornyakov et al, Phys. Rev. B 80, 092501 (2009)

# Correlations and lattice distortion: $\text{KCuF}_3$

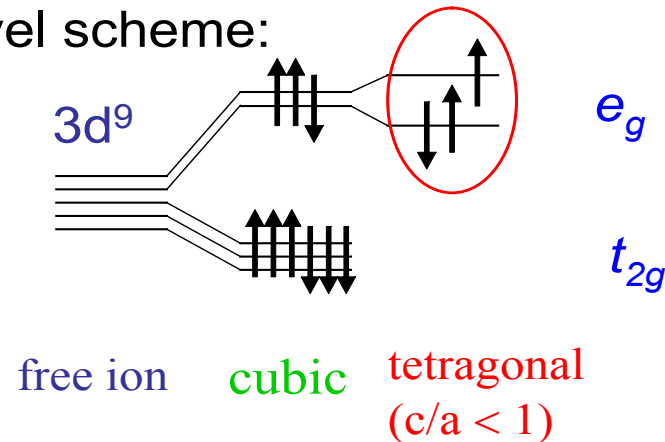
## $\text{KCuF}_3$ : a prototype $e_g$ ( $3d^9$ ) Jahn-Teller system

Crystal structure and  
Orbital order (OO):

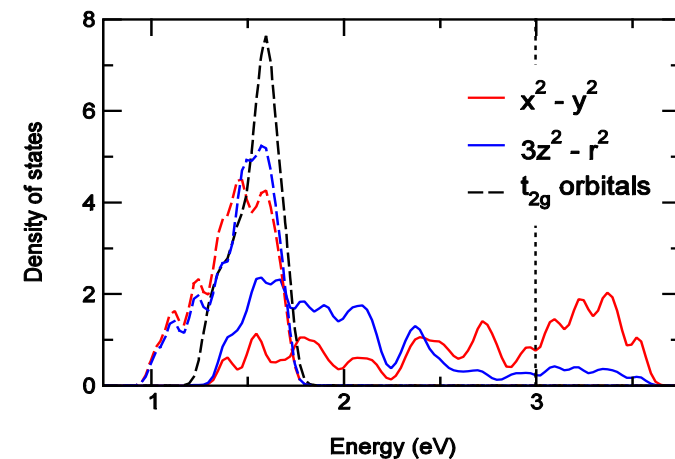


- pseudo cubic perovskite  $I4/mcm$
- cooperative JT distortion below 1000 K
- $N_{eff}$  temperature  $\sim 38$  K
- $d_{x^2-y^2}$  hole antiferroorbital ordering

d-level scheme:



GGA (Cu 3d) density of state:



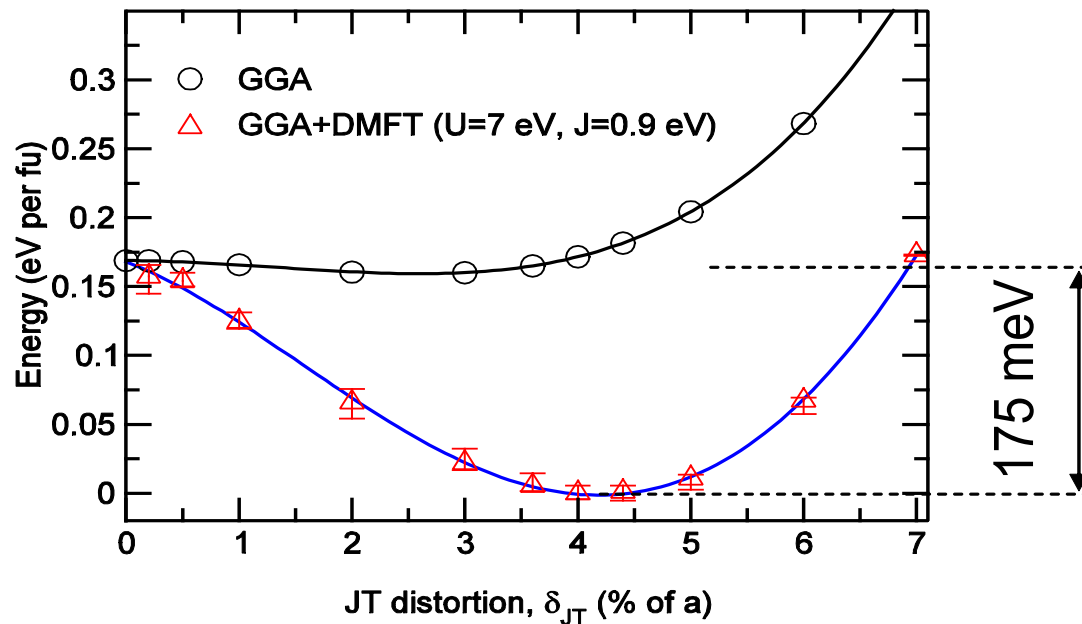
metallic solution  $\rightarrow$  inconsistent with exp

# Correlations and lattice distortion: $\text{KCuF}_3$

## KCuF<sub>3</sub>: GGA+DMFT results

$$U = 7.0 \text{ eV}, J = 0.9 \text{ eV}$$

Total energy:



→ structural relaxation due to electronic correlations !

GGA:

- *metallic* solution
- total energy almost **const** for JT distortion < 4 %
- **no JT distortion** (orbital order) for  $T > 100 \text{ K}$  !

→ inconsistent with experiment

GGA+DMFT:

- *paramagnetic* insulator
- energy gain of  $\sim 175 \text{ meV}$
- **antiferro-orbital order**
- **optimal** JT distortion at **4.2 %**
- JT distortion **persists** up to **1000 K** (melting tem-re)

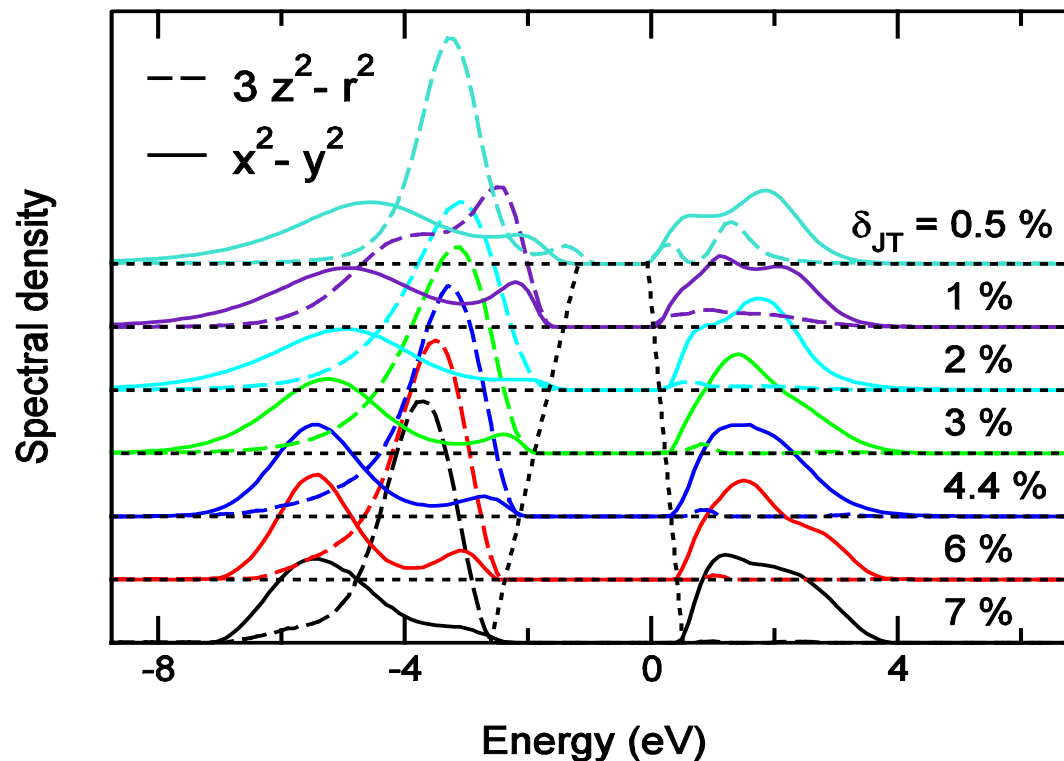
→ in **good agreement** with **exp**

# Correlations and lattice distortion: $\text{KCuF}_3$

## $\text{KCuF}_3$ : GGA+DMFT results

$$U = 7.0 \text{ eV}, J = 0.9 \text{ eV}$$

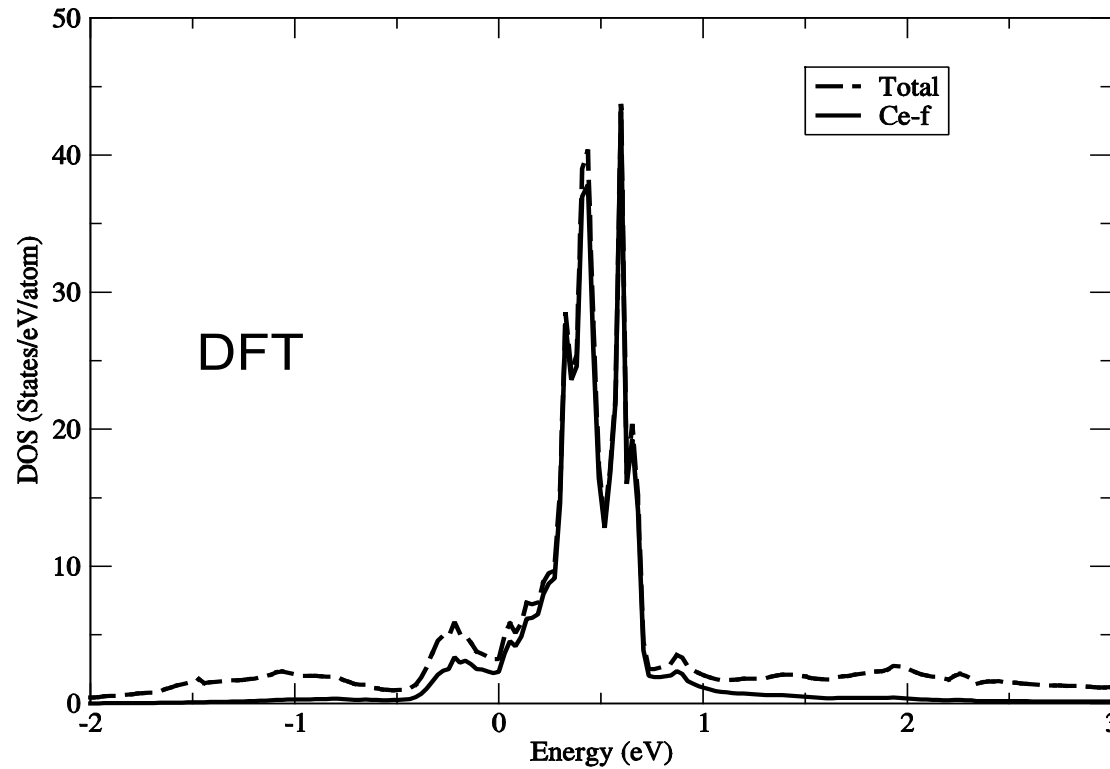
$e_g$  spectral density:



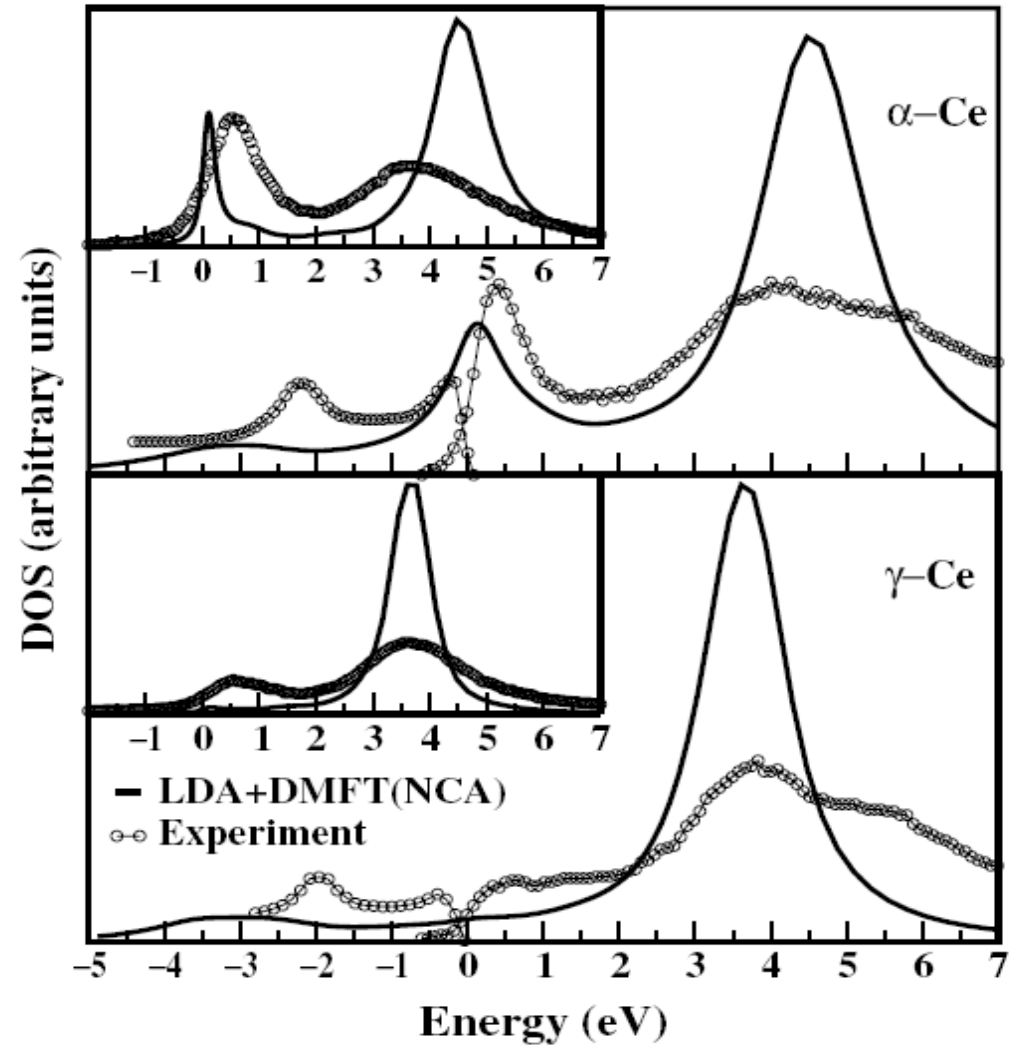
- *paramagnetic* insulator
- gap gradually increase with the JT distortion
- but large even at  $\sim 0.5\%$
- hole orbital polarization on  $x^2 - y^2$  (in LCS with  $z$ -axis along the longest Cu-F bond)



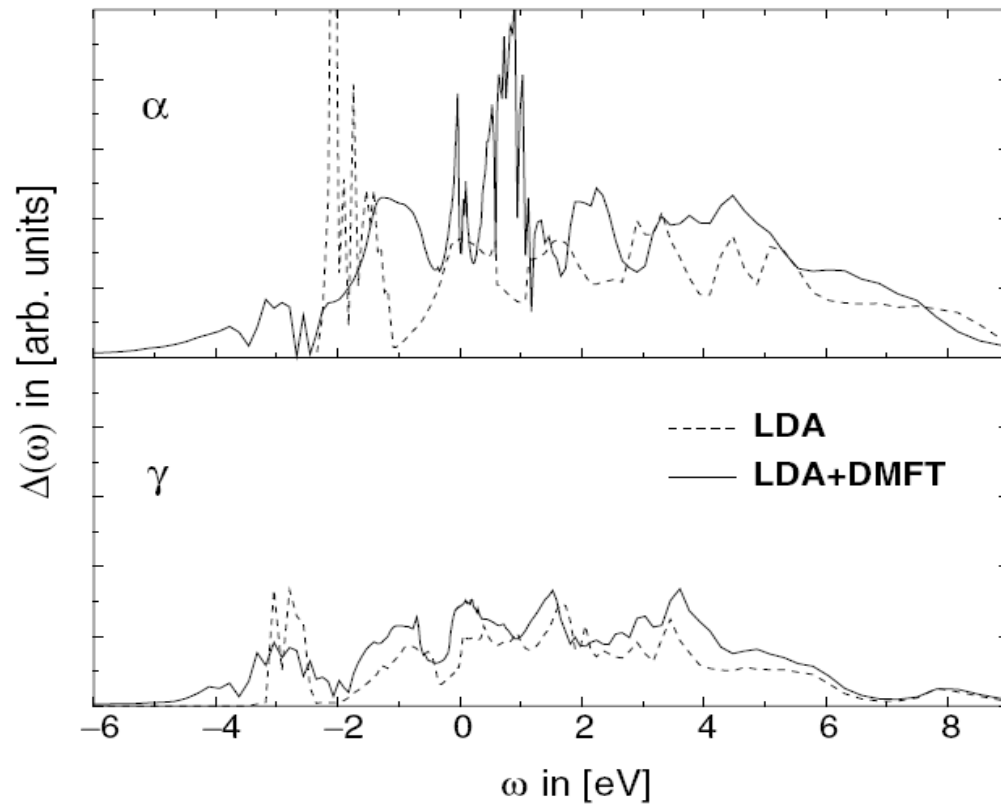
# ons localization in Ce



Ce  $\alpha - \gamma$  transition with 15% volume change.  
Kondo temperature  $T_K$  1000K ( $\alpha$ ), 30K ( $\gamma$ )



# f-electrons localization in Ce



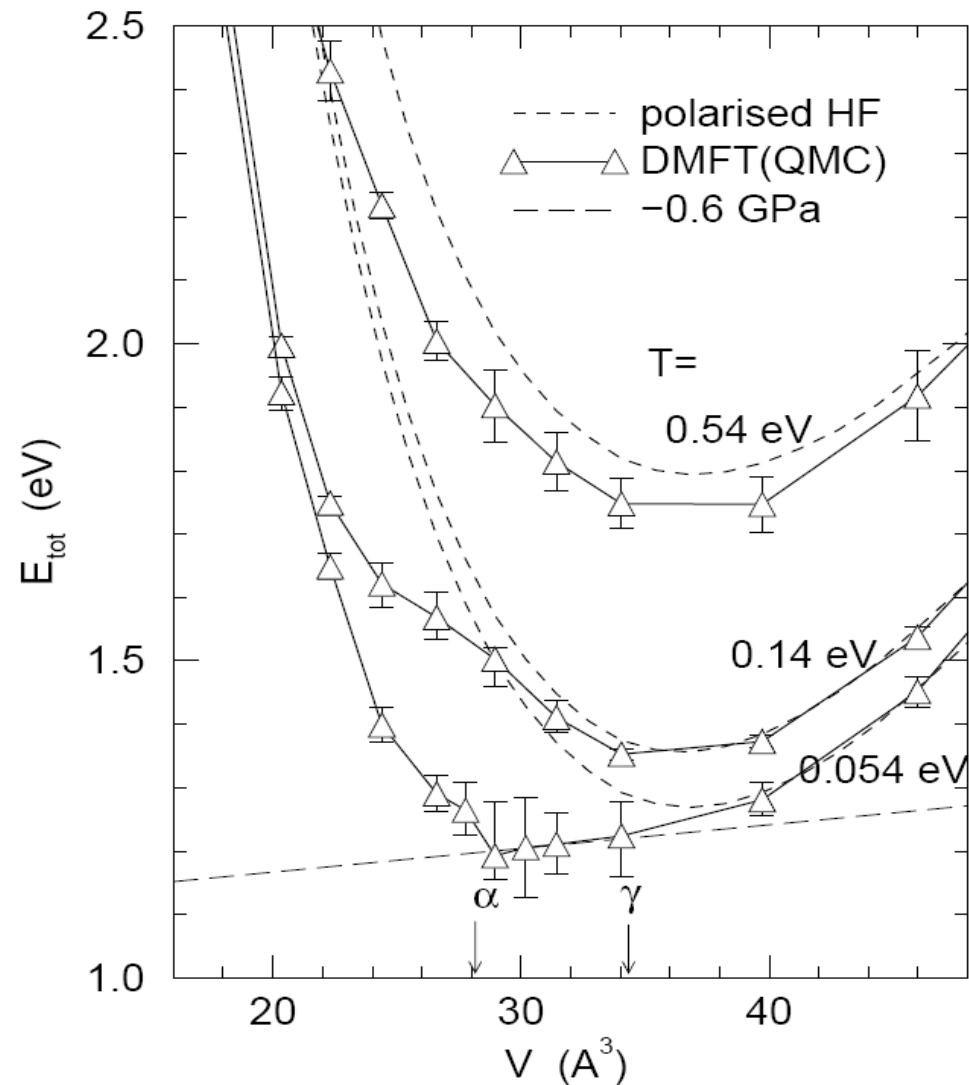
Hybridization of the site orbitals with the rest of the crystal in effective single impurity model is described by effective hybridization function  $\Delta(i\omega_n)$  or effective non-interacting bath Green function

$$G_0(i\omega_n):$$

$$\mathcal{G}_0(i\omega_n) = (i\omega_n + \mu - \Delta(i\omega_n))^{-1}$$

$$\mathcal{G}_0^{-1}(i\omega_n) = G^{-1}(i\omega_n) + \Sigma(i\omega_n)$$

# f-electrons localization in Ce



Total energy for Ce calculated in LDA+DMFT(QMC) (solid line) and in polarized Hartree-Fock approximation (dashed line) for three temperature values. Long dashed line corresponds to pressure for  $\alpha$ - $\gamma$ - transition:  $E = -P_{\text{exp}} V$ .

- ***Ab-initio* LDA+correlation Hamiltonian is defined with definition of correlated orbitals and interaction strength (U) between them based on Wannier functions representation .**
- **Static mean-field approximation lead to LDA+U method and dynamical mean-field approximation to LDA+DMFT**
- **LDA+U method describes all kinds of spin, orbital and charge order effects in Mott insulators**
- **LDA+DMFT method is adequate for paramagnetic strongly correlated metals**